

VISUALIZING MULTI-ATTRIBUTE DATA

DATA TABLES

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RECAP

you have learned about

- visual channels and marks
- that their perceptual properties matter

RECAP

➔ Magnitude Channels: Ordered Attributes


Position on common scale 

Position on unaligned scale 

Length (1D size) 

Tilt/angle 


Area (2D size) 

Depth (3D position) 

Color luminance 

Color saturation 

Curvature 

Volume (3D size) 

➔ Identity Channels: Categorical Attributes

Spatial region 

Color hue 

Motion 

Shape 

Most

Effectiveness

Least

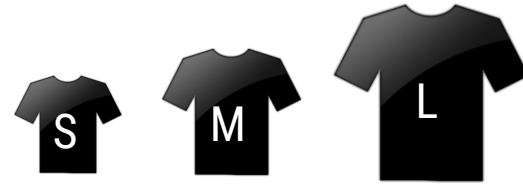
Same

Same

RECAP

DATA TYPES

ORDINAL (ranking)



NOMINAL (categorical)

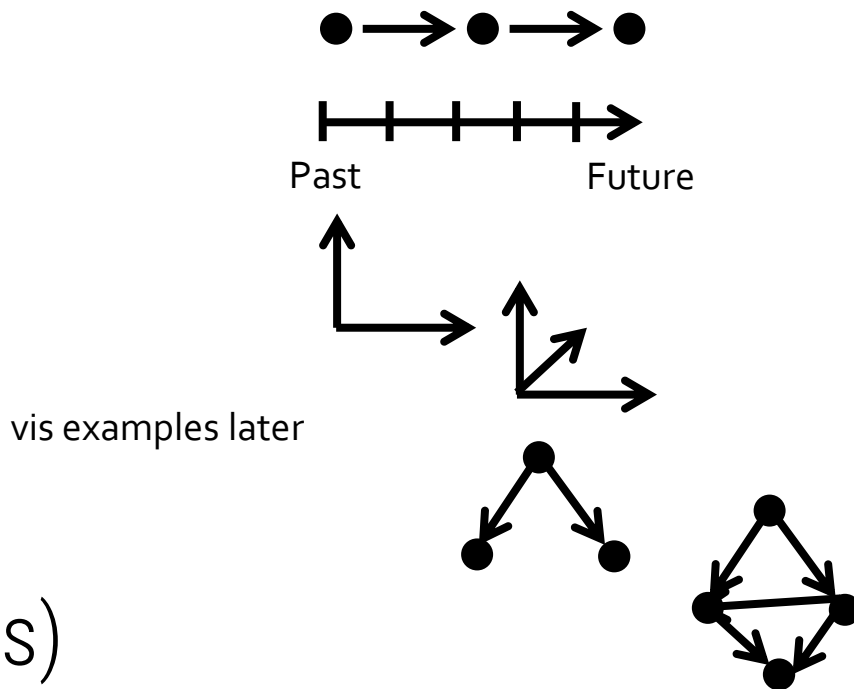


QUANTITATIVE (numerical)



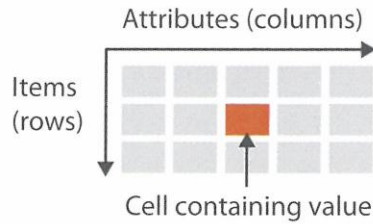
OTHER VIEWS ON DATA TYPES

- 1D (linear)
- Temporal
- 2D (maps)
- 3D
- nD (relational)
- Trees (hierarchies)
- Networks (graphs)

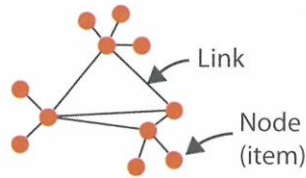


ANOTHER VIEW

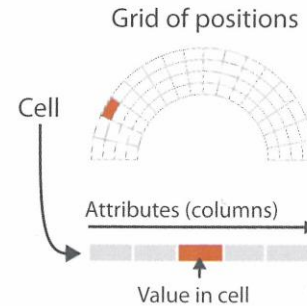
→ Tables



→ Networks



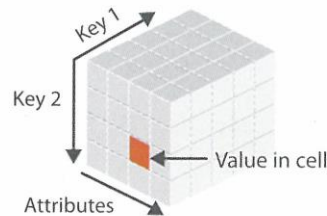
→ Fields (Continuous)



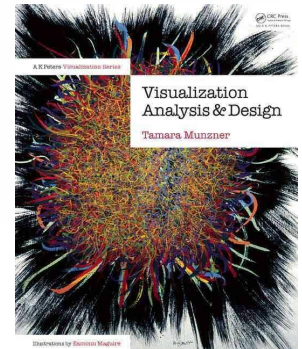
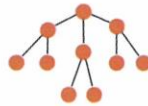
→ Geometry (Spatial)



→ Multidimensional Table



→ Trees



TODAY

How to turn something like this ... into a multi-dimensional data representation

Vélib' : Disponibilité temps réel

[Informations](#) [Tableau](#) [Carte](#) [Analyse](#) [Export](#) [API](#)

| | Code de la station | Nom de la station | Etat des stations | Etat du Totem | Nombres de bornes en station | Nombre de bornes disponibles | Nombre de vélo mécanique | Nombre vélo électrique | Achat possible en |
|----|--------------------|--------------------------------------|-------------------|---------------|------------------------------|------------------------------|--------------------------|------------------------|-------------------|
| 1 | 11037 | Faubourg Du Temple - Republique | Close | yes | 39 | 36 | 2 | 1 | yes |
| 2 | 11104 | Charonne - Robert et Sonia Delauney | Operative | yes | 20 | 17 | 2 | 1 | no |
| 3 | 14111 | Cassini - Denfert-Rochereau | Close | yes | 25 | 25 | 0 | 0 | yes |
| 4 | 12109 | Mairie du 12ème | Operative | yes | 30 | 30 | 0 | 0 | no |
| 5 | 5110 | Lacépède - Monge | Operative | yes | 23 | 16 | 6 | 1 | yes |
| 6 | 17038 | Grande Armée - Brunel | Operative | yes | 62 | 40 | 20 | 2 | yes |
| 7 | 10152 | Gare du Nord - Place de Valenciennes | Operative | yes | 25 | 18 | 6 | 1 | yes |
| 8 | 13007 | Le Brun - Gobelins | Operative | yes | 48 | 47 | 1 | 0 | yes |
| 9 | 41301 | Bois de Vincennes - Gare | Operative | yes | 51 | 39 | 8 | 4 | yes |
| 10 | 31024 | Romainville - Vaillant-Couturier | Operative | yes | 38 | 35 | 2 | 1 | no |
| 11 | 15028 | Grenelle - Dr Finlay | Operative | yes | 71 | 63 | 7 | 2 | yes |
| 12 | 16118 | Michel-Ange - Parent de Rosan | Operative | yes | 26 | 25 | 0 | 1 | no |
| 13 | 20035 | Pyrénées - Ménilmontant | Operative | yes | 26 | 24 | 0 | 2 | no |
| 14 | 10027 | Dunkerque - Alsace | Operative | yes | 18 | 10 | 8 | 0 | no |
| 15 | 8048 | Marceau - Chaillot | Operative | yes | 21 | 8 | 9 | 4 | no |
| 16 | 14013 | Liard - Amiral Mouchez | Operative | yes | 1 | 1 | 1 | 0 | yes |
| 17 | 5024 | Place Monge | Close | yes | 21 | 21 | 0 | 0 | no |
| 18 | 7018 | Ségur - d'Estrées | Operative | yes | 19 | 8 | 10 | 1 | no |
| 19 | 10029 | Dunkerque - Rocroy | Operative | yes | 23 | 16 | 6 | 1 | no |
| 20 | 8009 | Gare Saint-Lazare - Isly | Operative | yes | 27 | 14 | 10 | 3 | yes |
| 21 | 8036 | Lisbonne - Monceau | Operative | yes | 33 | 7 | 25 | 1 | yes |
| 22 | 17040 | Pereire - Ternes | Operative | yes | 48 | 44 | 2 | 2 | yes |
| 23 | 31708 | Noisy le Sec - Jean-Baptiste Clément | Operative | yes | 22 | 21 | 0 | 1 | no |
| 24 | 10105 | Mazagran - Bonne Nouvelle | Operative | yes | 26 | 15 | 9 | 2 | yes |

SOME INSPIRING EXAMPLES

TOP SONGS

by album
spotify popularity

80

song types
energy & valence

5

10

15

us album sales rank

petals = E Street member

TOP ALBUMS

the history of BRUCE SPRINGSTEEN

Over a 45 year career Bruce Springsteen has released over 200 songs and 17 studio albums. Born in Long Branch NJ and raised in working class Freehold NJ he is known for his poetic lyrics and energetic stage performances. He has sold 135 million albums worldwide. The following is a musical history of Bruce Springsteen using excerpts from his autobiography "Born to Run", interviews, and Wikipedia.

John Hammond of Columbia Records signed Bruce after he played Saint in the City for him in his office. Columbia wanted a solo artist like Bob Dylan and James Taylor but Bruce insisted on recording with a band to get the new sound he was pursuing: "an amalgam of good song-writing mixes with a soul-and-R&B influenced, rock music" as Bruce said in his autobiography "Born to Run".

Greetings from Asbury Park, N.J. is Bruce's debut studio album released on January 5, 1973. After completing the album Clive Davis of Columbia Records was worried there were no hits. So Bruce wrote "Spirit in the Night" and "Blinded by the Light" the next day at the beach. They were the two biggest hits on the album. Early reviews of the album made favorable comparisons to Dylan.

The Wild, the Innocent & the E Street Shuffle is Bruce's second album released on November 11, 1973. Bruce recorded this album over 3 months at the 914 Sound Studios in Blauvelt NY. Bruce and Clarence Clemons slept in a tent behind the studio to save money. Like Greetings from Asbury Park the album was not a commercial success but received positive

TOP SONGS

by album
spotify popularity

80

song types
energy & valence

5

10

15

us album sales rank

petals = E Street member

TOP ALBUMS

Born to Run
1975

Darkness on Edge of Town
1978

The River
1980

Nebraska
1982

Born in the USA
1984

Tunnel of Love
1987

Human Touch
1992

Lucky Town
1992

Ghost of Tom Joad
1995

The Rising
2002

Devils & Dust
2005

Magic
2007

Working on Dream
2009

Wrecking Ball
2012

the history of BRUCE SPRINGSTEEN

Song
Popularity
by Album

Single
Song

Song Types
Energy & Valence
Size = # Songs

High Energy
High Valence

Album
Sales Rank

Bar Length =
Album Duration

Non-Platinum
Platinum
Multi Platinum

E Street Members
on the Album
in order of appearance

Max Weinberg
on Album

Sources Spotify API via @plamer (popularity, song attributes), Wikipedia (narrative, album sales) and "Born to Run" book (narrative)

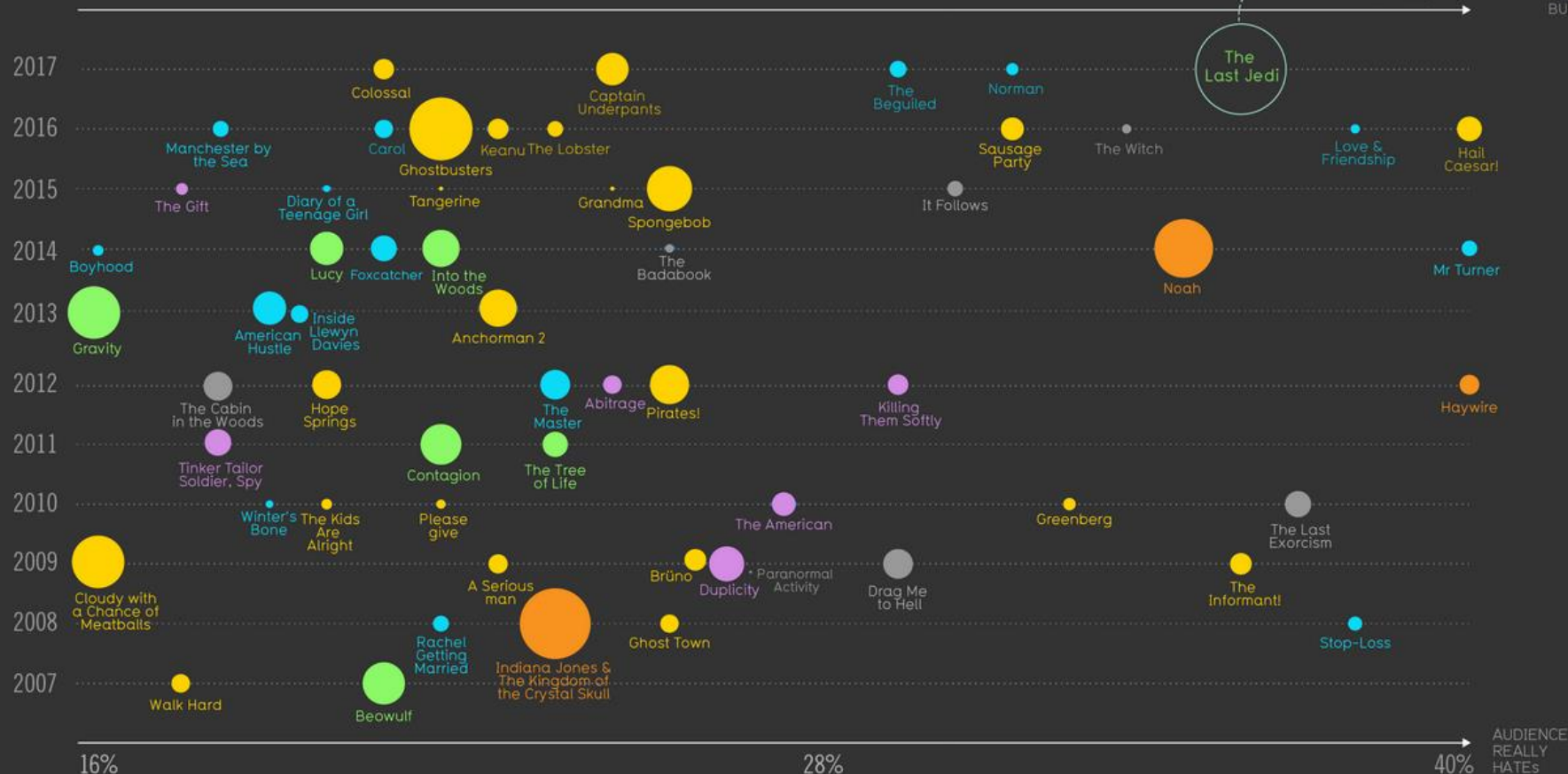
created by Adam McCann @adamemccann | inspired by Federica Fragapane @fedfragapane & Giorgia Lupi @giorgialupi

How to Read

Movies Critics Loved, But Audiences Really Didn't

% gap between audience & critics 'rotten tomatoes' score

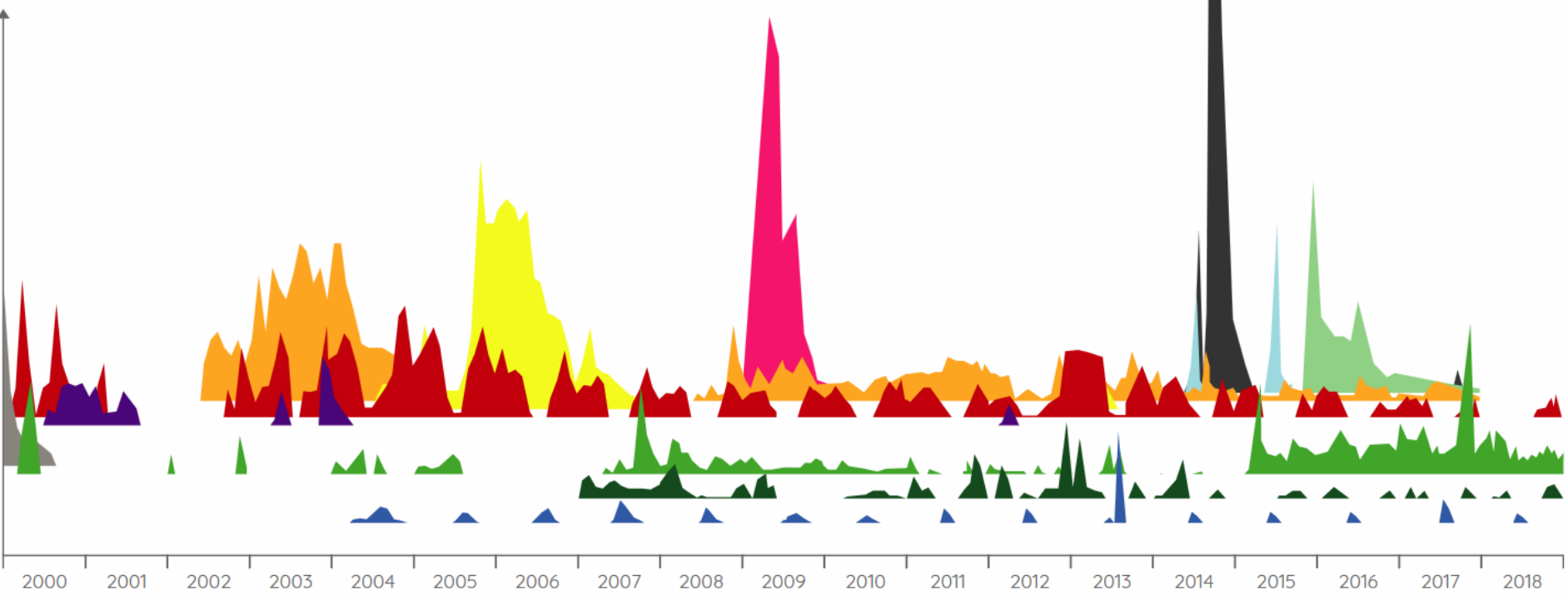
biggest budget movie with the most dramatic split between critics & audience opinion



Mountains Out of Molehills

A timeline of media-inflamed fears

INTENSITY
(no. of news media mentions)



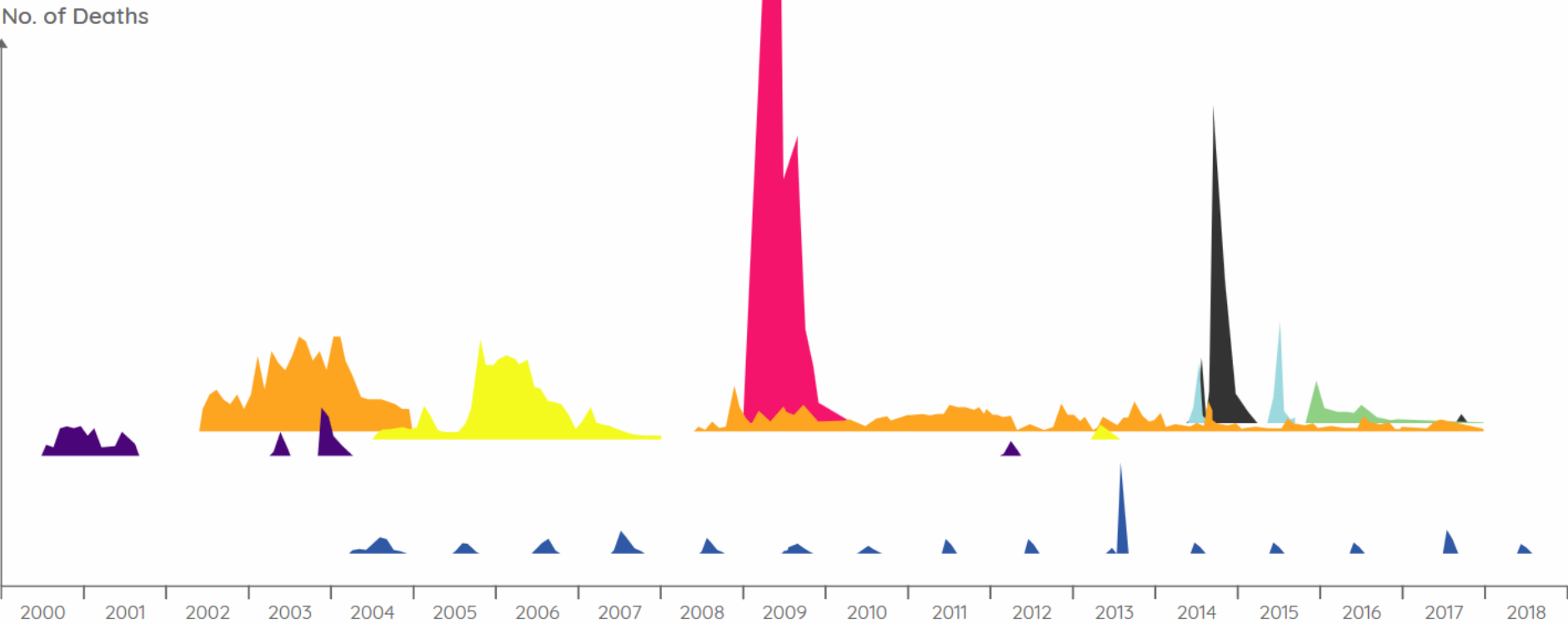
ASTEROIDS BIRD FLU EBOLA KILLER WASPS MAD COW DISEASE MERS MILLENNIUM BUG SARS SWINE FLU VACCINES & AUTISM VIOLENT VIDEO GAMES ZIKA

David McCandless, Fabio Bergamaschi // source: Google Trends

☐ align to baseline ☐ scale to fit Ebola ☐ scale by deaths

Mountains Out of Molehills

A timeline of media-inflamed fears



ASTEROIDS BIRD FLU EBOLA KILLER WASPS MAD COW DISEASE MERS MILLENNIUM BUG SARS SWINE FLU VACCINES & AUTISM VIOLENT VIDEO GAMES ZIKA

David McCandless, Fabio Bergamaschi // source: [Google Trends](#)

☐ align to baseline ☐ scale to fit Ebola ☒ scale by deaths

THE MANY MOONS OF JUPITER

IN 1610, Galileo Galilei gazed up through his telescope in the direction of Jupiter. In that moment he likely became the first person to see a moon other than our own, as light that had left the vicinity of the gas giant around half an hour earlier crashed into his pupils and revealed four dotted silhouettes. These Galilean moons, one of which is even larger than the planet Mercury, became the opening entries into a collection that is still increasing today. In fact in 2018, 407 years after the Italian polymath made his discovery, scientists confirmed the existence of

12 more moons locked in slow rotation with the largest planet in our solar system. These newly found satellites form part of a diverse family, many of which share little commonality other than their gravitational anchor. Their orbital shapes range from near perfect circles to highly eccentric and inclined. Their scales vary hugely, from the size of planets to just a kilometer across. Some may have been asteroids captured by Jupiter's powerful gravitational pull, while others were likely a by-product of the very formation of the planet itself.

This data visualization displays every currently known moon of Jupiter, each featuring the year of discovery, discoverer and a representation of scale. Additionally, on the right are some additional insights about the moons. Finally, while all information is correct as of 2018, scientists are finding new wonders in our solar system every day; so who knows how many new Jovian moons are out there right now, held in endless revolutions, just waiting for eyes to meet them for the first time?

79
Moons discovered as of 2018

18
The number of moons that are prograde

61
The number of moons that are retrograde

The Voyager probes, launched in 1977, discovered three of Jupiter's large inner moons

99.997%
The approx. % of the total mass in orbit around Jupiter that comes from the four Galilean moons

One of the newly discovered moons has an odd prograde orbit which sees its path cross several other retrograde moons. This means a collision is very likely, although scientists predict it could take another billion years to actually happen

As of 2018, five of the moons are considered lost

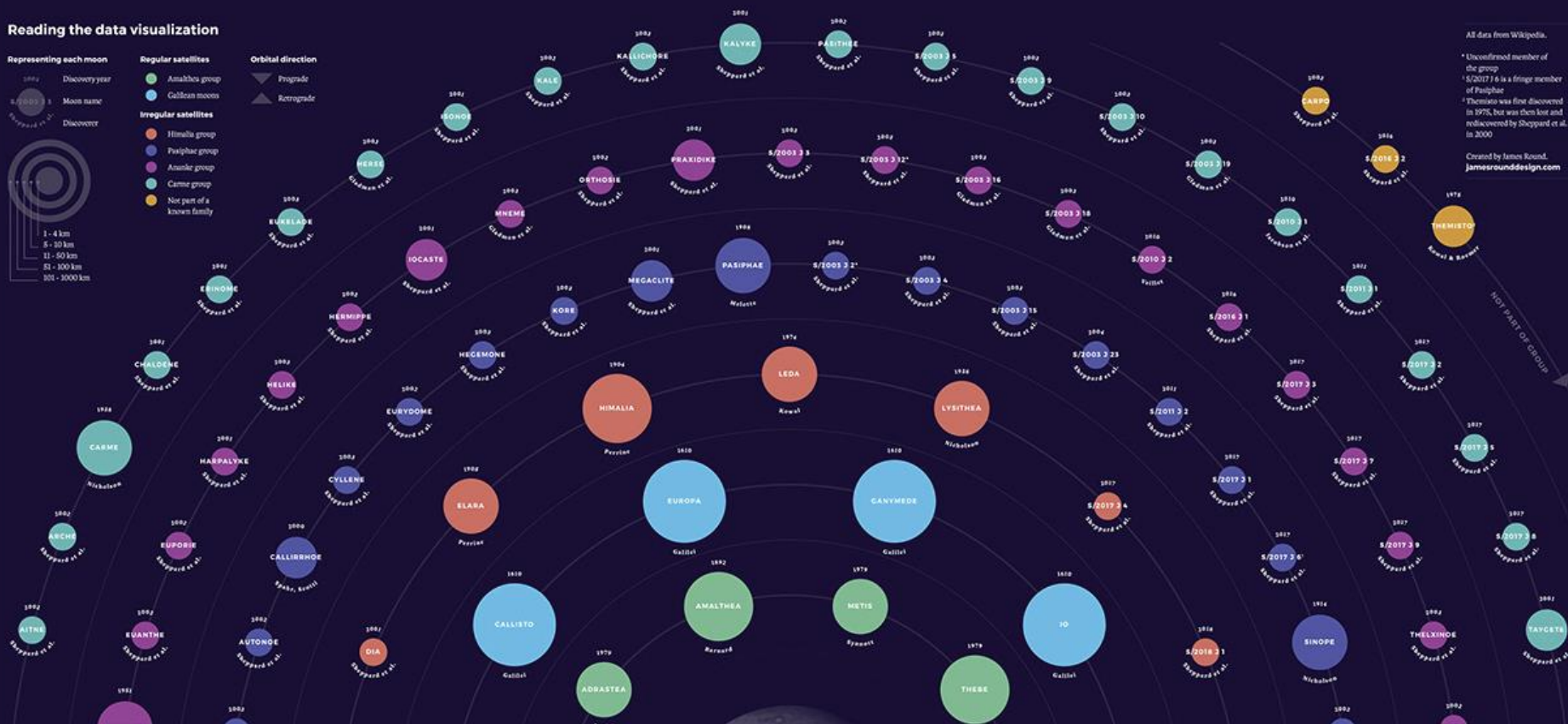
Ganymede, Jupiter's largest moon, is actually 8% larger than the planet Mercury, making it the 9th largest object in our solar system

It's thought that several of the larger moons could feature subsurface oceans, leading to some exciting possibilities about the existence of life there

54
The most moons have been found by a team led by Scott Sheppard

A German astronomer called Simon Markus independently discovered the four Galilean moons at the same time as Galileo. While he didn't receive the title of discoverer, he is responsible for their names, which are still used today

Reading the data visualization



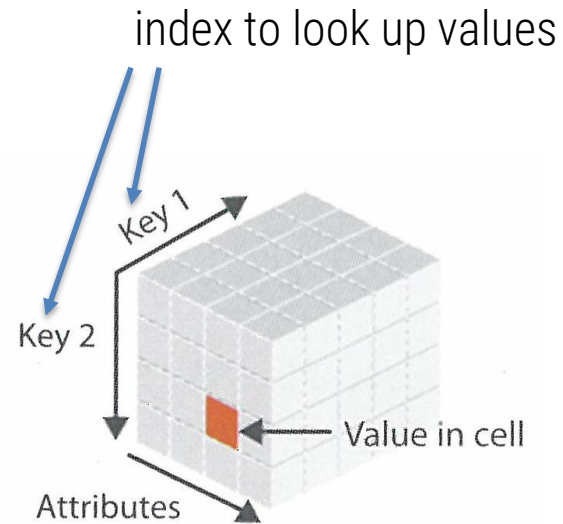
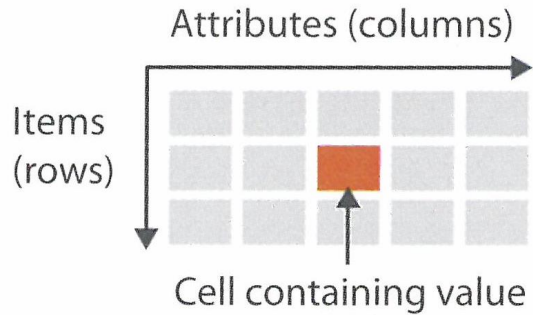
All data from Wikipedia.

* Unconfirmed member of the group
 † S/2017 16 is a fringe member of Pasiphae
 ‡ Themisto was first discovered in 1976, but was then lost and rediscovered by Sheppard et al. in 2000

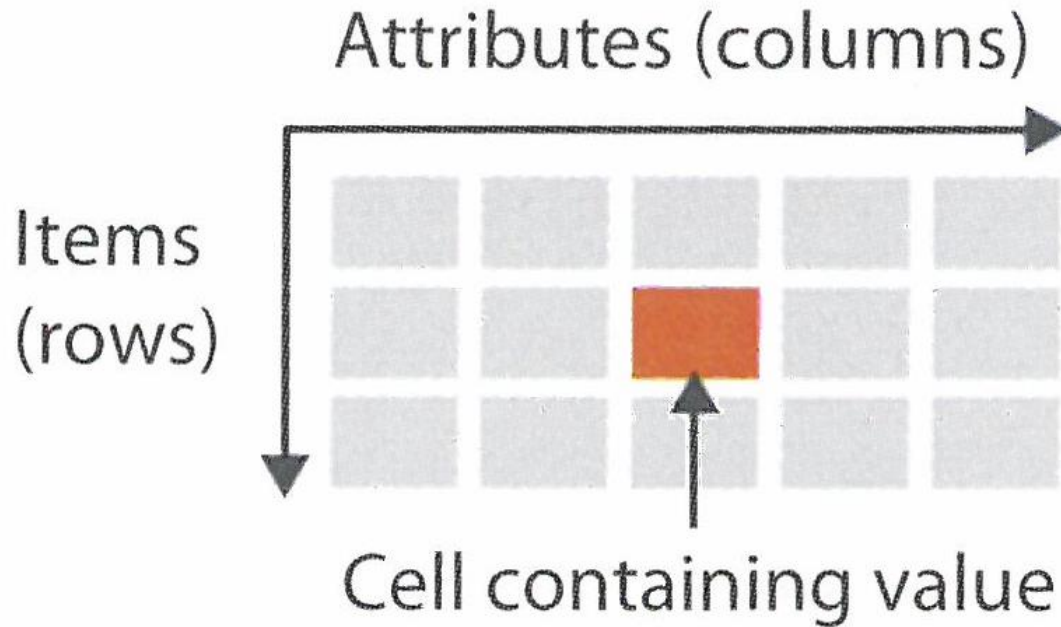
Created by James Round, jamesrounddesign.com

BACK TO THE BASICS

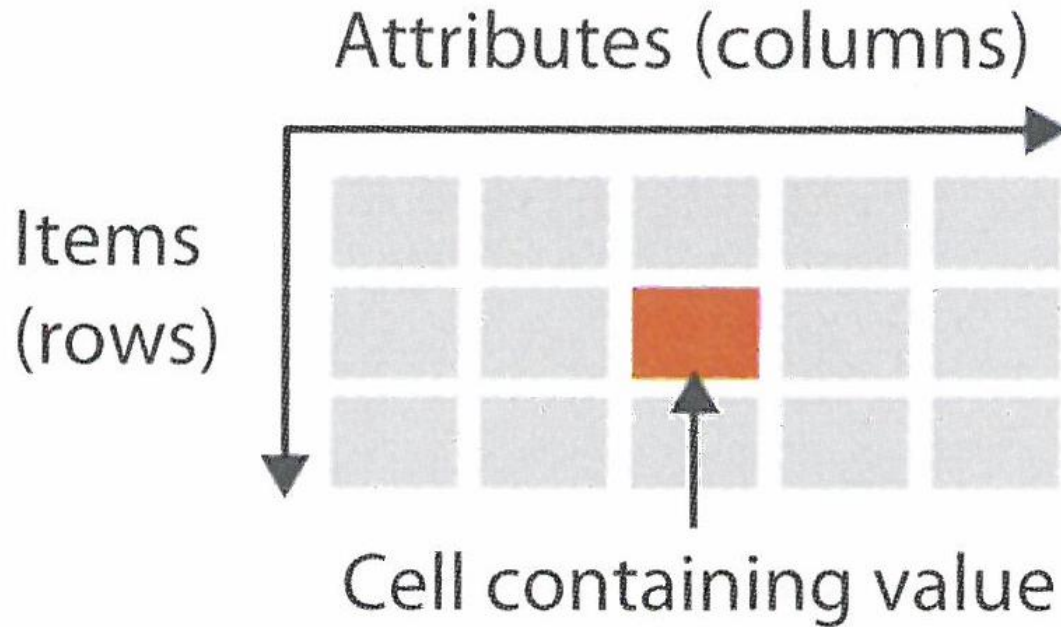
DATA TABLES - TERMINOLOGY



WHAT COULD BE THE KEY HERE?



WHAT DATA TYPE IS SUITABLE FOR A KEY?



KEYS VS. VALUES

key attributes are also sometimes called:

- independent attribute
- dimension

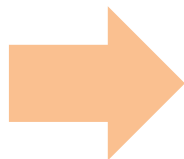
value attributes are also sometimes called:

- dependent attribute
- measure

LEVELS

= unique values for a categorical or ordered attribute

| Conference | Year | Paper.Title |
|------------|------|---------------------------|
| InfoVis | 2015 | A comparative study ... |
| InfoVis | 2015 | A Linguistic Approach... |
| InfoVis | 2015 | A Psychophysical Inv... |
| InfoVis | 2015 | A Simple Approach fo... |
| InfoVis | 2015 | Acquired Codes of Me... |
| InfoVis | 2015 | AggreSet: Rich and Sc... |
| InfoVis | 2015 | AmbiguityVis: Visuali... |
| InfoVis | 2015 | Automatic Selection ... |
| InfoVis | 2015 | Beyond Memorability... |
| InfoVis | 2015 | Beyond Weber's Law:... |
| InfoVis | 2015 | Evaluation of Parallel... |
| InfoVis | 2015 | Guidelines for Effecti... |
| InfoVis | 2015 | High-Quality Ultra-Co... |
| InfoVis | 2015 | HOLA: Human-like Ort... |
| InfoVis | 2015 | How do People Make ... |



CONFERENCE:
InfoVis, Vis, SciVis, VAST

YEAR:
1990 – 2015

PAPER.TITLE:
>2500 different

VISPUBDATA

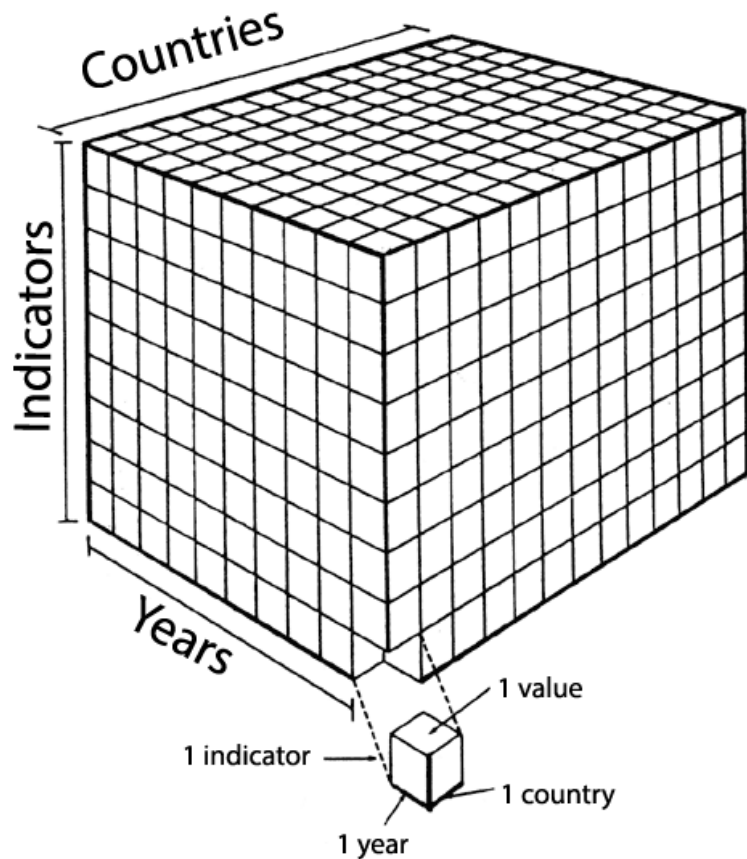
ATTRIBUTES



ITEMS

| | # | Abc | Abc | Abc | # | # | Abc | Abc | Abc | Abc | Abc | Abc | Abc | Abc |
|---------|------|---------------------------|----------------------|-------------------------|------------|-----------|-----------------------|---------------------------|-----------------------------|----------------------------|-----------------------------|----------------------|----------------------------|-----------------------------|
| | Year | Paper.Title | Paper.DOI | Link | First.page | Last.page | Paper.type..C.conf... | Abstract | Author.Names | First.Author.Affilia... | Deduped.author.n... | References | Author.Keywords | OCR.Authors |
| | 2015 | A comparative study ... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 619 | 628 | J | RadViz and star coord... | Rubio-Sanchez, M.; Ra... | ... | Rubio-Sanchez, M.; Ra... | 10.1109/VAST.2010... | RadViz, Star coordina... | Rubio-S ' Anchez, Ma... |
| | 2015 | A Linguistic Approach... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 698 | 707 | J | When data categorie... | Setlur, V.; Stone, M. C. | ; | Setlur, V.; Stone, M. C. | null | Linguistics, natural la... | Setlur, Vidya; Stone, M... |
| | 2015 | A Psychophysical Inv... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 479 | 488 | J | Physical visualization... | Jansen, Y.; Hornbaek, K. | Univ. of Copenhagen, ... | Jansen, Y.; Hornbaek, K. | 10.1109/TVCG.2012... | Data physicalization, ... | Jansen, Yvonne; Hornb... |
| | 2015 | A Simple Approach fo... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 678 | 687 | J | General methods for ... | Simonetto, P.; Archam... | ;; | Simonetto, P.; Archam... | 10.1109/TVCG.2011... | Euler diagrams, Boun... | Simonetto, Paolo; Arc... |
| | 2015 | Acquired Codes of Me... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 509 | 518 | J | While information vis... | Byrne, L.; Angus, D.; W... | ;; | Byrne, L.; Angus, D.; W... | 10.1109/TVCG.2013... | Visual Design, Taxono... | Byrne, Lydia; Angus, D... |
| | 2015 | AggreSet: Rich and Sc... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 688 | 697 | J | Datasets commonly i... | Yalcin, M. A.; Elmqvist... | Univ. of Maryland, Co... | Yalcin, M. A.; Elmqvist... | 10.1109/TVCG.2011... | Multi-valued attribut... | Adil Yalcin, M; Beders... |
| | 2015 | AmbiguityVis: Visuali... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 359 | 368 | J | Node-link diagrams p... | Yong Wang; Qiaomu S... | | Yong Wang; Qiaomu S... | 10.1109/TVCG.2006... | Visual Ambiguity, Vis... | Wang, Yong; Shen, Qia... |
| InfoVis | 2015 | Automatic Selection ... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 669 | 677 | J | Effective small multi... | Anand, A.; Talbot, J. | ; | Anand, A.; Talbot, J. | 10.1109/VAST.2010... | Small multiple displa... | Anand, Anushka; Talbo... |
| InfoVis | 2015 | Beyond Memorability... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 519 | 528 | J | In this paper we mov... | Borkin, M. A.; Bylinskii... | | Borkin, M.; Bylinskii, Z... | 10.1109/TVCG.2012... | Information visualiza... | null |
| InfoVis | 2015 | Beyond Weber's Law... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 469 | 478 | J | Models of human per... | Kay, M.; Heer, J. | ; | Kay, M.; Heer, J. | 10.1109/TVCG.2014... | Weber's law, percept... | Kay, Matthew; Heer, Je... |
| InfoVis | 2015 | Evaluation of Parallel... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 579 | 588 | J | The parallel coordina... | Johansson, J.; Forsell... | Norrkoping Visualiza... | Johansson, J.; Forsell... | 10.1109/TVCG.2014... | Survey, evaluation, g... | Johansson, Jimmy; For... |
| InfoVis | 2015 | Guidelines for Effecti... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 489 | 498 | J | Semi-automatic text ... | Strobelt, H.; Oelke, D... | | Strobelt, H.; Oelke, D... | 10.1109/TVCG.2012... | Text highlighting tec... | Strobelt, Hendrik; Oel... |
| InfoVis | 2015 | High-Quality Ultra-Co... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 339 | 348 | J | Prior research into ne... | Yoghourdjian, V.; Dwy... | | Yoghourdjian, V.; Dwy... | 10.1109/TVCG.2008... | Network visualizatio... | Yoghourdjian, Vahan; |
| InfoVis | 2015 | HOLA: Human-like Ort... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 349 | 358 | J | Over the last 50 year... | Kieffer, S.; Dwyer, T... | ... | Kieffer, S.; Dwyer, T... | 10.1109/TVCG.2006... | Graph layout, orthog... | Kieffer, Steve; Dwyer... |
| InfoVis | 2015 | How do People Make ... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 499 | 508 | J | In this paper, we wou... | Sukwon Lee; Sung-He... | Sch. of Ind. Eng., Purd... | Sukwon Lee; Sung-He... | 10.1109/TVCG.2013... | Sensemaking model, I... | Lee, Sukwon; Kim, Sun... |
| InfoVis | 2015 | Improving Bayesian R... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 529 | 538 | J | Decades of research ... | Ottley, A.; Peck, E. M... | | Ottley, A.; Peck, E. M... | 10.1109/TVCG.2014... | Bayesian Reasoning, ... | Ottley, Alvitia; Peck, E... |
| InfoVis | 2015 | Matches, Mismatche... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 449 | 458 | J | The energy performa... | Brehmer, M.; Ng, J.; Ta... | ... | Brehmer, M.; Ng, J.; Ta... | 10.1109/TVCG.2011... | Design study, design ... | Brehmer, Matthew; N... |

THE DATA CUBE



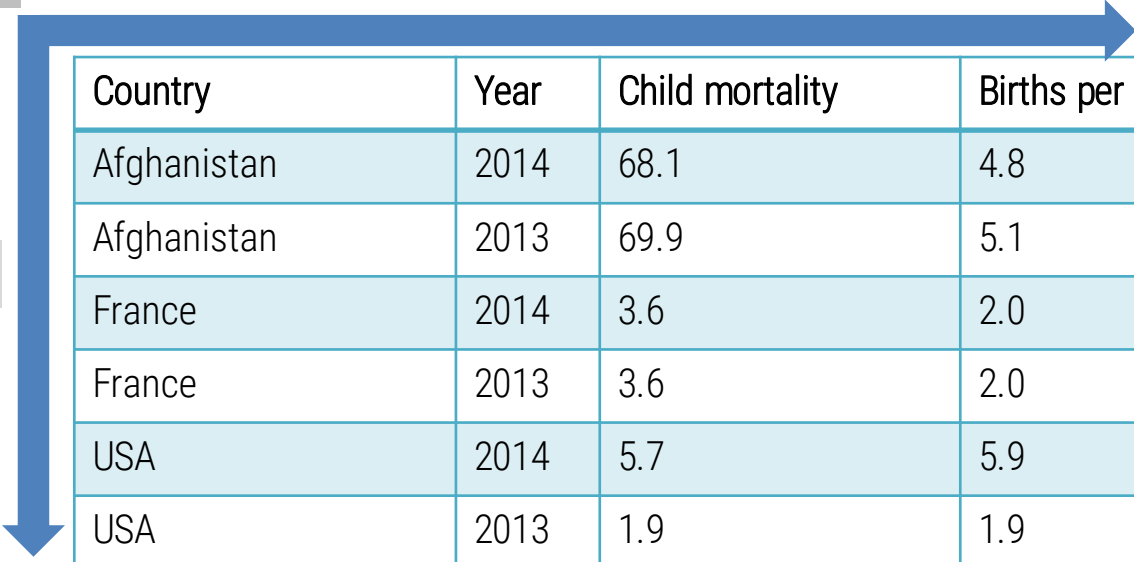
| Country | Year | Child mortality | Births per woman |
|-------------|------|-----------------|------------------|
| Afghanistan | 2014 | 68.1 | 4.8 |
| Afghanistan | 2013 | 69.9 | 5.1 |
| France | 2014 | 3.6 | 2.0 |
| France | 2013 | 3.6 | 2.0 |
| USA | 2014 | 5.7 | 5.9 |
| USA | 2013 | 1.9 | 1.9 |

MULTI-ATTRIBUTE DATA – OUR VIEW TODAY

n x d matrix

n attributes

d items (data points)



| Country | Year | Child mortality | Births per woman |
|-------------|------|-----------------|------------------|
| Afghanistan | 2014 | 68.1 | 4.8 |
| Afghanistan | 2013 | 69.9 | 5.1 |
| France | 2014 | 3.6 | 2.0 |
| France | 2013 | 3.6 | 2.0 |
| USA | 2014 | 5.7 | 5.9 |
| USA | 2013 | 1.9 | 1.9 |

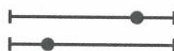
ARRANGING TABULAR DATA

In Space

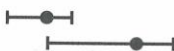
WHY ARRANGING DATA

➔ Magnitude Channels: Ordered Attributes

Position on common scale



Position on unaligned scale



Length (1D size)



Tilt/angle



Area (2D size)



Depth (3D position)



Color luminance



Color saturation



Curvature



Volume (3D size)



Same

Same

Most
Effectiveness
Least

➔ Identity Channels: Categorical Attributes

Spatial region



Color hue



Motion



Shape



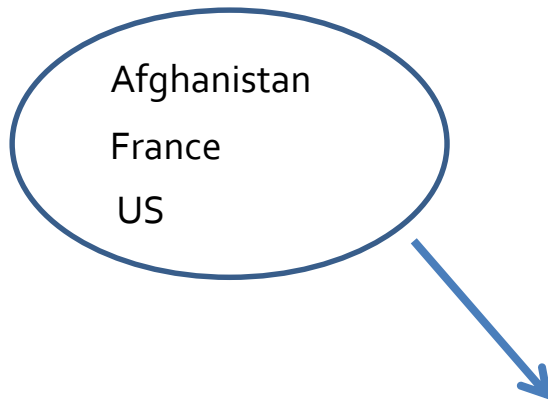
QUANTITATIVE VALUES

APPROACH

Let's start with two attributes:
country & income per person

| Country | Income per person |
|-------------|-------------------|
| Afghanistan | 850 |
| France | 29500 |
| US | 41000 |

1. FIND A LAYOUT

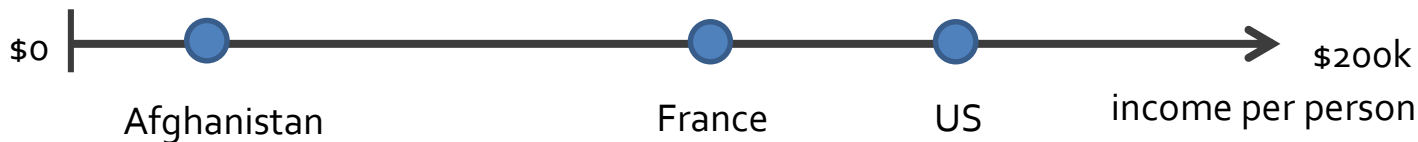


| Country | Income per person |
|-------------|-------------------|
| Afghanistan | 850 |
| France | 29500 |
| US | 41000 |



2. CHOOSE A VISUAL ENCODING & MARK

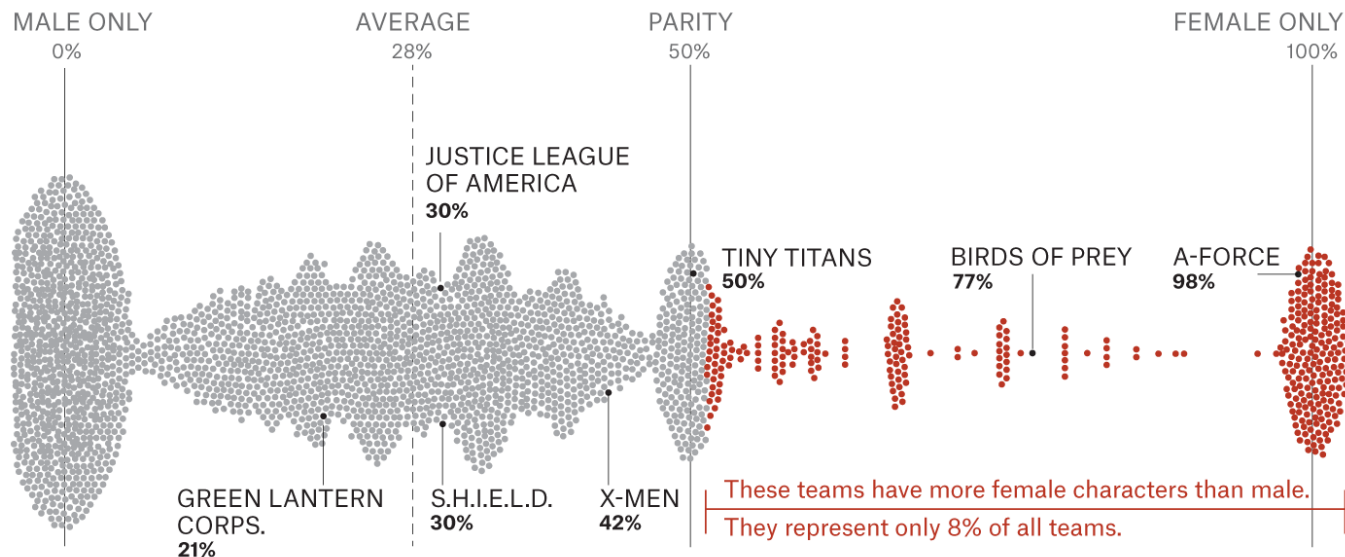
E.g. position + circle





Analyzing the Gender Representation of 34,476 Comic Book Characters

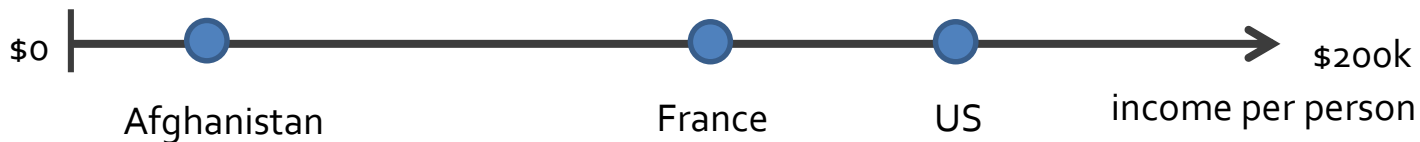
Female percentage of
every team
Each dot represents
one of 2,862 teams in
DC and Marvel.



1. FIND A LAYOUT

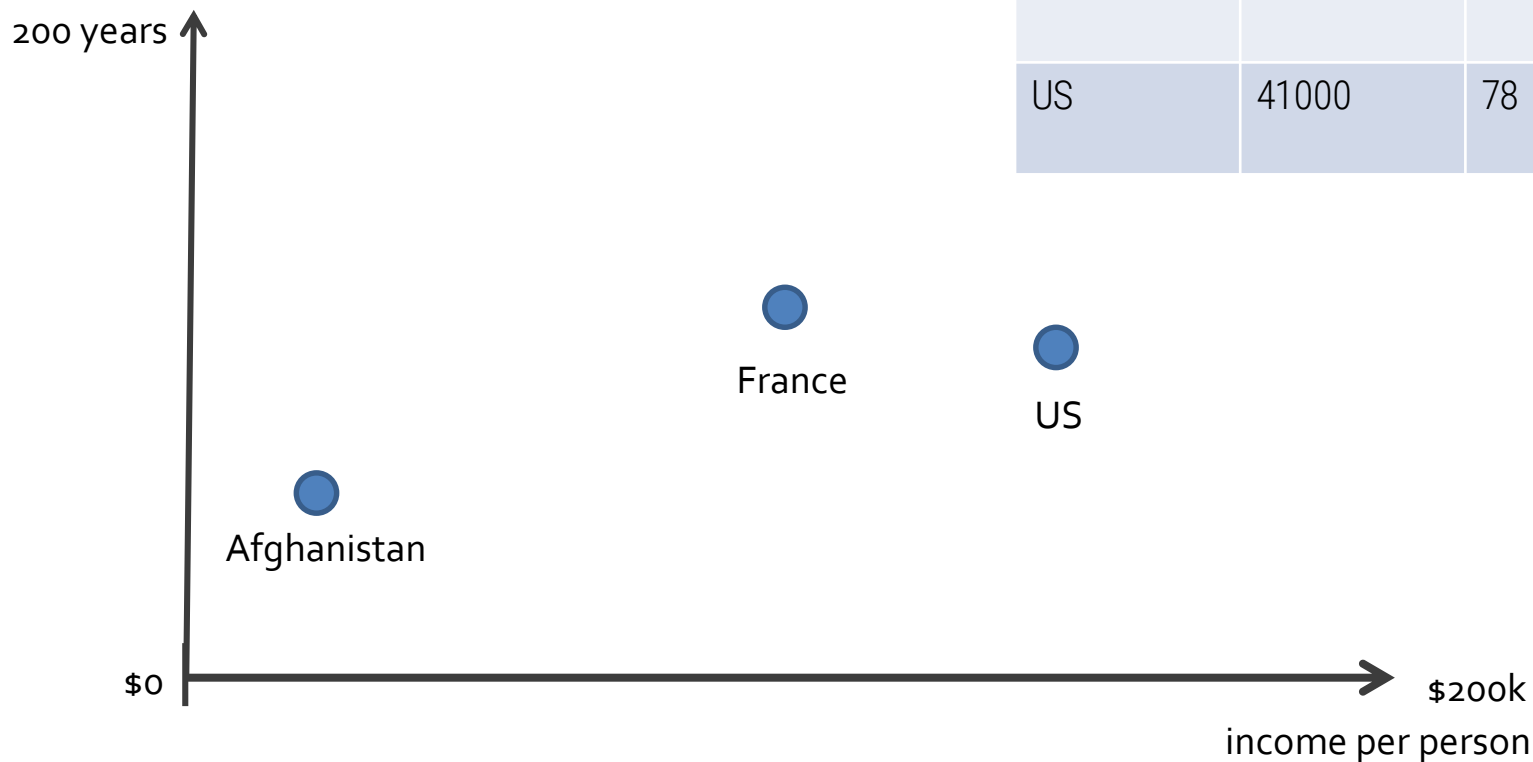
| Country | Income per person | Life expectancy |
|-------------|-------------------|-----------------|
| Afghanistan | 850 | 57 |
| France | 29500 | 81 |
| US | 41000 | 78 |

How do we extend this to 3 data attributes?



1. FIND A LAYOUT

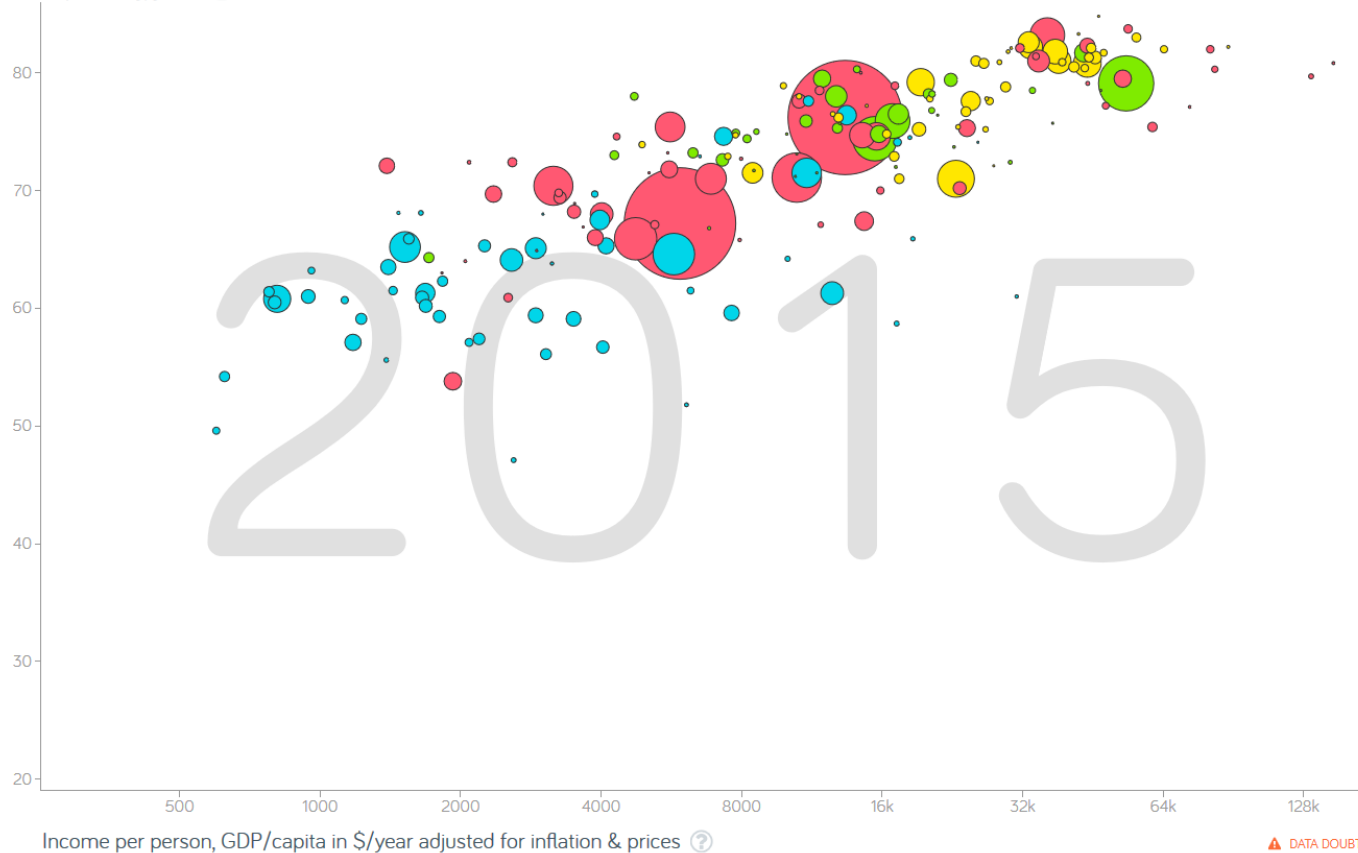
| Country | Income per person | Life expectancy |
|-------------|-------------------|-----------------|
| Afghanistan | 850 | 57 |
| France | 29500 | 81 |
| US | 41000 | 78 |



SCATTERPLOTS

- two quantitative values
- horizontal and vertical spatial dimensions
- mark type = point

Life expectancy, years ?



Color World Regions ?



Select Search...

- ☐ Afghanistan
- ☐ Albania
- ☐ Algeria
- ☐ Andorra
- ☐ Angola
- ☐ Antigua and Barbuda
- ☐ Argentina
- ☐ Armenia
- ☐ Aruba
- ☐ Australia
- ☐ Austria
- ☐ Azerbaijan
- ☐ Bahamas
- ☐ Bahrain
- ☐ Bangladesh
- ☐ Barbados
- ☐ Belarus
- ☐ Belgium
- ☐ Belize
- ☐ Benin

Size Population ?

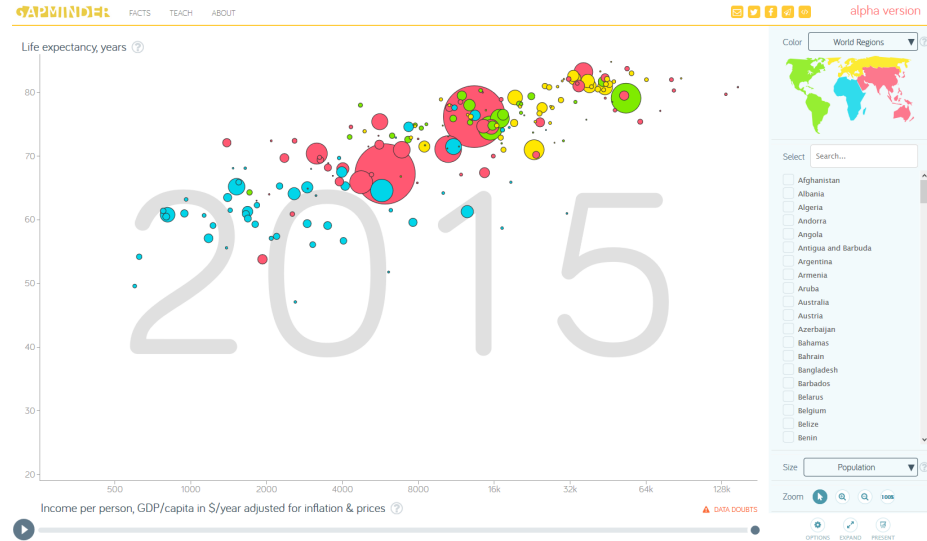
Zoom   100% OPTIONS  EXPAND  PRESENT

when marks are sized, the chart is often called a bubble chart or bubble plot



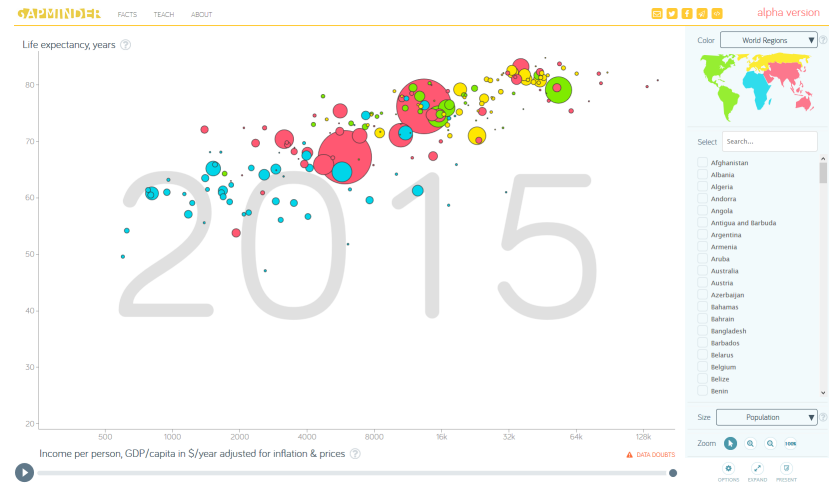
Why choose a scatterplot?

What can you show with them?

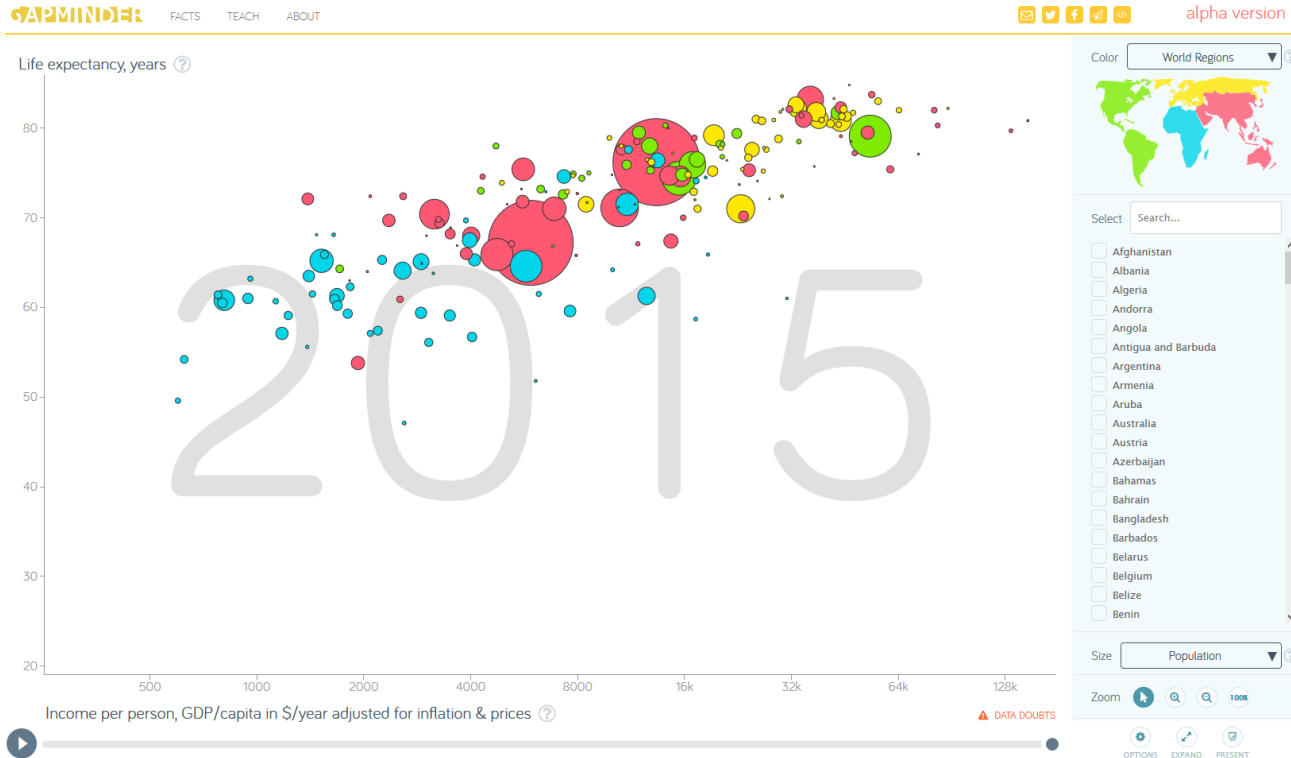


TASKS

- find trends
- find outliers
- show distribution
- show correlation
- locate clusters



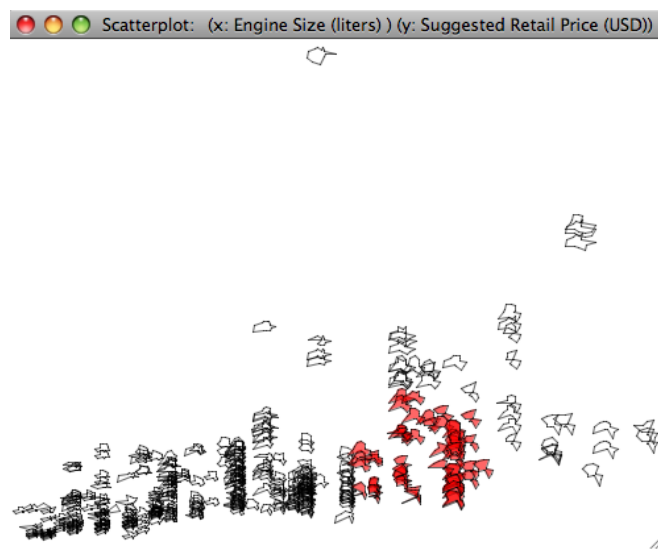
how many items are reasonable to put on a scatterplot?



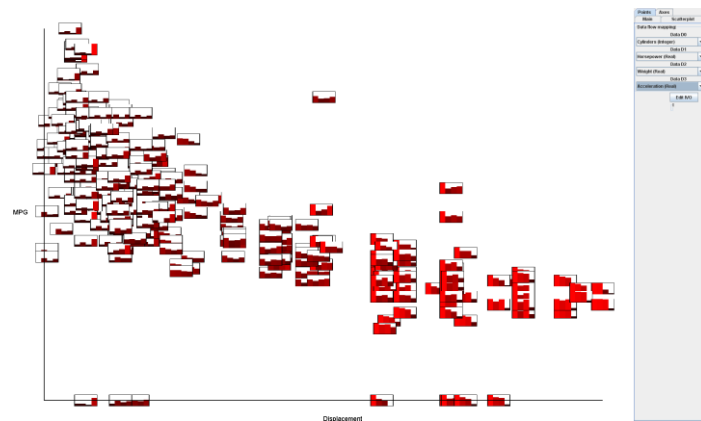
GLYPHS

marks can be replaced with glyphs

glyphs are themselves composed of multiple marks



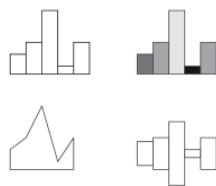
<http://rosuda.org/software/Gauguin/gauguin.html>



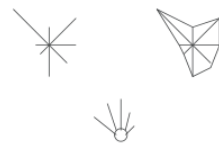
<https://engineering.purdue.edu/~elm/projects/gpuvis.html>

GLYPHS

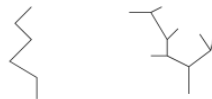
- Small composite visual representations of multi-dimensional data points
- Characterized generally by lack of reference structures (grid lines, axes labels, ...)



Variations on Profile glyphs



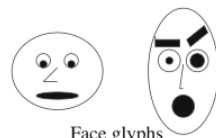
Stars and Anderson/metroglyphs



Sticks and Trees



Autoglyph and box glyph



Face glyphs



Arrows and Weathervanes

From Ward, 2002

A taxonomy of glyph placement strategies for multidimensional data visualization

EXAMPLE: CHERNOFF FACES

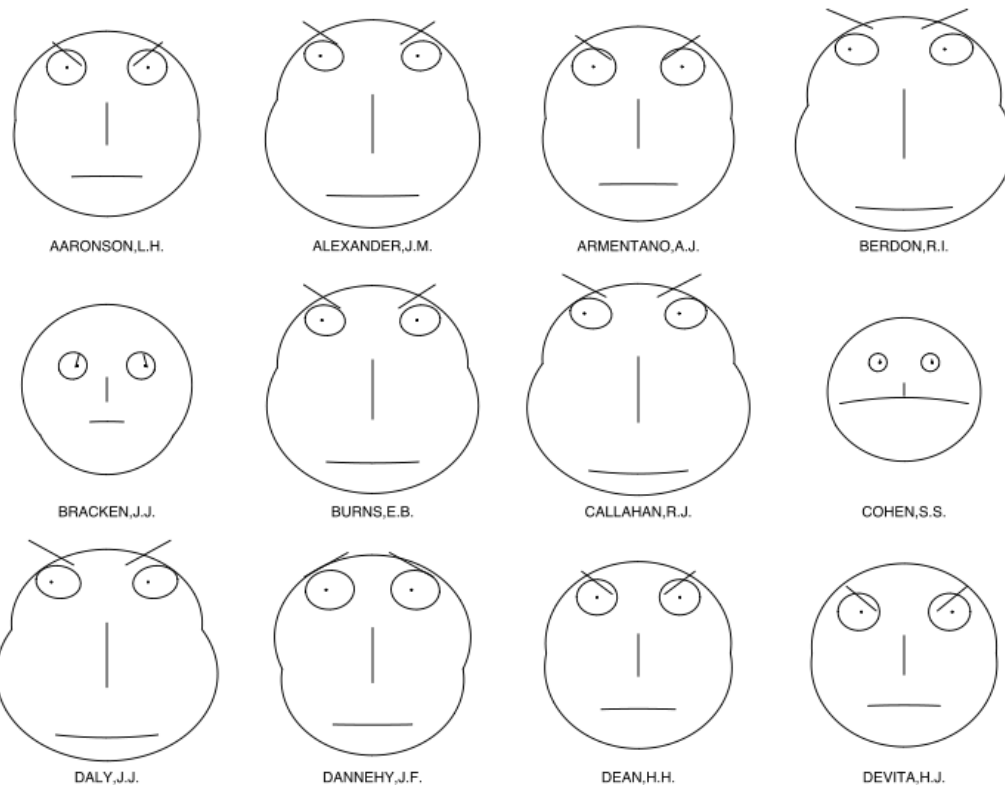
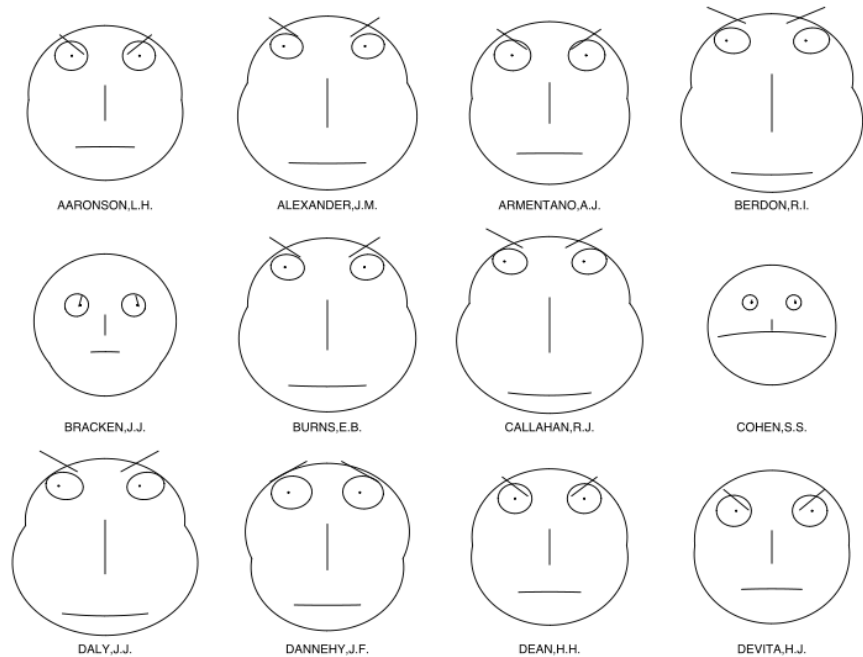


Image source: Wikipedia

Herman Chernoff, [The Use of Faces to Represent Points in K-Dimensional Space Graphically](#), 1973.

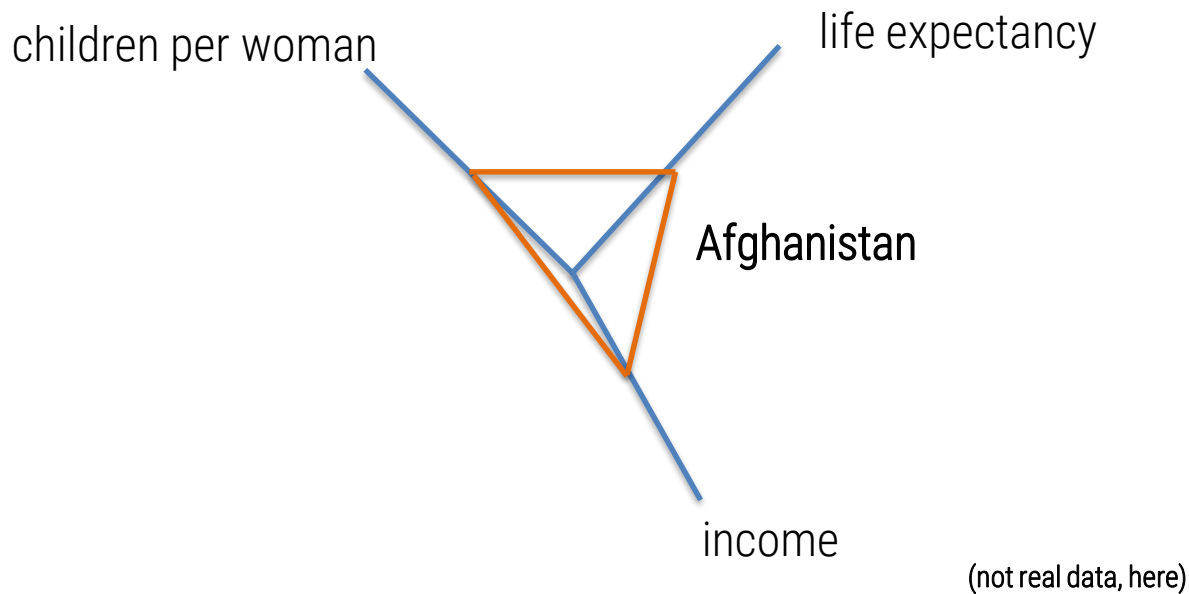
CHERNOFF FACES

- features of a human face encode data values (e.g. slant of eye brows, size of eyes, ...)
- reasoning: humans are good at differentiating faces and reading face features
- problem: chernoff faces have generally been found not to be very effective

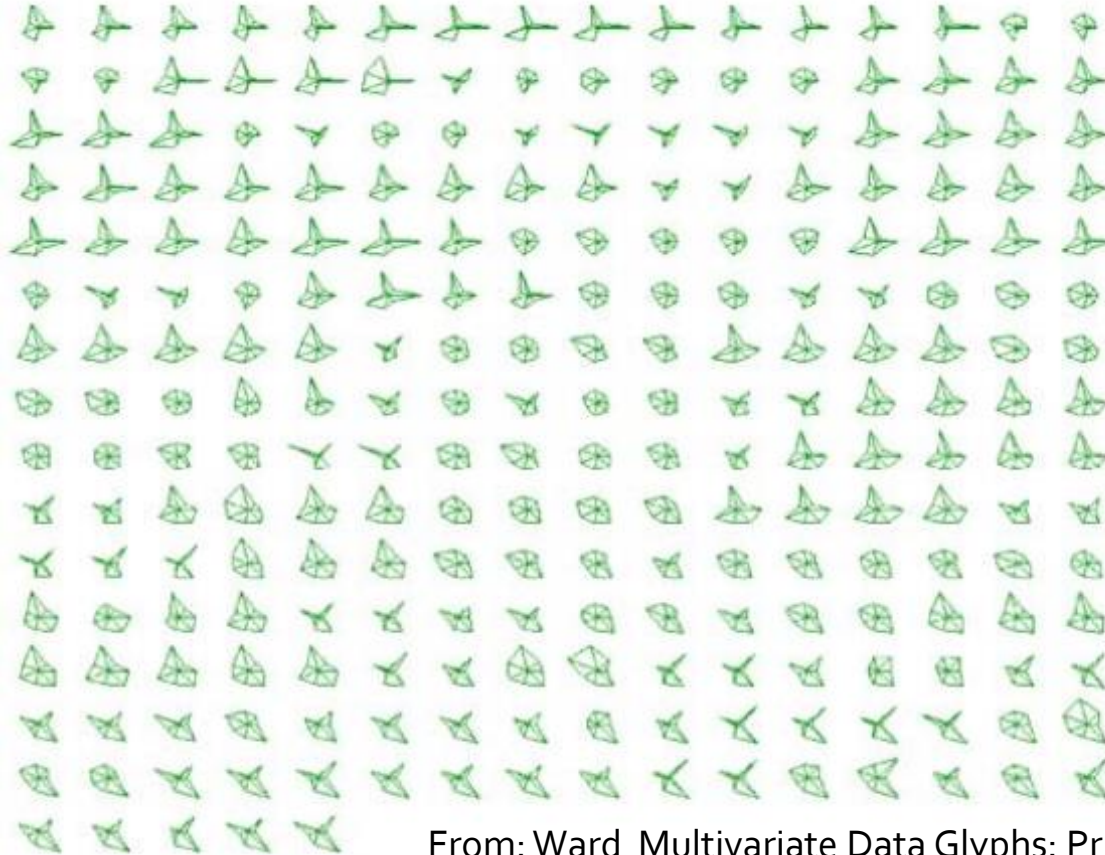


EXAMPLE: STAR GLYPHS

- Lay out dimension in radial fashion
- Draw each point as a ring



STAR GLYPHS



From: Ward Multivariate Data Glyphs: Principles and Practice. Handbook of Data Visualization (2008)

It's gettin hot out here

2015: WARMEST DECEMBER

<http://www.studioterp.nl/its-gettin-h>

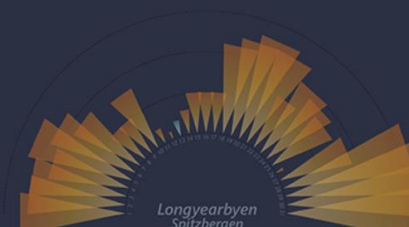
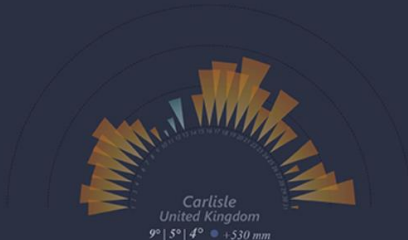
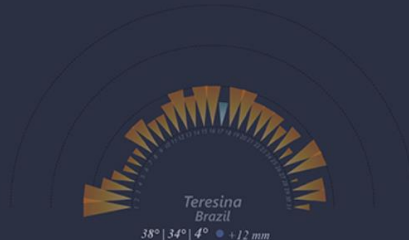
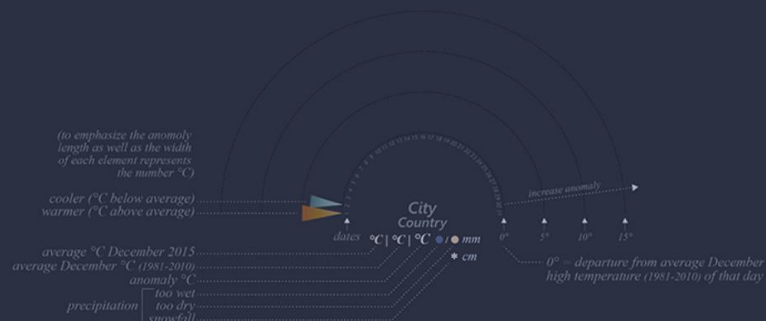
HOW TO READ IT

This visualization shows 8 places around the globe chosen for their location in areas where anomalies occurred. Shown are the number of °C departing from the average temperature of each December day.

Across the globe, record warm temperatures were observed over every continent, including a large swath of eastern North America, southern Mexico through northern South America, western and central Europe, most of southern Africa, parts of central and southeastern Asia, and a large section of southeastern Australia.

The link between the tumultuous weather events experienced around the world in December is likely to be down to the natural phenomenon known as El Niño making the effects of man-made climate change worse. The 2015 El Niño is one of the strongest on record, leading to record temperatures, rainfall and weather extremes.

During December, the globally-averaged land surface temperature was almost 2°C above the 20th century average. This was the highest for December in the 1880–2015 record, surpassing the previous record of 2006 by 0.5°C. The December temperature departure from average was also the highest departure among all months in the historical record and the first time a monthly departure has reached little over +1°C from the 20th century average.



SHOW CATEGORICAL DATA

Using Regions: Separate, Order, and Align

CATEGORICAL VALUES

- spatial position is an ordered magnitude visual channel
- categorical attributes are unordered identities (no magnitude)
 - cannot be encoded with spatial position
- BUT: can be differentiated with a spatial region

REGIONS

- contiguous bounded areas
- distinct from one another
- need to be separated, ordered, and aligned



LIST ALIGNMENT

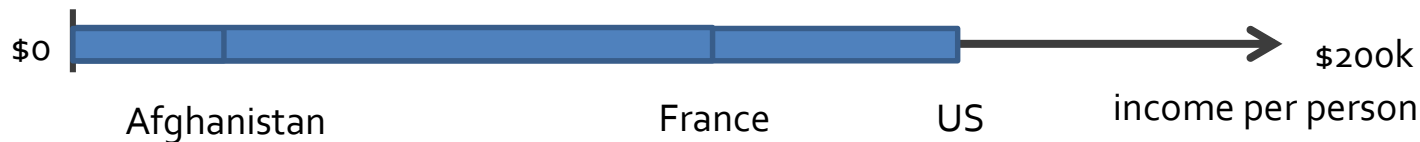
ONE KEY

LIST ALIGNMENT

separate into regions by key

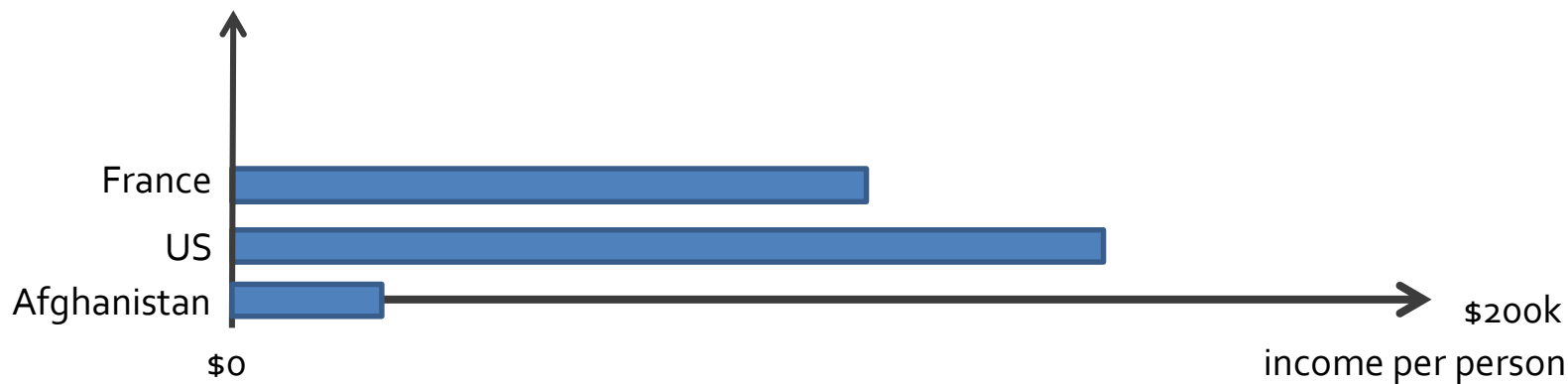
E.g. length + rectangle

Ok, this is weird



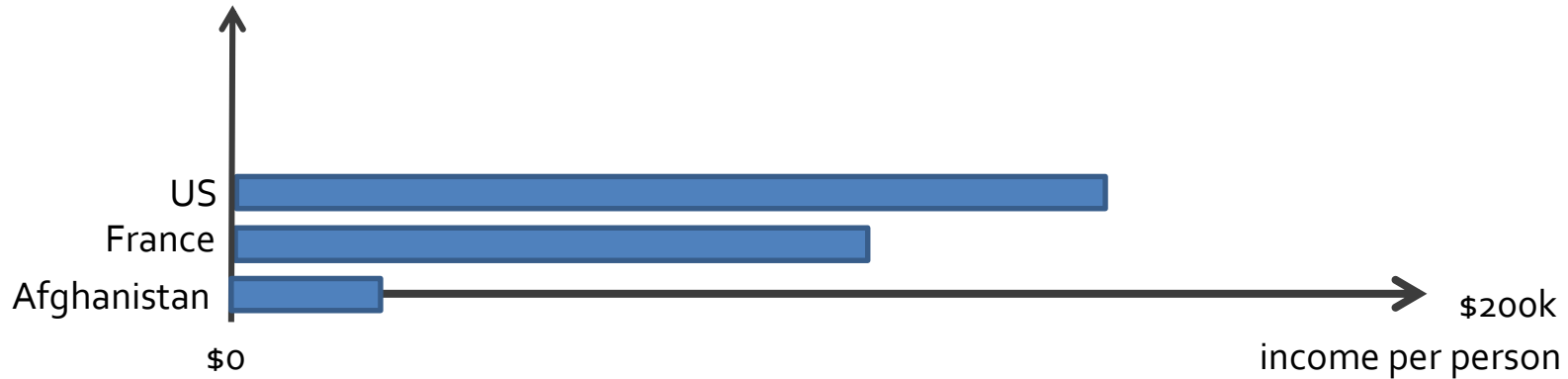
ALIGN

align regions of key categorical values along one axis in a common frame



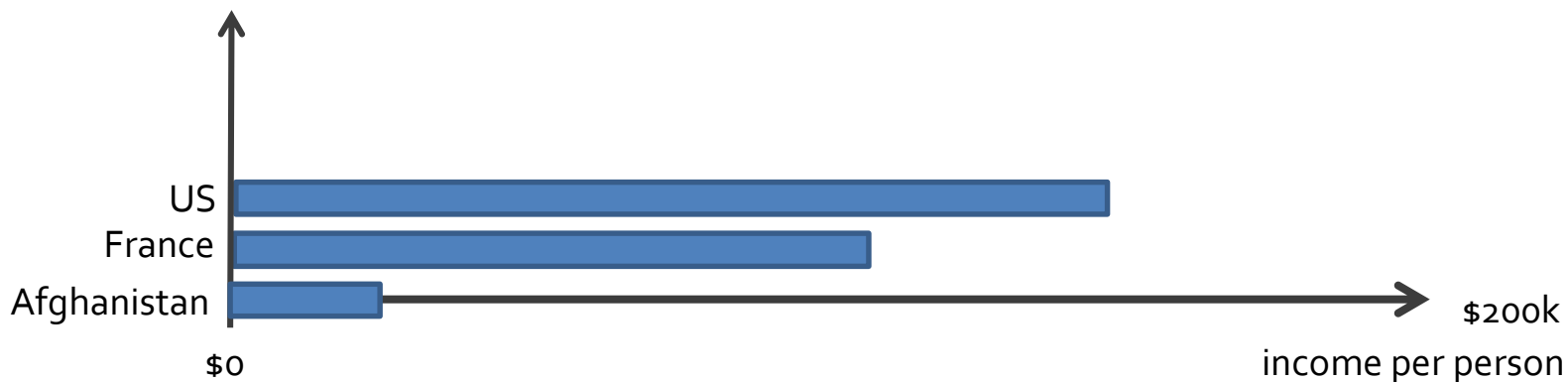
ORDER

- using a derived attribute such as alphabet
- and/or using dependent data values



BAR CHARTS

| | |
|--------|--|
| DATA | one quantitative value attribute, one categorical key attribute |
| ENCODE | line marks, express value attribute with aligned vertical position (length), separate key attribute with horizontal position |
| TASK | lookup and compare values |
| SCALE | key attribute: dozens to hundreds of levels |



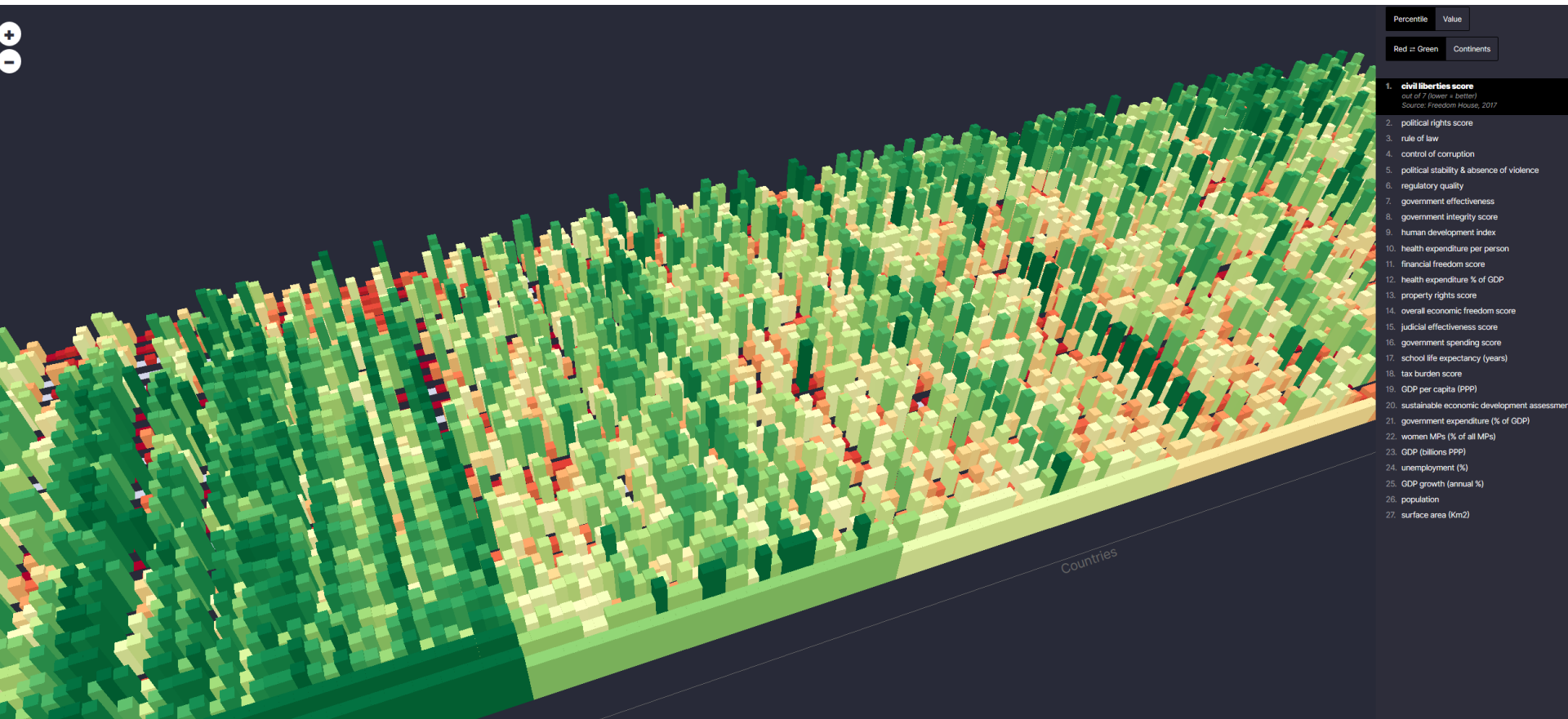
US Inmates held in Private vs. Public Prisons, by Jurisdiction



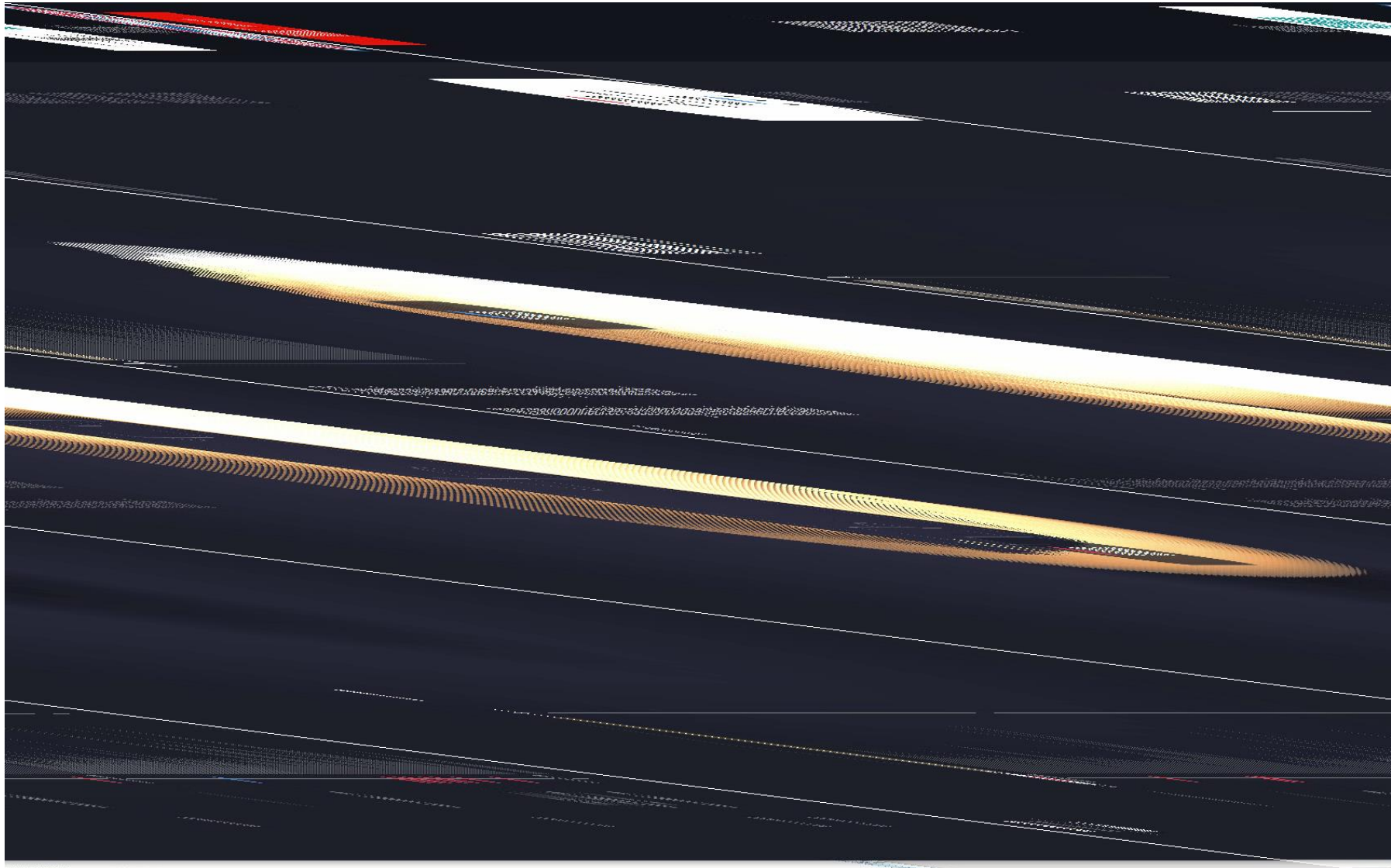
<https://pudding.cool/2017/03/incarceration/index.html>

[Source](#) | [Download Data](#)

Be careful with 3D bar charts. Only use them when you know what you are doing.

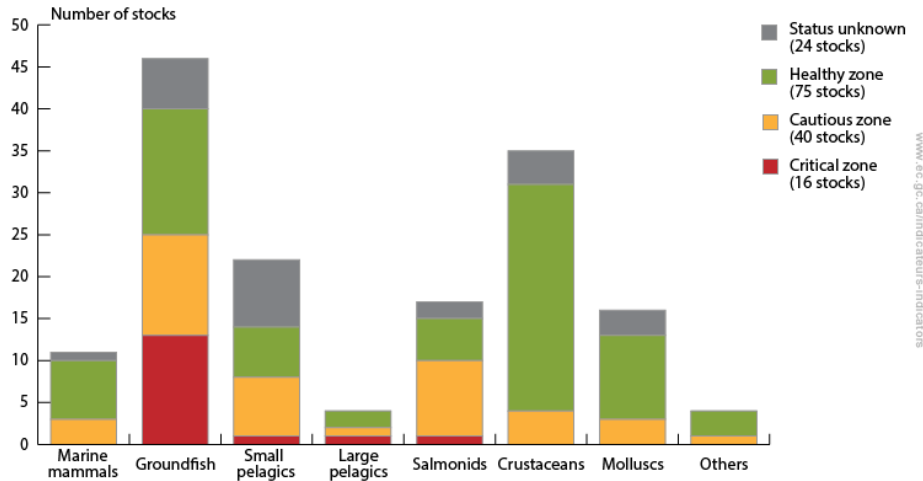


<https://wattenberger.com/wdvp>



<https://reimaginethegame.economist.com>

ALTERNATIVE

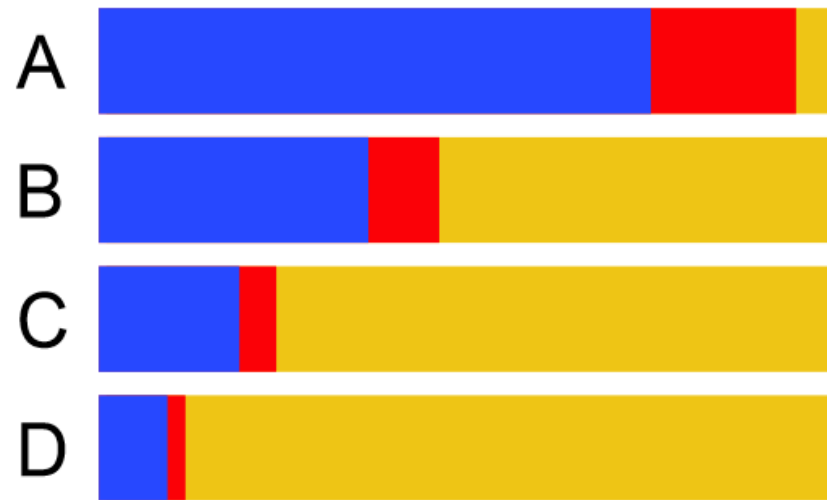
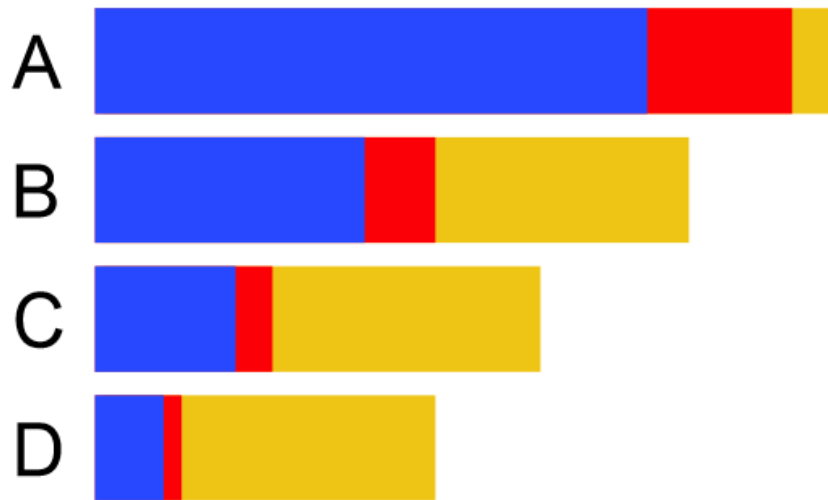


<https://www.ec.gc.ca/indicateurs-indicators/default.asp?lang=en&n=1BCD421B-1>

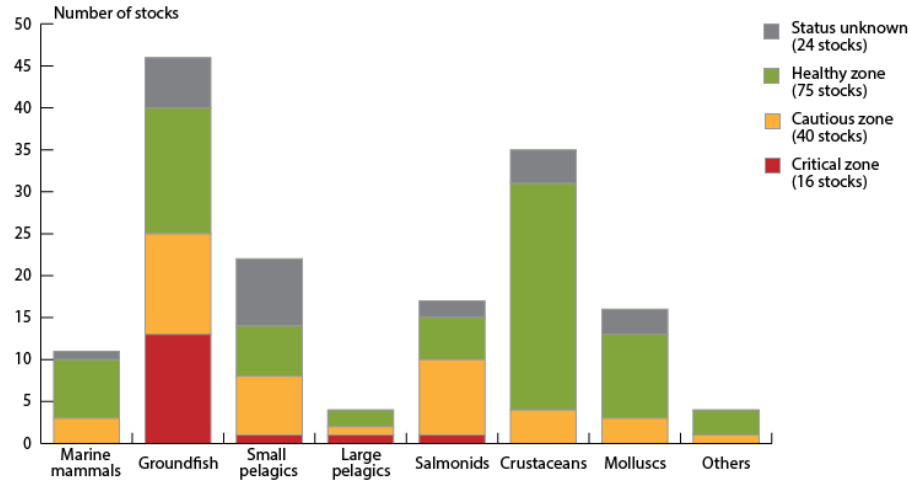
Stacked bar chart

- each bar is a composite glyph
- each bar part encodes a value
- composite glyphs arranged as a list according to primary key
- color used to distinguish secondary key
- typically used for absolute values (use a normalized stacked bar for proportions)

STACKED BARS VS. NORMALIZED STACKED BARS



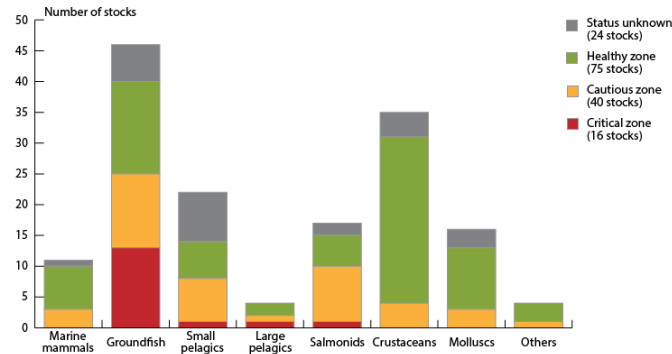
STACKED BARS



- ADVANTAGE
 - can compare totals and lowest level well
- DISADVANTAGE
 - upper levels of secondary key require comparison against non-aligned scale

STACKED BARS

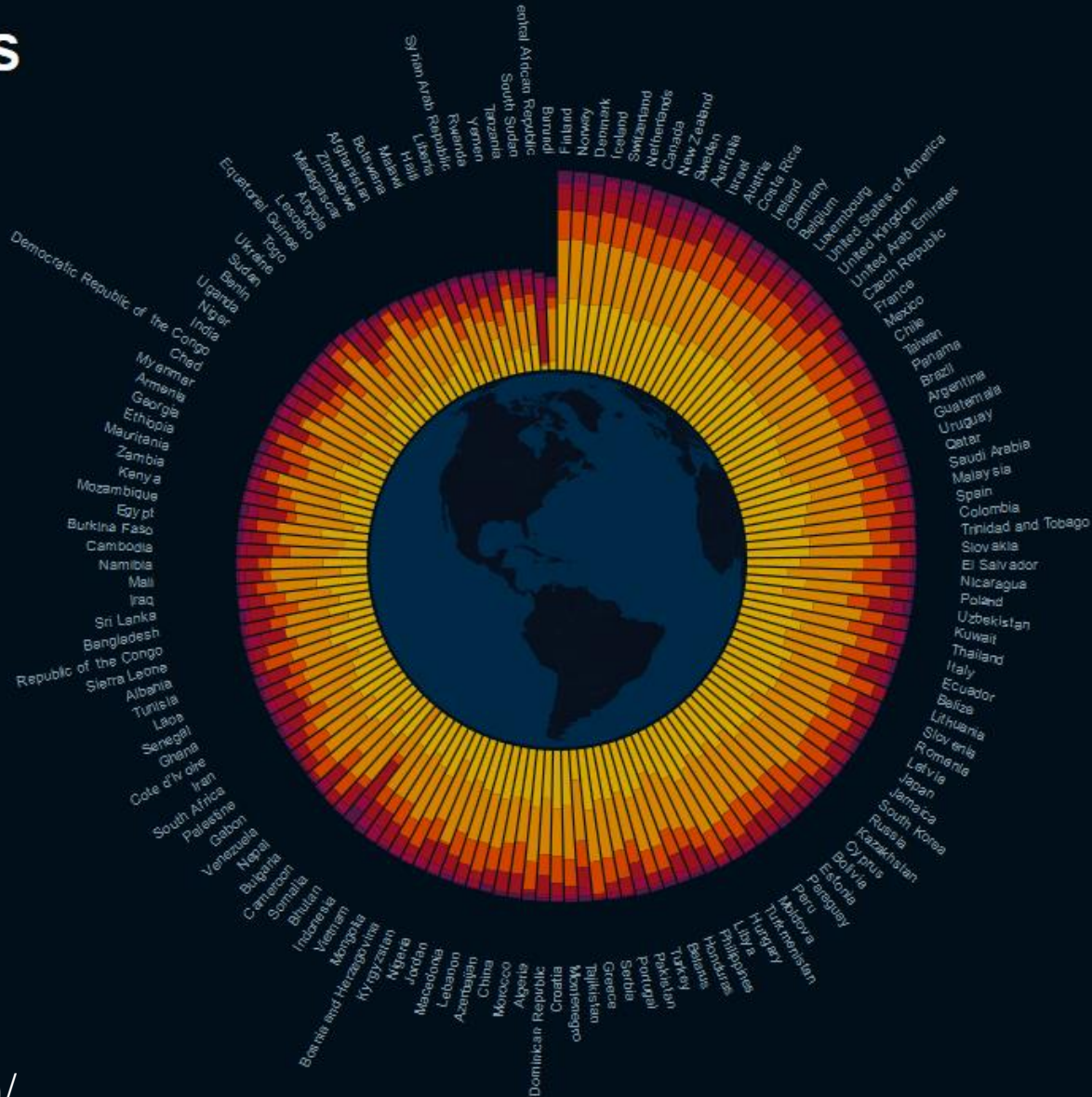
| | |
|--------|---|
| DATA | MD table; one quantitative value attribute, two categorical key attributes |
| ENCODE | bar glyph: length-encoded subcomponents for each level of secondary key attribute separate bars by category of primary key |
| TASK | part-to-whole relationship, lookup values, find trends |
| SCALE | key attribute (main axis): dozens to hundreds of levels key attribute (stacked glyph axis): several to one dozen |



A WORLD OF HAPPINESS

According to the UN World Happiness Report, these factors combined contribute to national happiness.

Explore the globe and see how your country measures up.



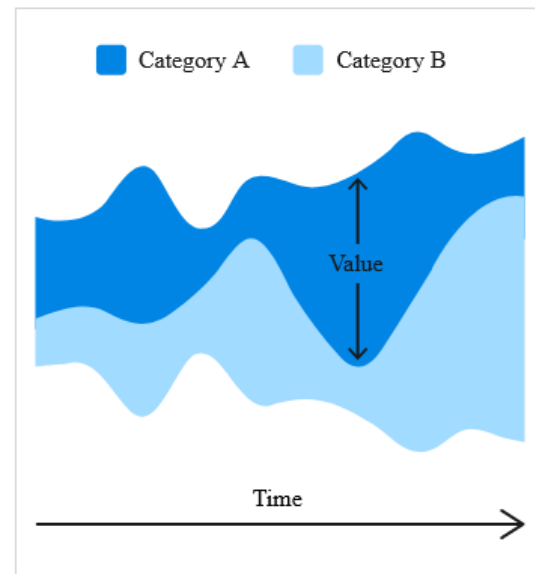
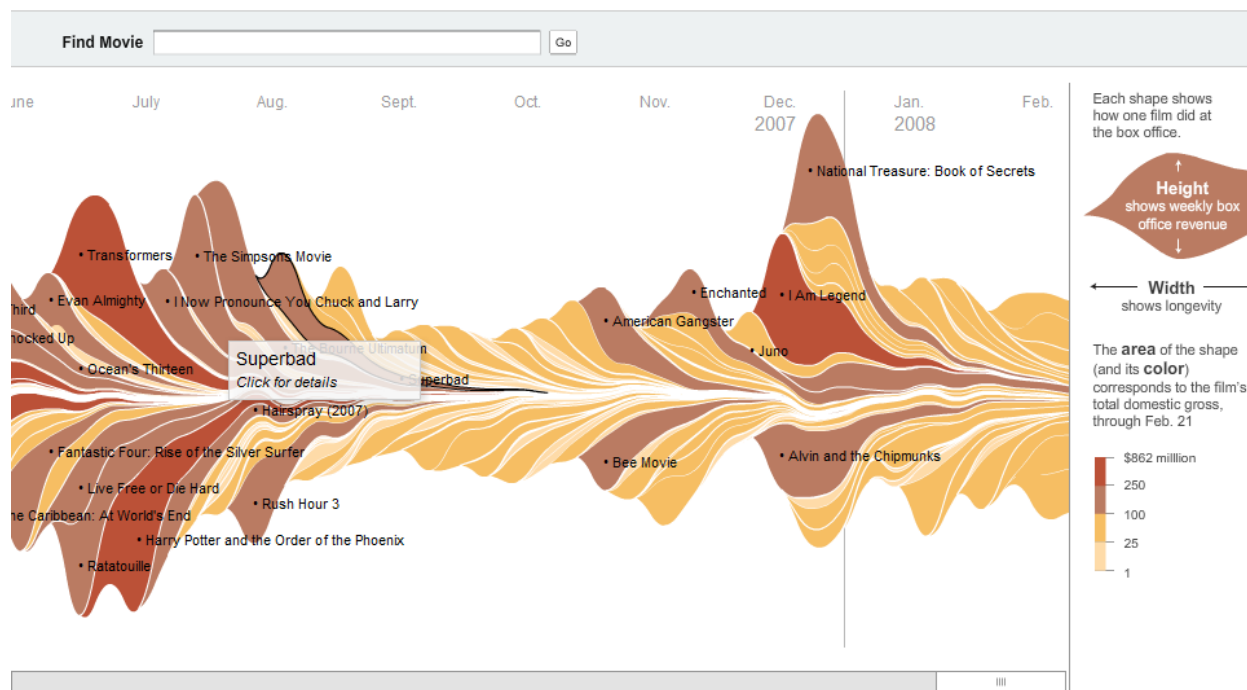
STREAMGRAPH

February 23, 2008

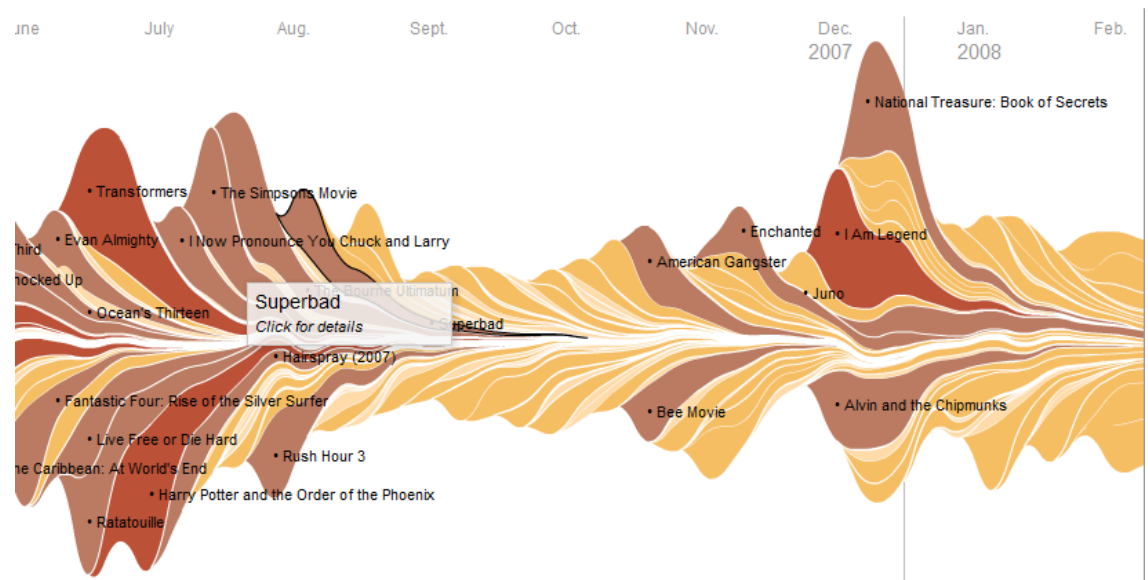
[SIGN IN TO E-MAIL OR SAVE THIS](#) | [FEEDBACK](#)

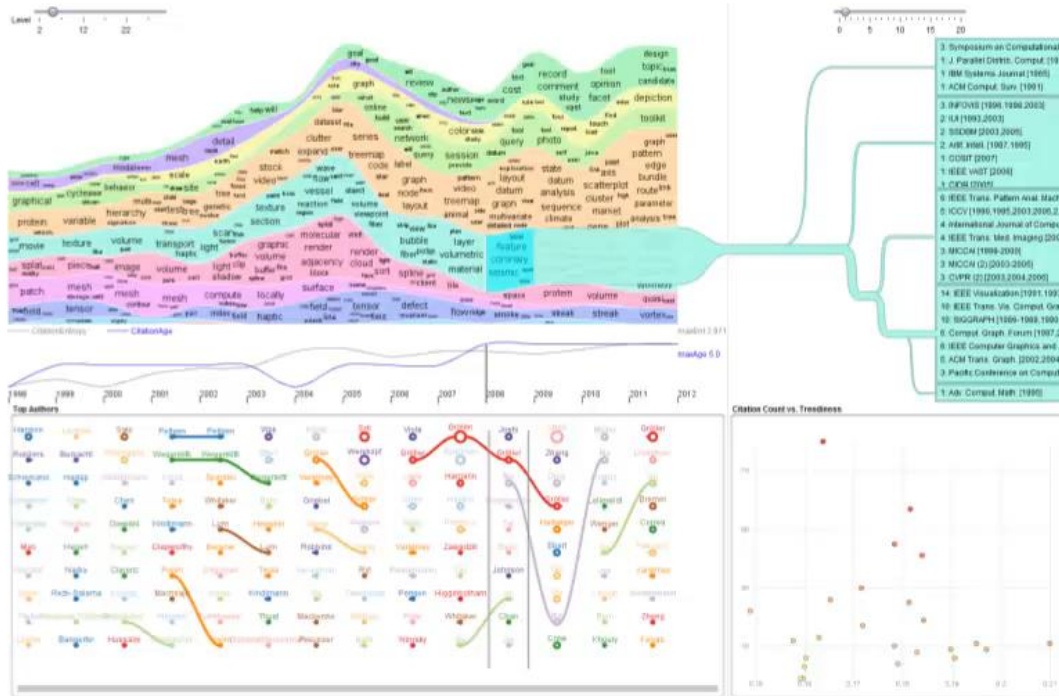
The Ebb and Flow of Movies: Box Office Receipts 1986 — 2008

Summer blockbusters and holiday hits make up the bulk of box office revenue each year, while contenders for the Oscars tend to attract smaller audiences that build over time. Here's a look at how movies have fared at the box office, after adjusting for inflation.



| | |
|--------|--|
| DATA | MD table; one quantitative value attribute (e.g. counts), one ordered key attribute (e.g. time), one categorical key attribute (e.g. film) |
| DERIVE | order of layers is derived from a quantitative attribute |
| ENCODE | use derived geometry to show layers across time, layer height encodes count |
| SCALE | key attributes (time, main axis): hundreds of time points key attributes (short axis): dozens to hundreds |





CiteRivers

Florian Heimerl, Qi Han,
Steffen Koch, Thomas Ertl

University of Stuttgart

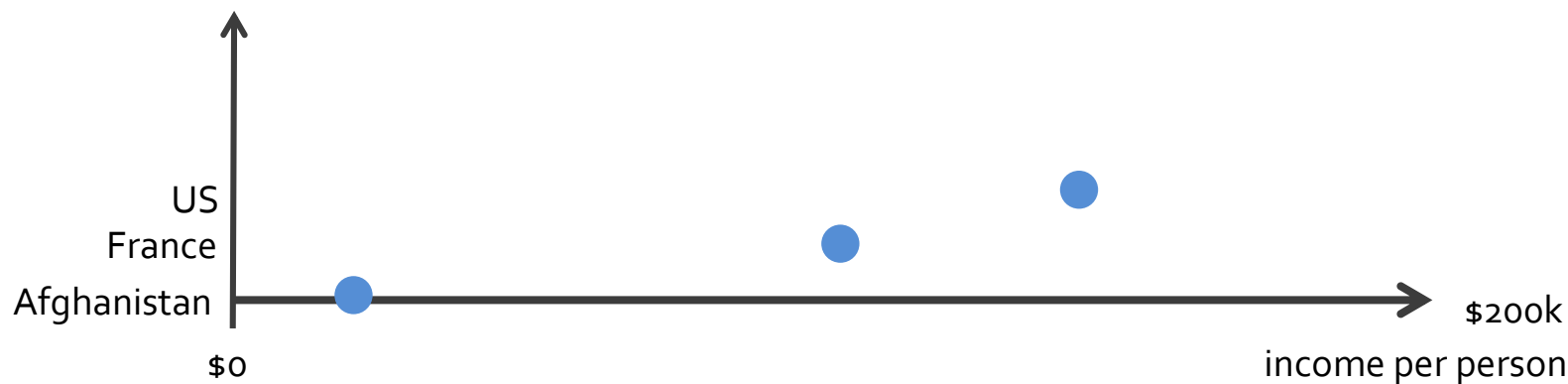
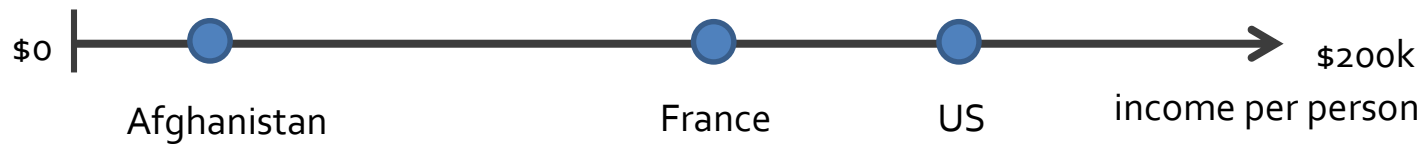
florian.heimerl@vis.uni-stuttgart.de

IEEE VAST 2015

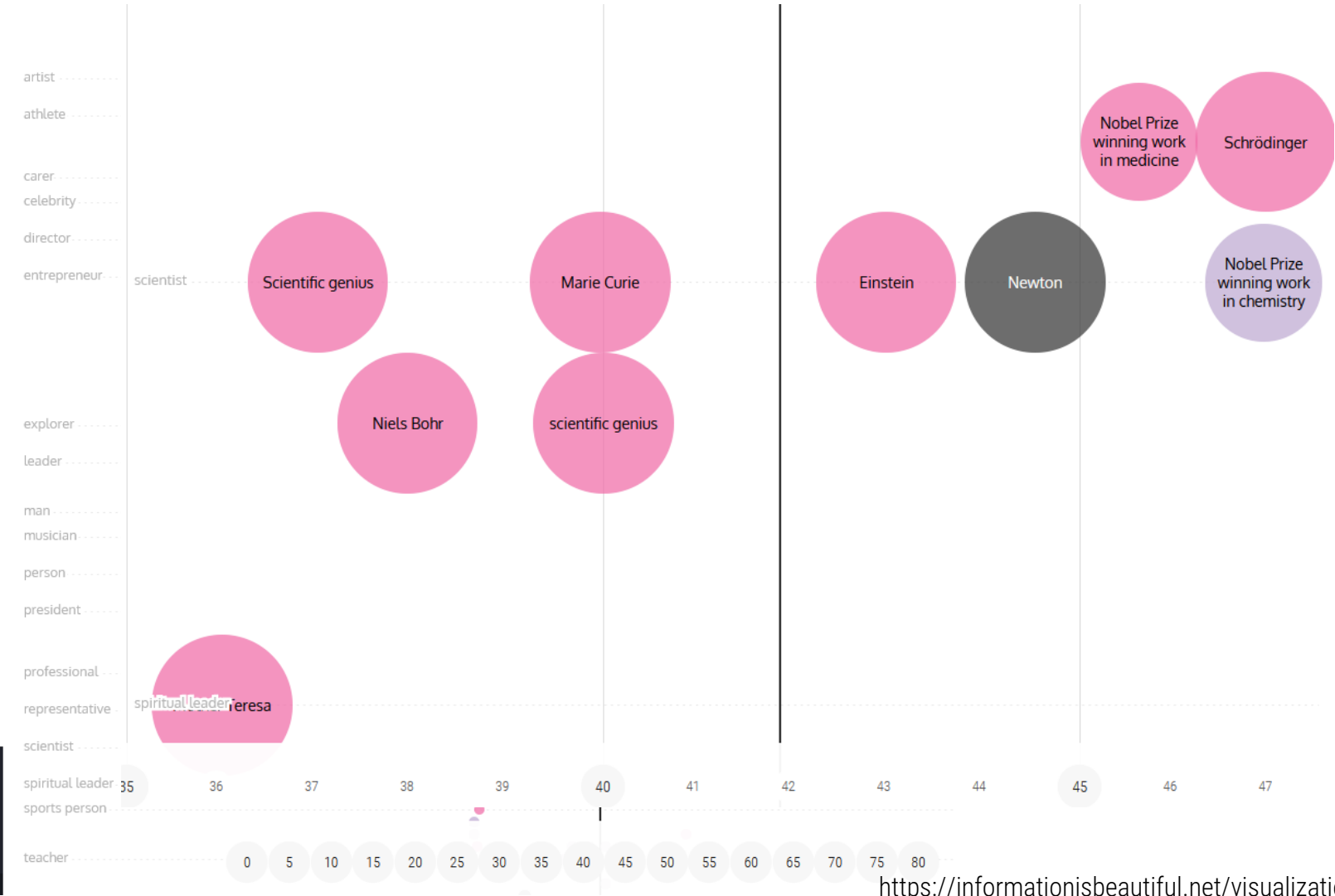


Institute for Visualization
and Interactive Systems

DOT CHART/PLOT

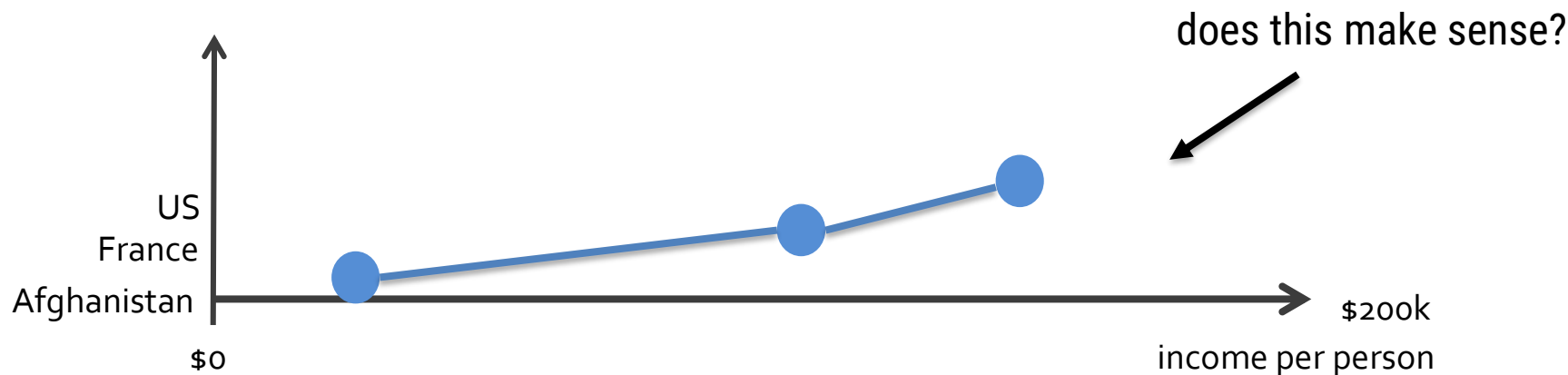


Who Old Are You?



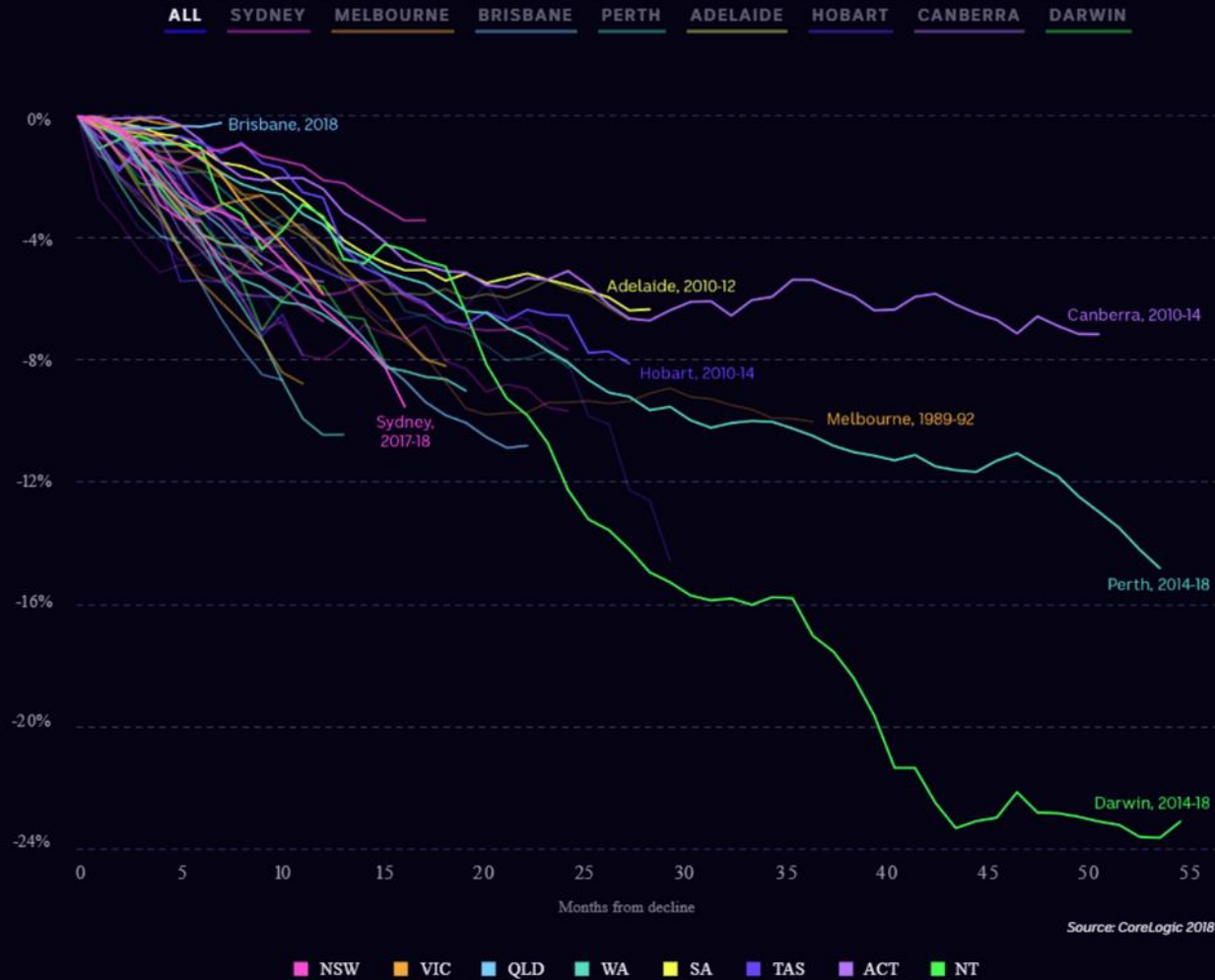
LINE CHART

augment with line connection marks
emphasize the ordering and show trends
should not be used with categorical keys



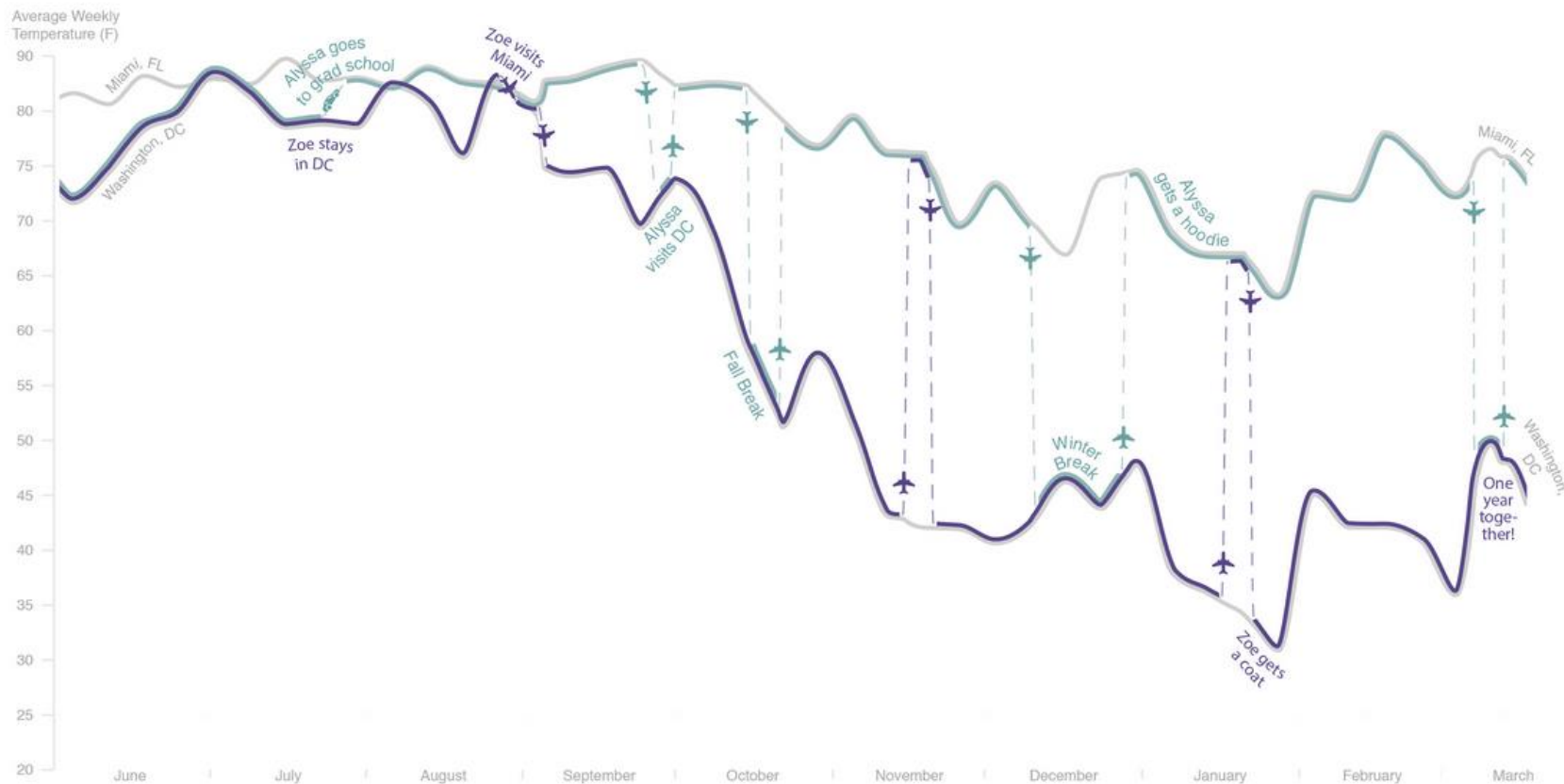
Housing market declines since 1980

Each line represents a downturn.
(Longer line = longer downturn; steeper line = steeper downturn)



Running Hot and Cold

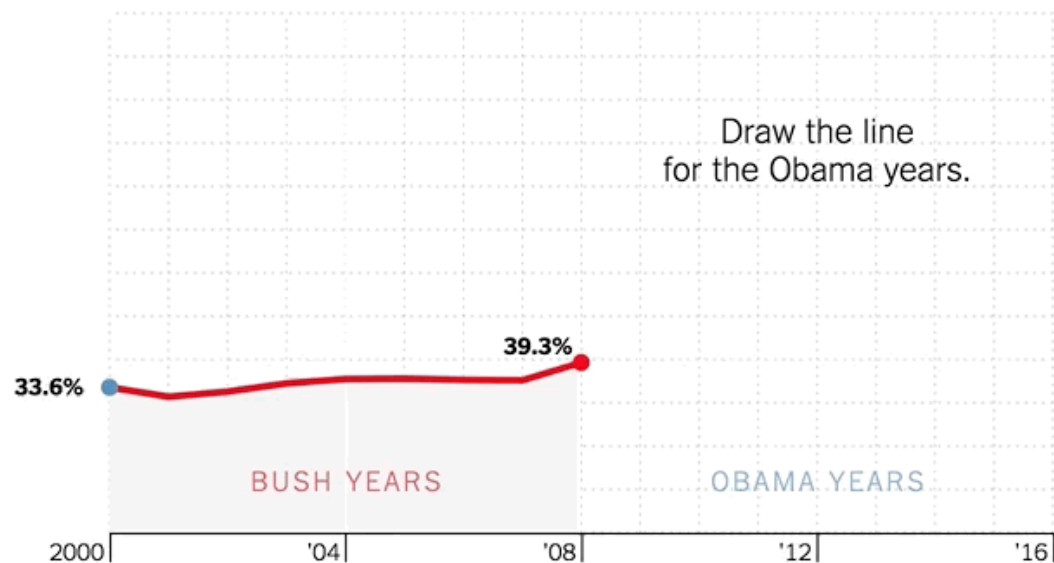
Temperature differentials in Alyssa and Zoe's long-distance relationship



Temperature data from NOAA
Graphics by Alyssa Fowers

<https://www.alyssafowers.com/portfolio/#/running-hot-and-cold/>

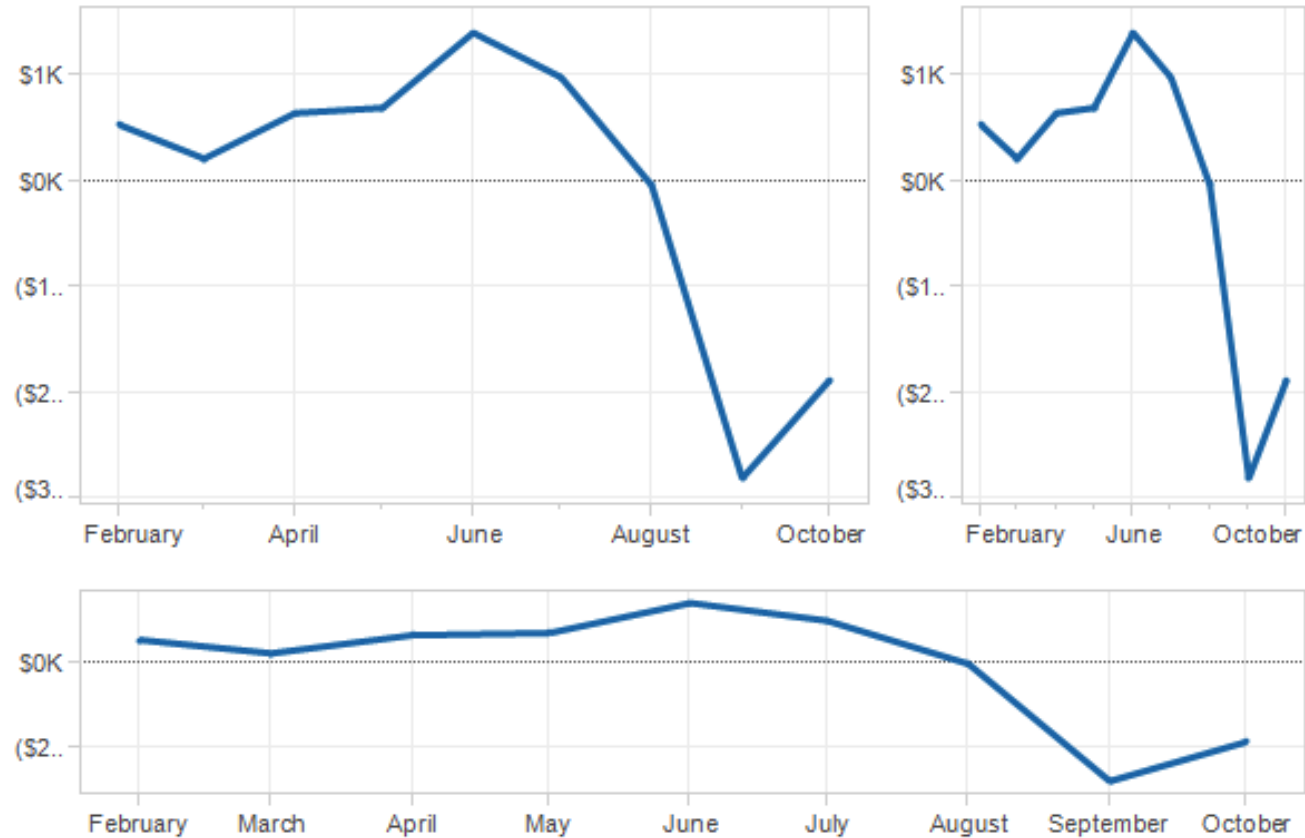
Under Mr. Obama, the **national debt** as a percentage of the gross domestic product ...



Show me how I did.

Numbers

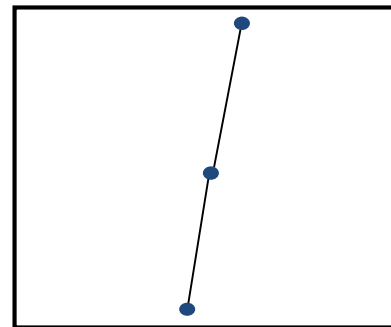
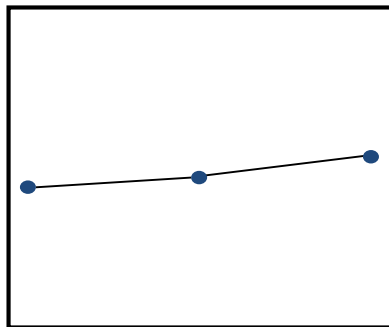
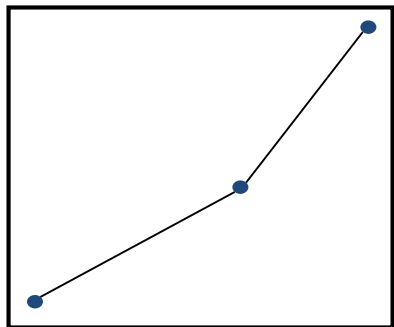
ASPECT RATIO SELECTION



BANKING TO 45°

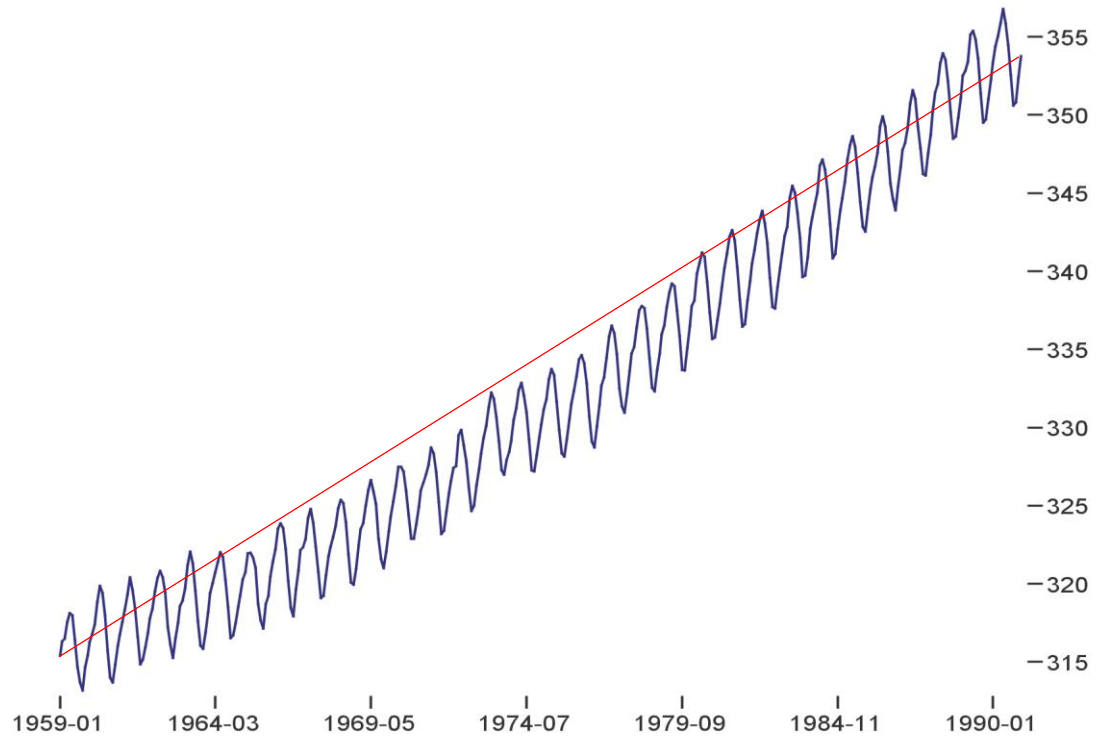
[Cleveland]

TO FACILITATE PERCEPTION OF TRENDS,
MAXIMIZE THE DISCRIMINABILITY OF LINE
SEGMENT ORIENTATIONS

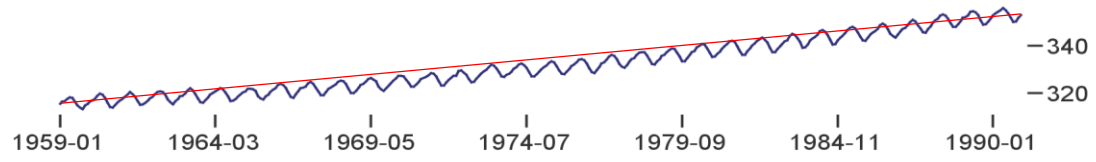


TWO SEGMENTS ARE MAXIMALLY DISCRIMINABLE WHEN THEIR AVG ABSOLUTE ANGLE IS
45°

OPTIMIZE THE *ASPECT RATIO* TO BANK TO 45°

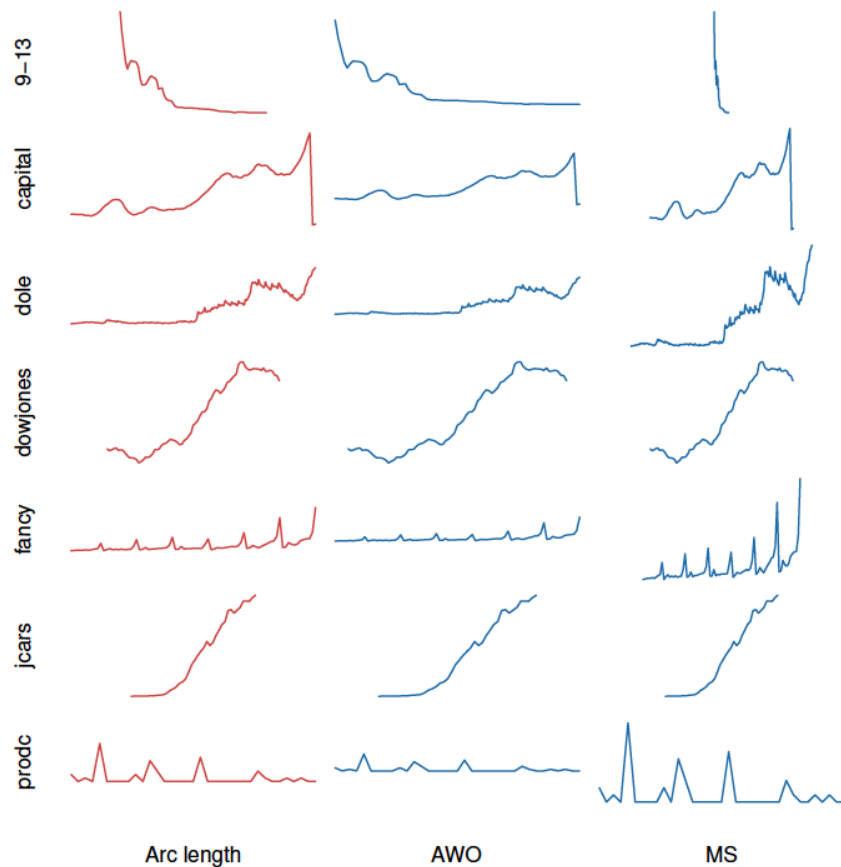


ASPECT RATIO = 1.17



ASPECT RATIO = 7.87

ALTERNATIVE METHODS



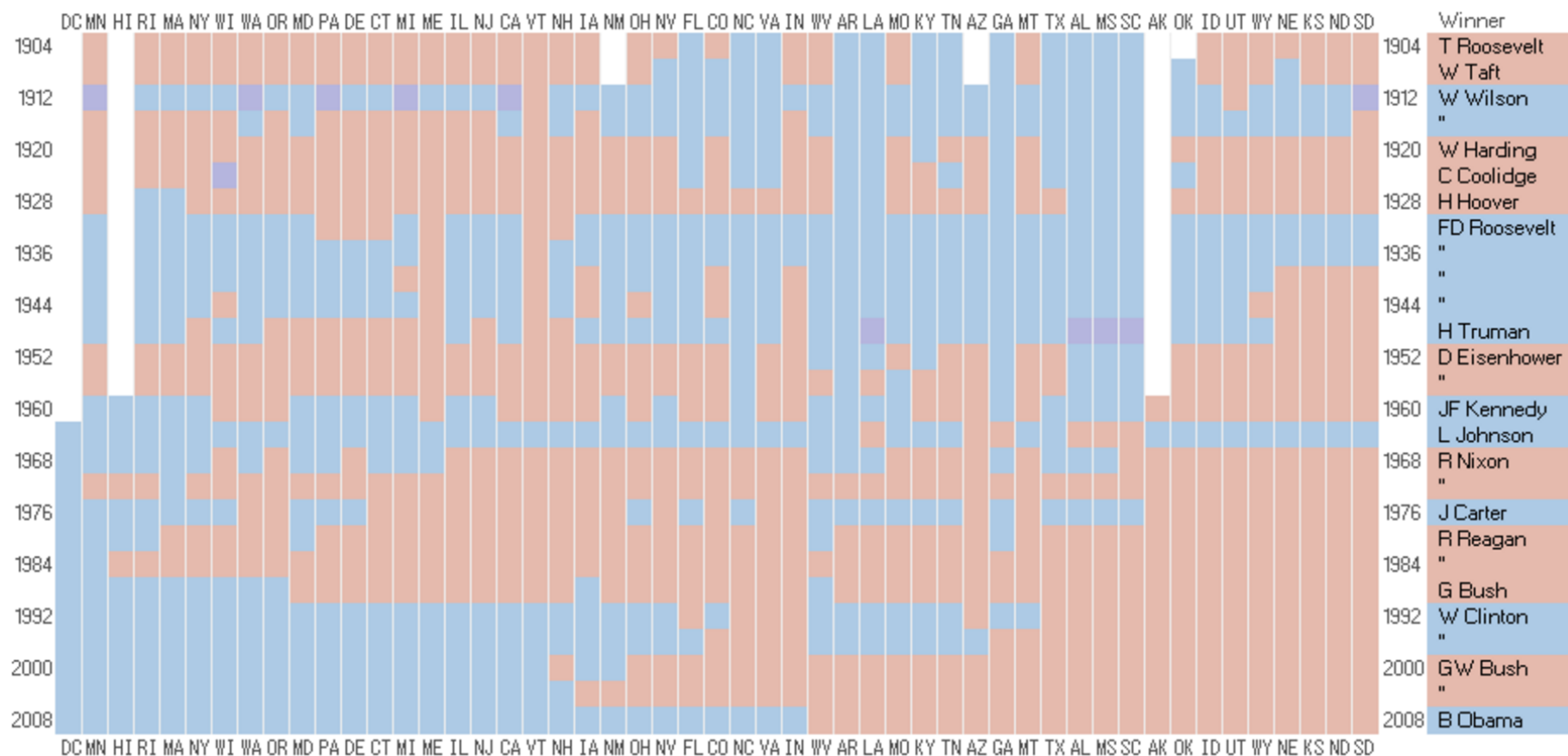
Practical advice:

CHOOSE AN **ASPECT RATIO** THAT
EMPHASIZES THE IMPORTANT DETAILS
FOR YOUR TASK

[TALBOT ET AL, 2011]

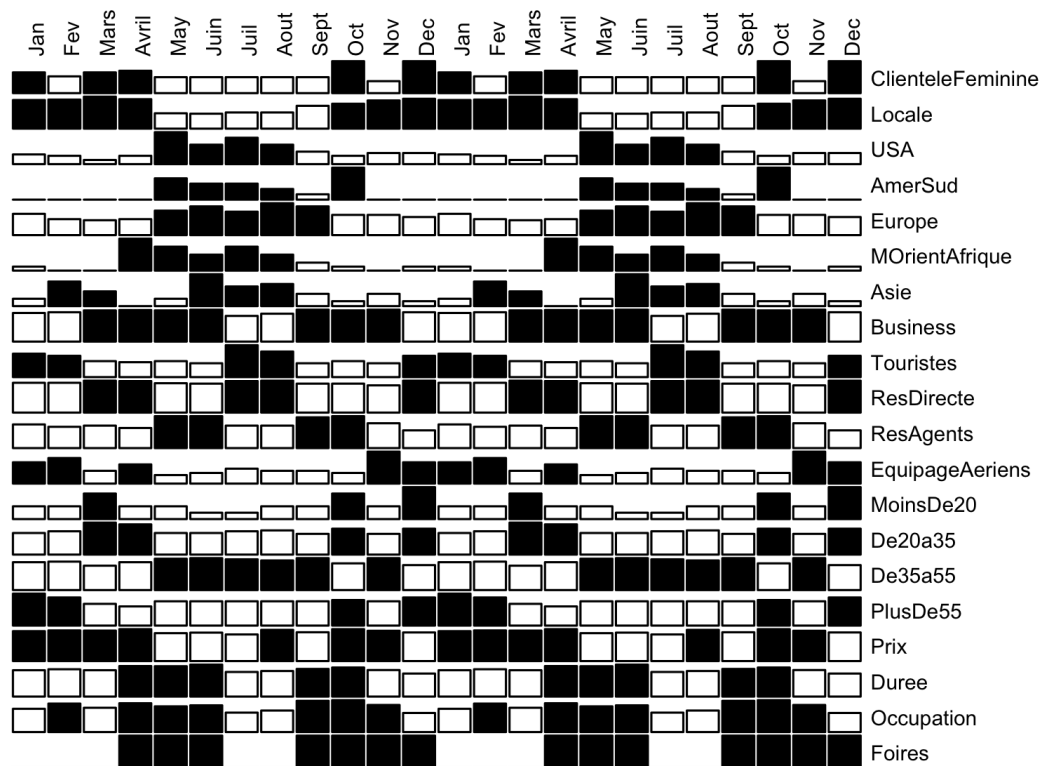
MATRIX ALIGNMENT

Two keys

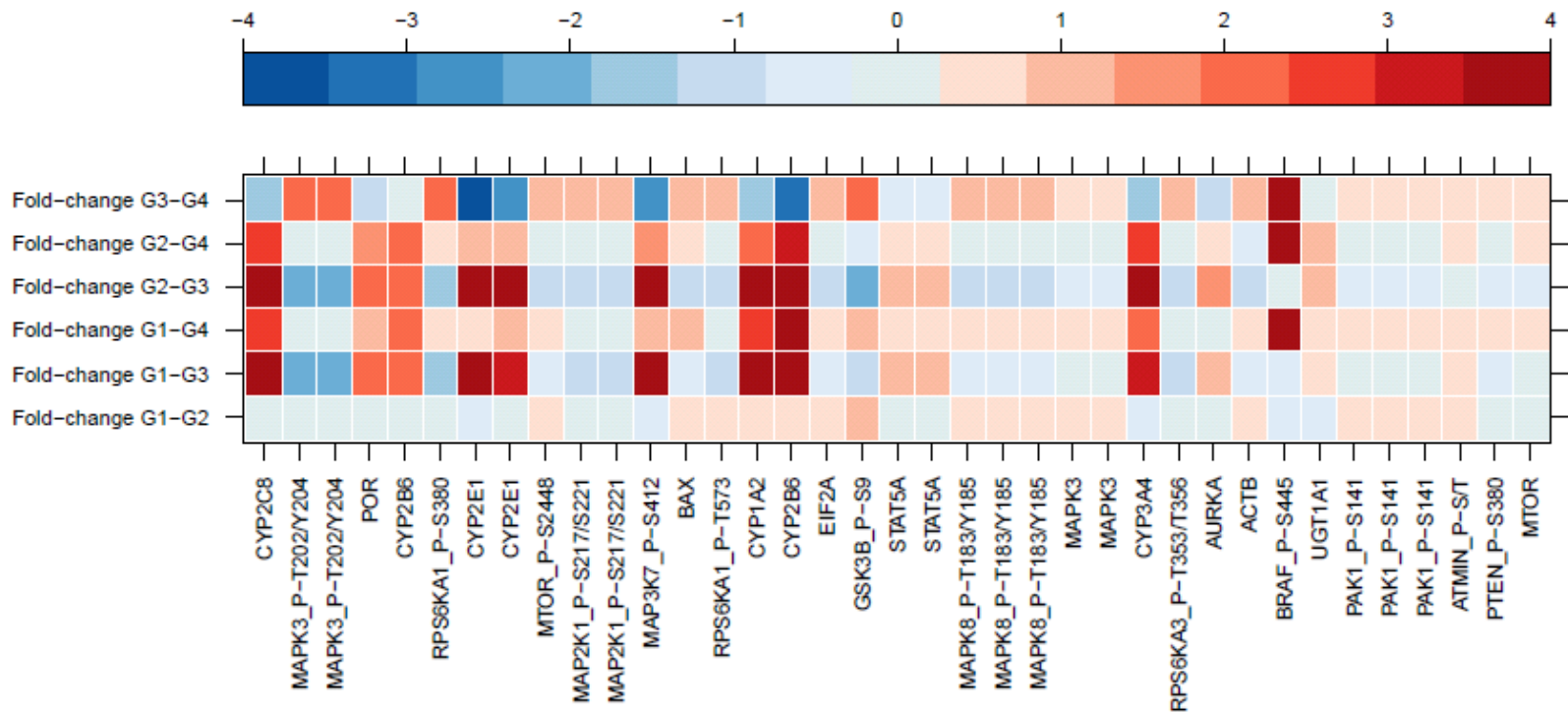


HEATMAP

Hotel 2

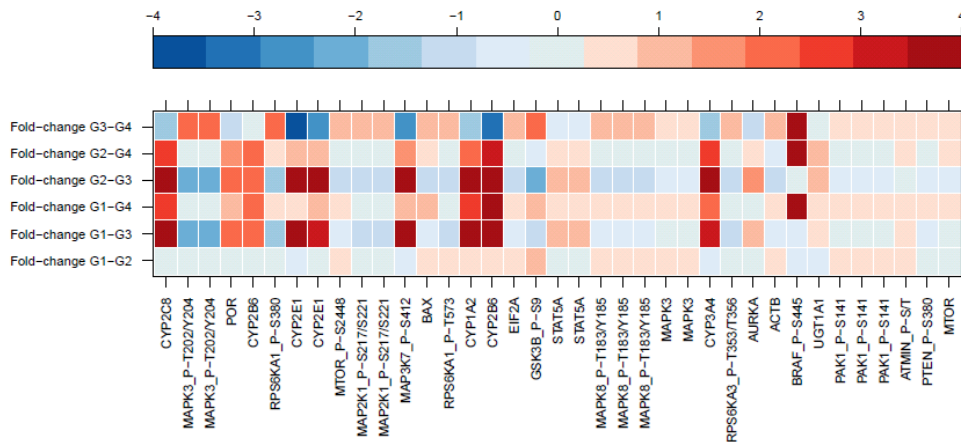


HEATMAP

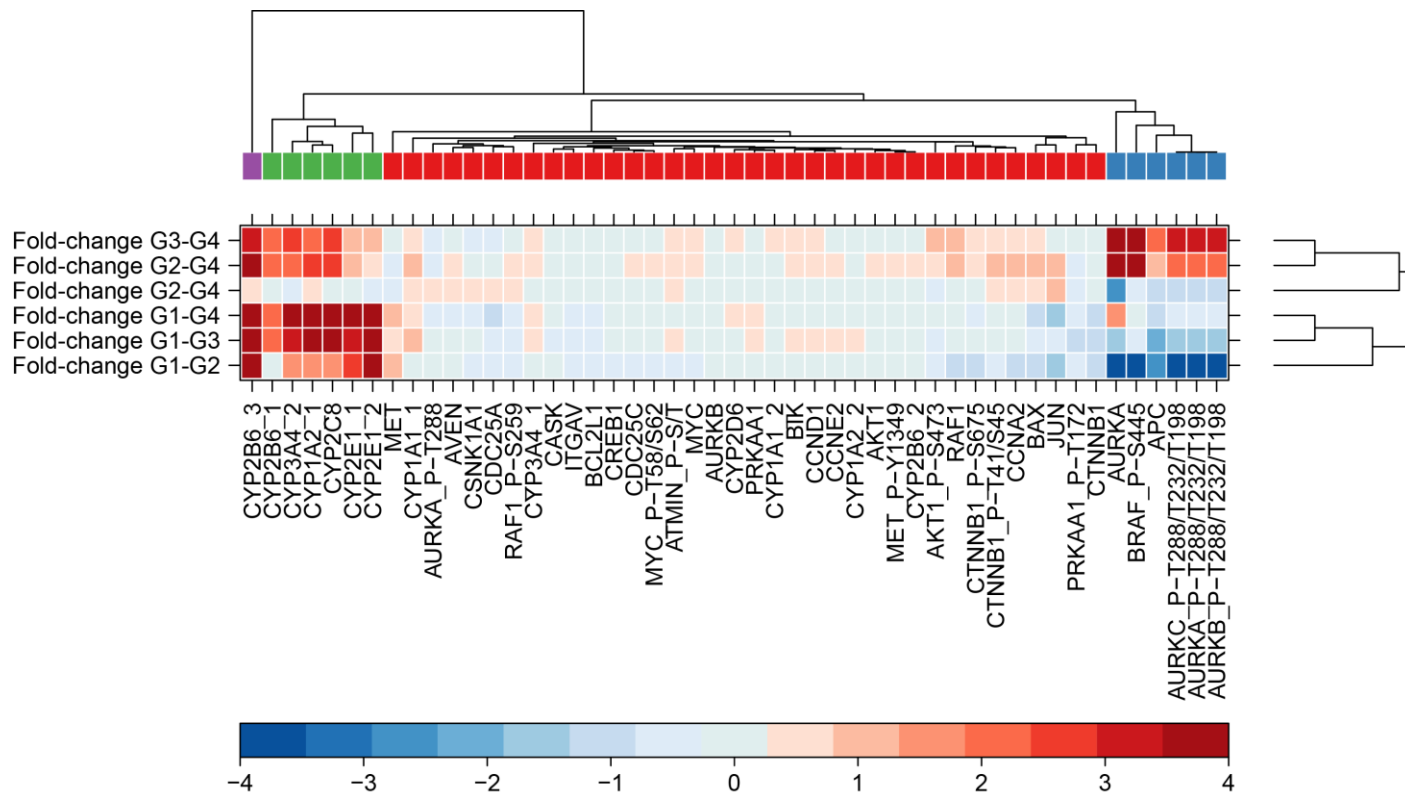


HEATMAP

| | |
|--------|---|
| DATA | Table; two categorical key attributes, one quantitative value attribute |
| ENCODE | 2D matrix alignment of area marks, e.g. with diverging color map |
| TASK | find clusters, outliers; summarize |
| SCALE | items: ~1 million (on 1000x1000px), categorical attribute levels: hundreds, quantitative attribute levels: 3-11 |



CLUSTERED HEATMAP



3D Map of Land Values in Japan: 1989 - 2019

26,000 points of official land prices of the whole country for the past 30 years

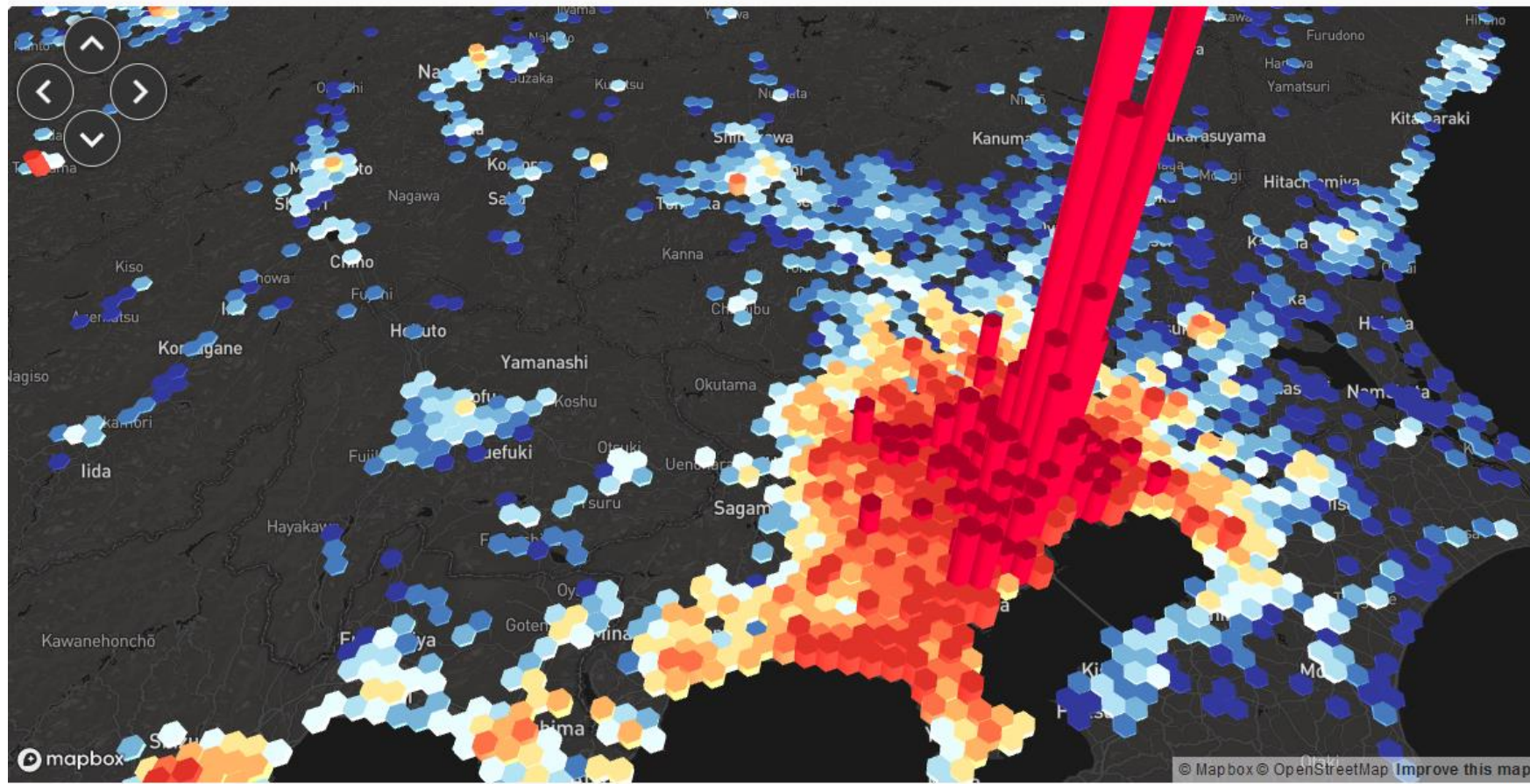
3rd April 2019

JAPANESE

Latest value

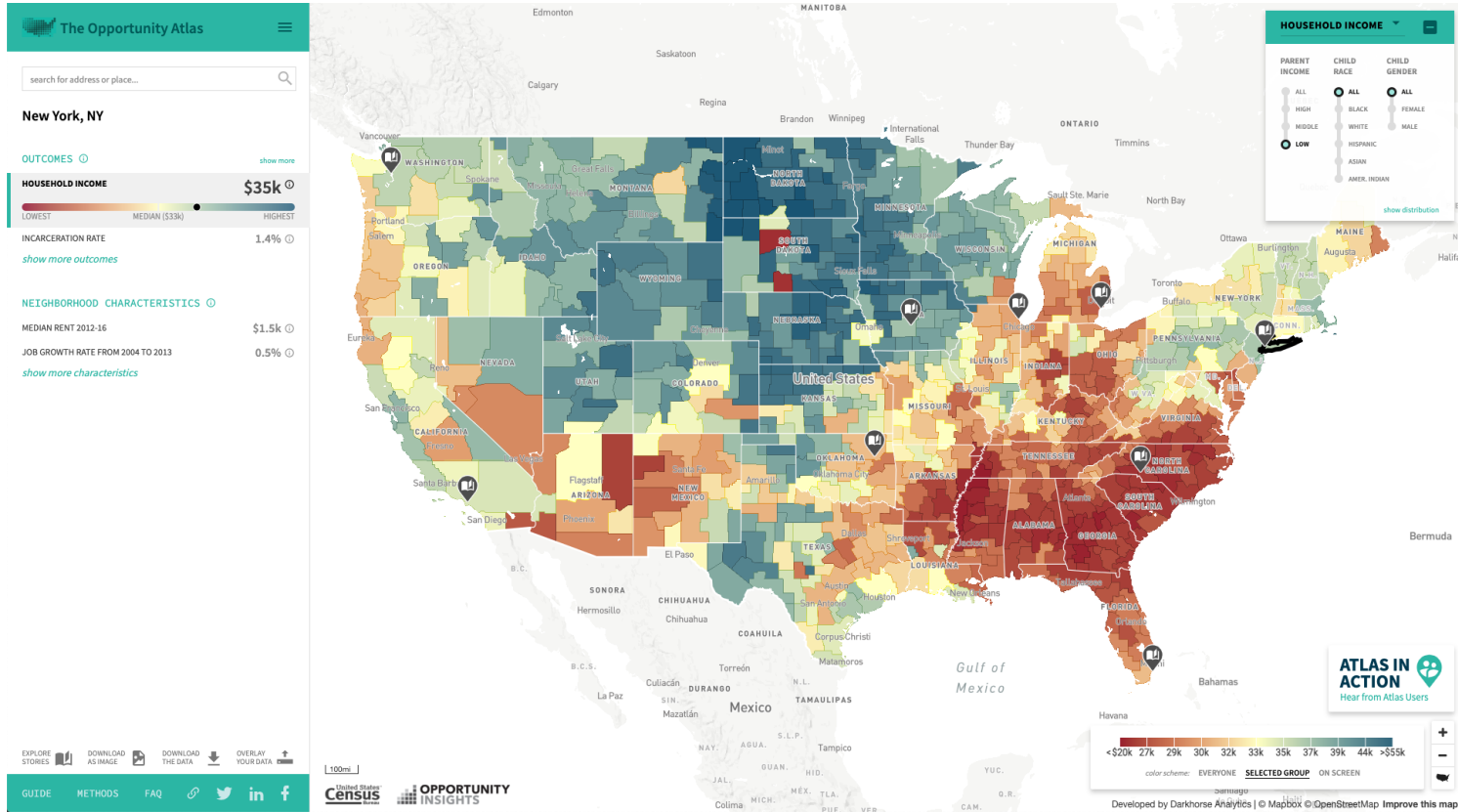


All points



<https://toyokeizai.net/sp/visual/tko/landprices3/en.html>

CLOROPLETH MAP



Uses heatmap idea

BACK TO OUR ORIGINAL EXAMPLE

| Country | Income per person | Life expectancy | Children per woman |
|-------------|-------------------|-----------------|--------------------|
| Afghanistan | 850 | 57 | 7.1 |
| France | 29500 | 81 | 1.9 |
| US | 41000 | 78 | 2.1 |

now with 4 attributes

200 years

Suggestions?

\$0



Afghanistan



France



US

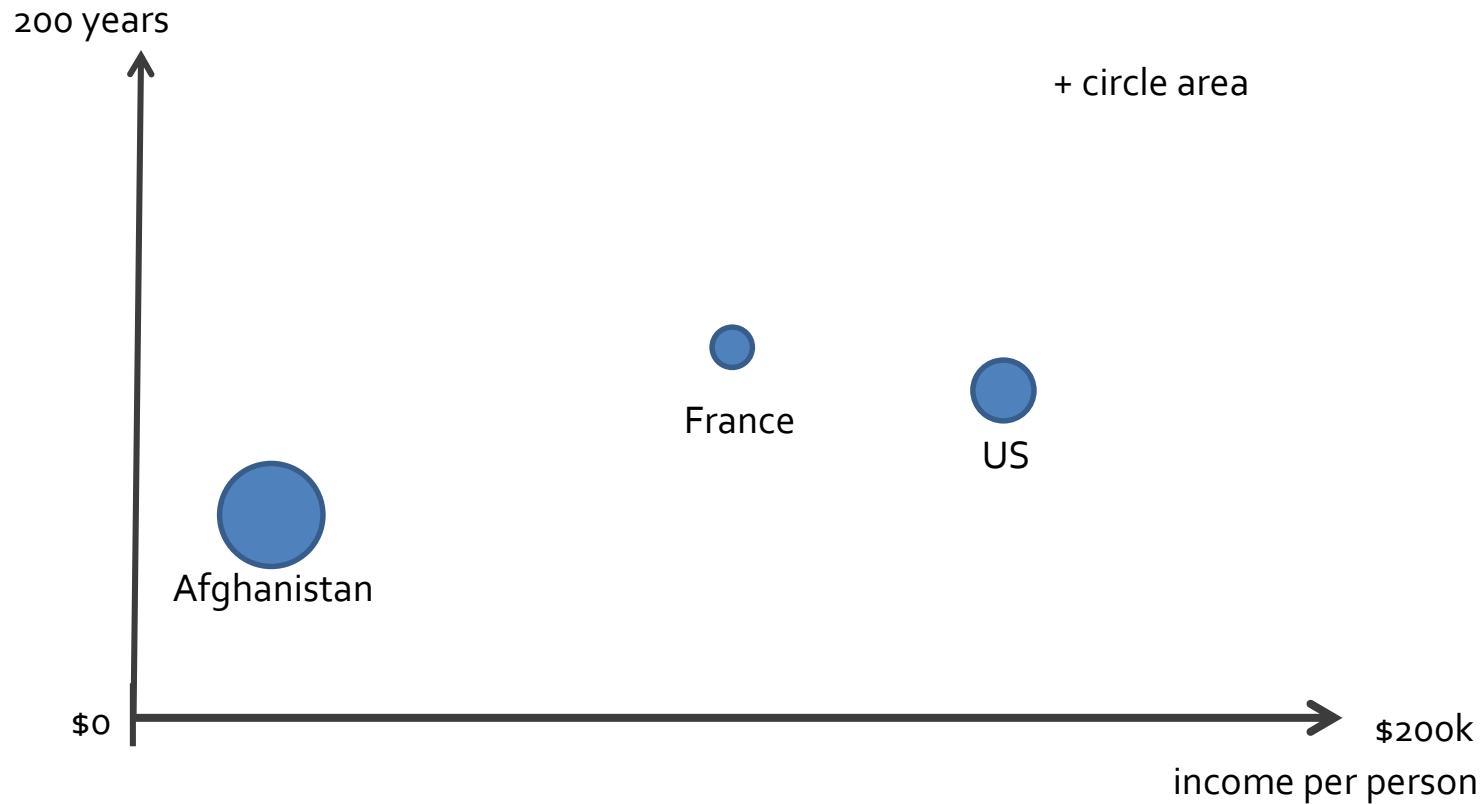


\$200k

income per person

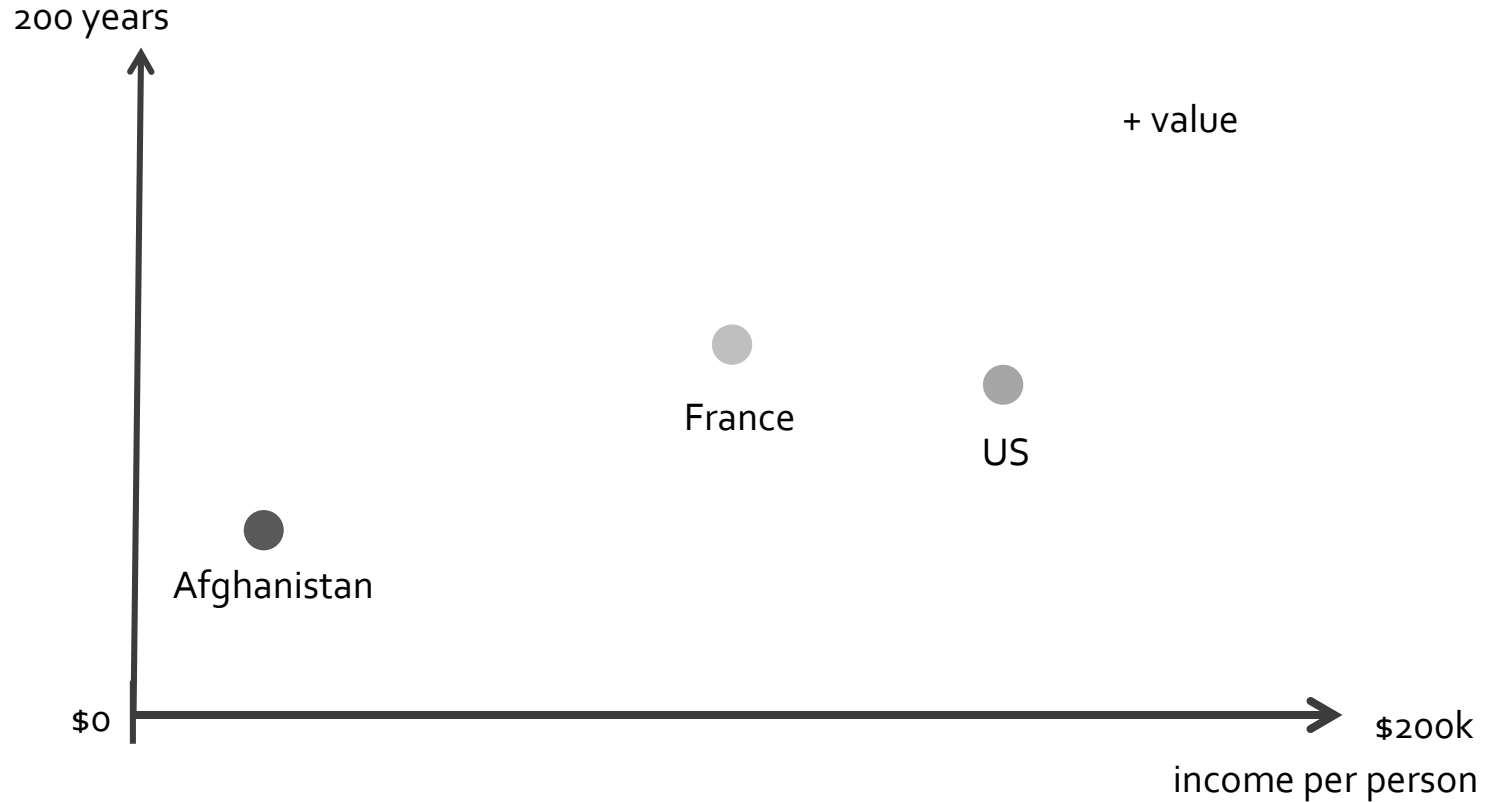
| Country | Income per person | Life expectancy | Children per woman |
|-------------|-------------------|-----------------|--------------------|
| Afghanistan | 850 | 57 | 7.1 |
| France | 29500 | 81 | 1.9 |
| US | 41000 | 78 | 2.1 |

ADD ANOTHER VISUAL ENCODING



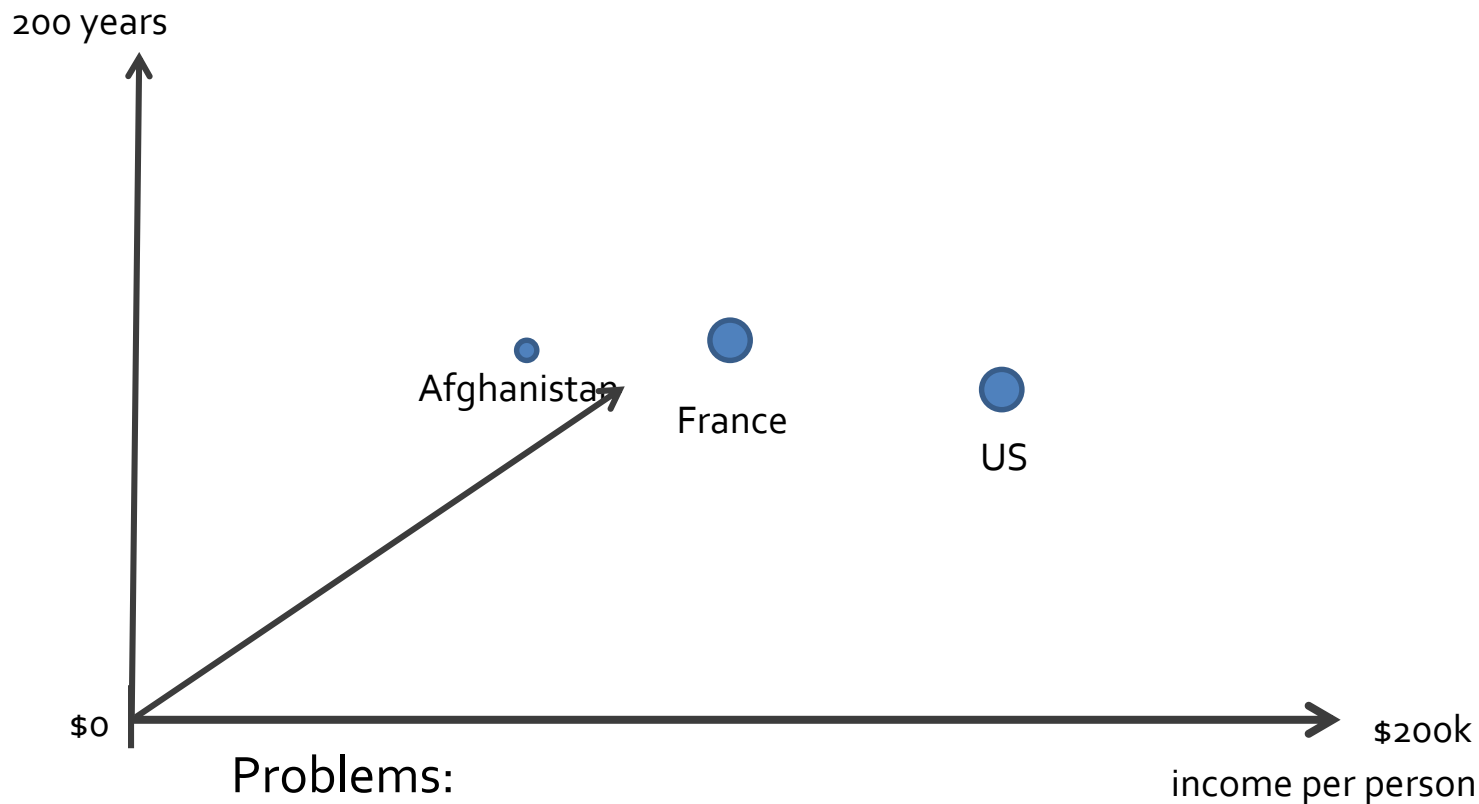
Problem:
Does not scale well to more attributes

ADD ANOTHER VISUAL ENCODING



Problem:
Does not scale well to more attributes

ADD AN AXIS

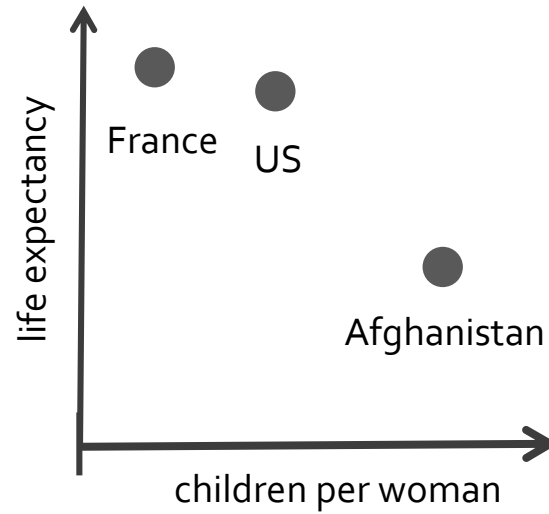
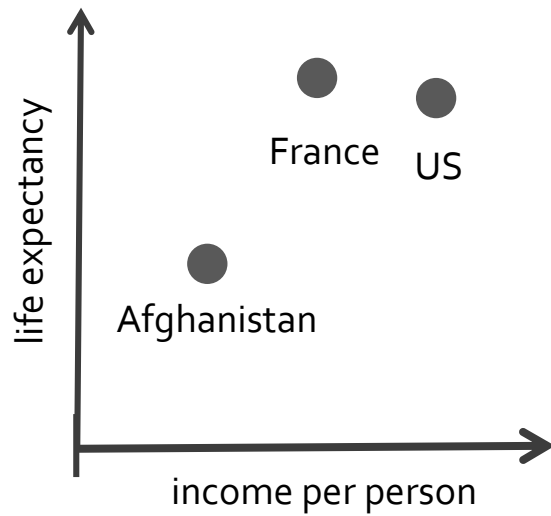


Problems:

Occlusion, perspective distortion, does not scale

→ Not usually recommended

ADD AN AXIS



SCATTERPLOT MATRIX

This idea scales relatively well

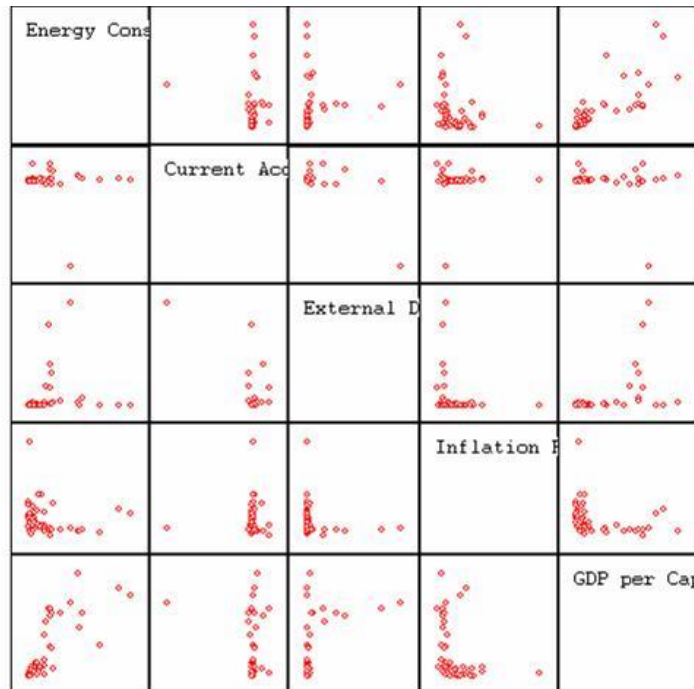


Image Source: Wikipedia

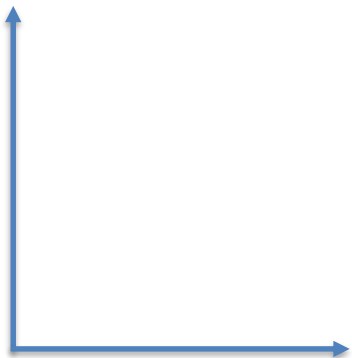
GraphDice: A System for Exploring Multivariate Social Networks

A. Bezerianos
F. Chevalier
P. Dragicevic
N. Elmqvist
J-D. Fekete

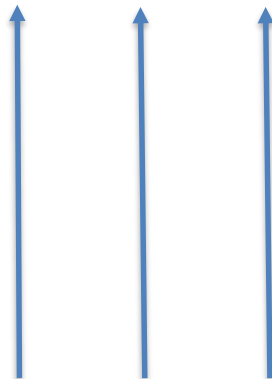
INRIA
École Centrale Paris
Purdue University

SPATIAL AXIS ORIENTATION

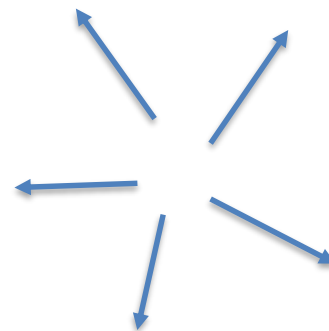
An additional design choice



rectilinear



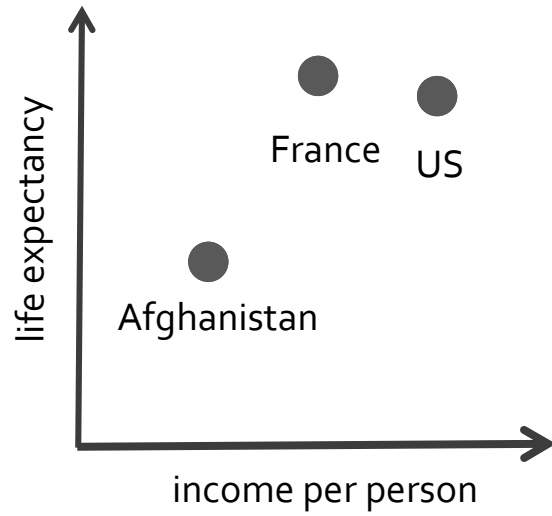
parallel



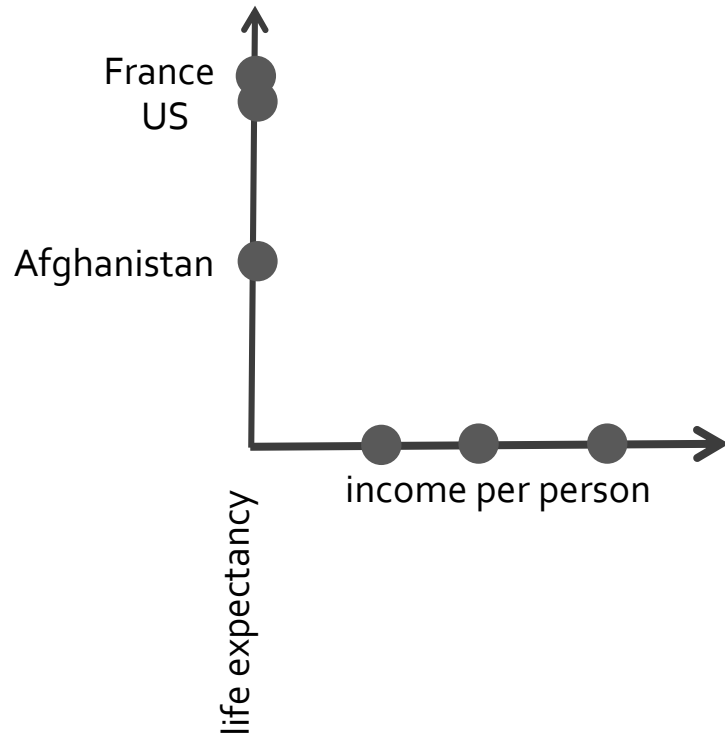
radial

parallel coordinates

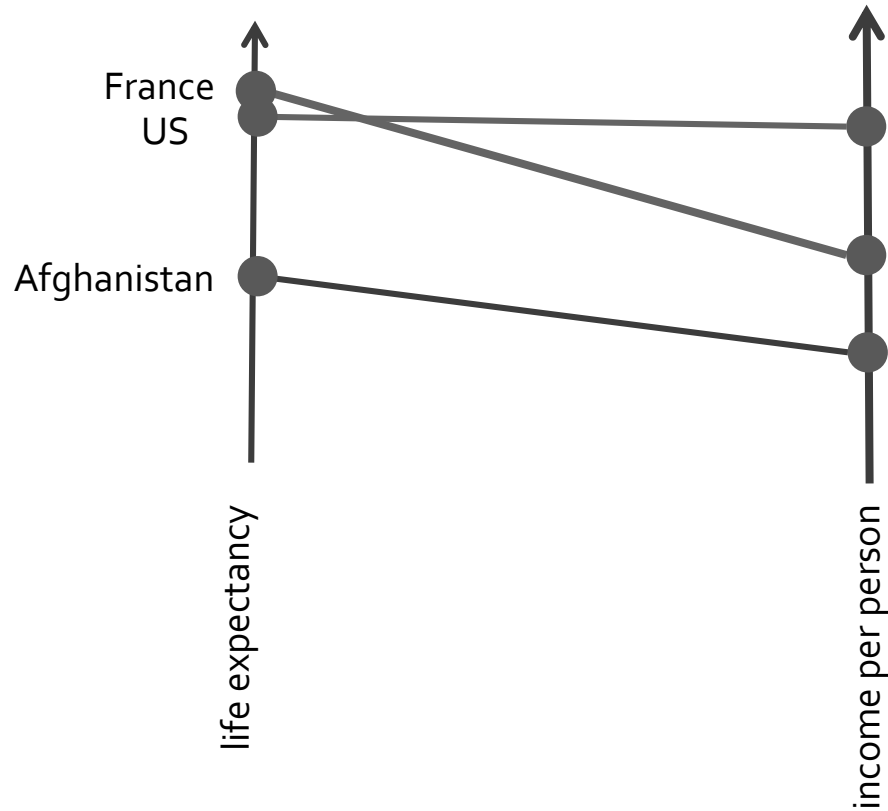
Back to our original example



Parallel Coordinates



parallel coordinates



- show correlations between neighboring axes

MULTIDIMENSIONAL DETECTIVE

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&

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Abstract

The display of multivariate datasets in parallel coordinates, transforms the search for *relations* among the variables into a 2-D pattern recognition problem. This is the basis for the application to *Visual Data Mining*. The Knowledge Discovery process together with some general guidelines are illustrated on a dataset from the production of a VLSI chip. The special strength of parallel coordinates is in modeling **relations**. As an example, a simplified Economic Model is constructed with data from various economic sectors of a real country. The visual model shows the interrelationship and dependencies between the sectors, circumstances where there is competition for the same resource, and feasible economic policies. Interactively, the model can be used to do trade-off analyses, discover sensitivities, do approximate optimization, monitor (as in a Process) and Decision Support.

Introduction

In Geometry parallelism, which does not require a notion of angle, rather than orthogonality is the more fundamental concept. This, together with the fact that orthogonality "uses-up" the plane very

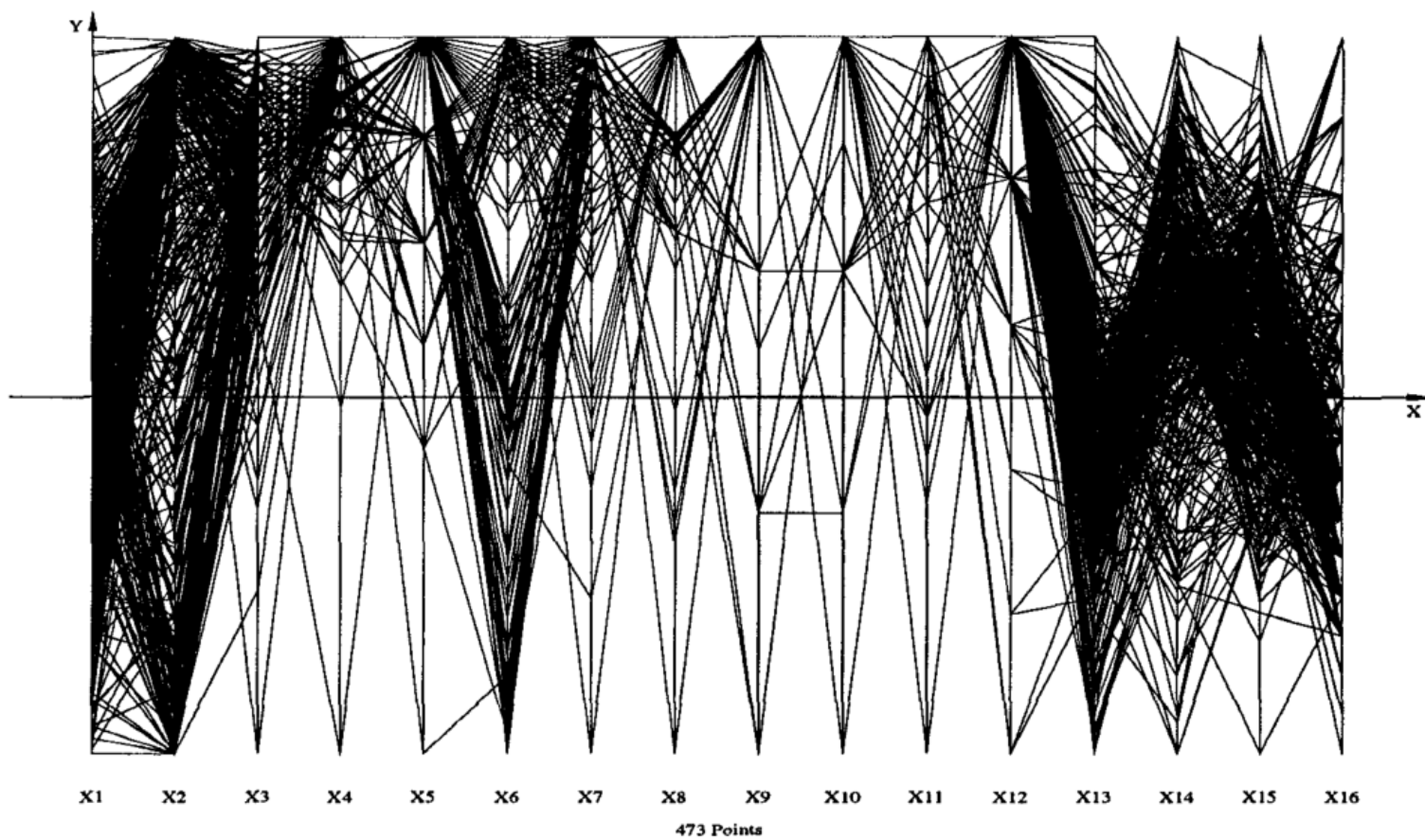
fast, was the inspiration in 1959 for "Parallel" Coordinates. The systematic development began in 1977 [4]. The goals of the program were and still are (see [6] and [5] for short reviews) the visualization of multivariate/multidimensional problems without loss of information and having the properties:

1. Low representational complexity. Since the number of axes, N equals the number of dimensions (variables) the complexity is $O(N)$,
2. Works for any N ,
3. Every variable is treated uniformly (unlike "Chernoff Faces" and various types of "glyphs"),
4. The displayed object can be recognized under projective transformations (i.e. rotation, translation, scaling, perspective),
5. The display easily/intuitively conveys information on the properties of the N -dimensional object it represents,
6. The methodology is based on rigorous mathematical and algorithmic results.

Parallel coordinates (abbr.||-coords) transform multivariate relations into 2-D patterns, a property that is well suited for Visual Data Mining.

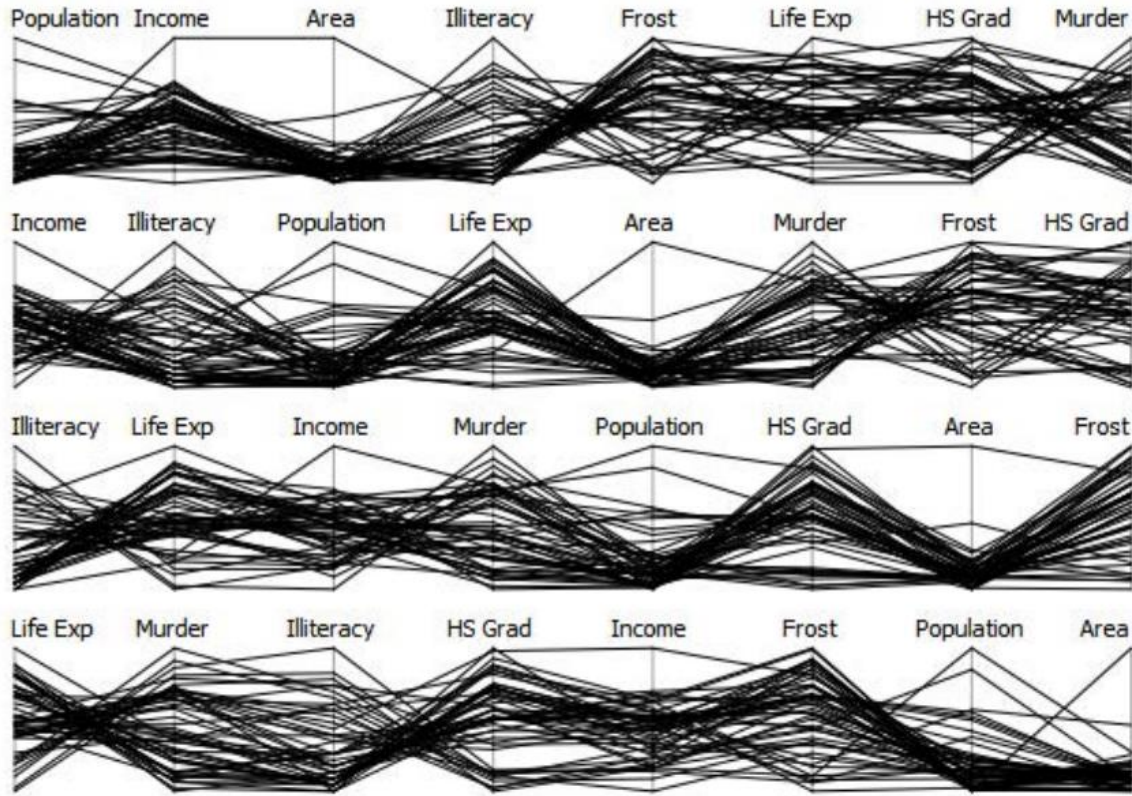
* Senior Fellow San Diego SuperComputing Center

[†]36A Yehuda Halevy Street, Raanana 43556, Israel



Original Example from Inselberg 1997

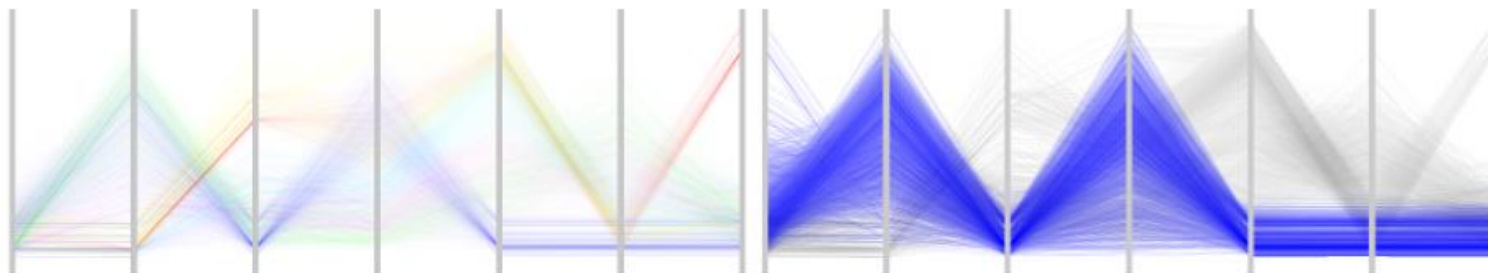
THE ORDER OF AXES MATTERS



Eurographics 2013, STAR Report
J. Heinrich, D. Weiskopf

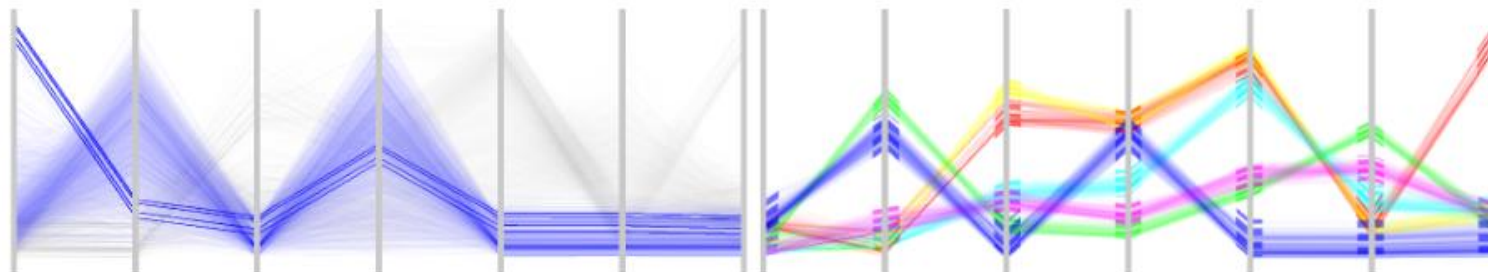
REDUCE CLUTTER - HIGHLIGHT CLUSTERS

Lots of work on this. For example:



(a) A linear transfer function has been applied to the high-precision texture in order to prevent cluttering and to provide overview of the data.

(b) A logarithmic transfer function is applied to a selected cluster. The structure is preserved and emphasis is put on the low density regions.



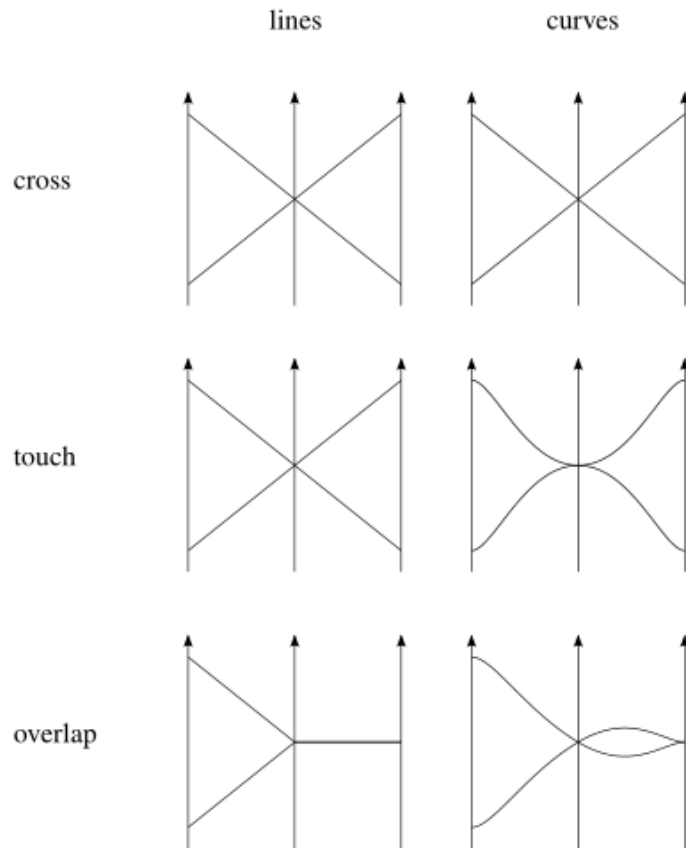
(c) Local cluster outliers are enhanced. A square root transfer function is used and the outliers are visible even through high-density regions.

(d) A complementary view of the clusters with uniform bands. 'Feature animation' presents statistics about the clusters and acts as a guidance.

Revealing Structure within Clustered Parallel
Coordinates Displays, InfoVis 2005

HOW TO DRAW THE LINES

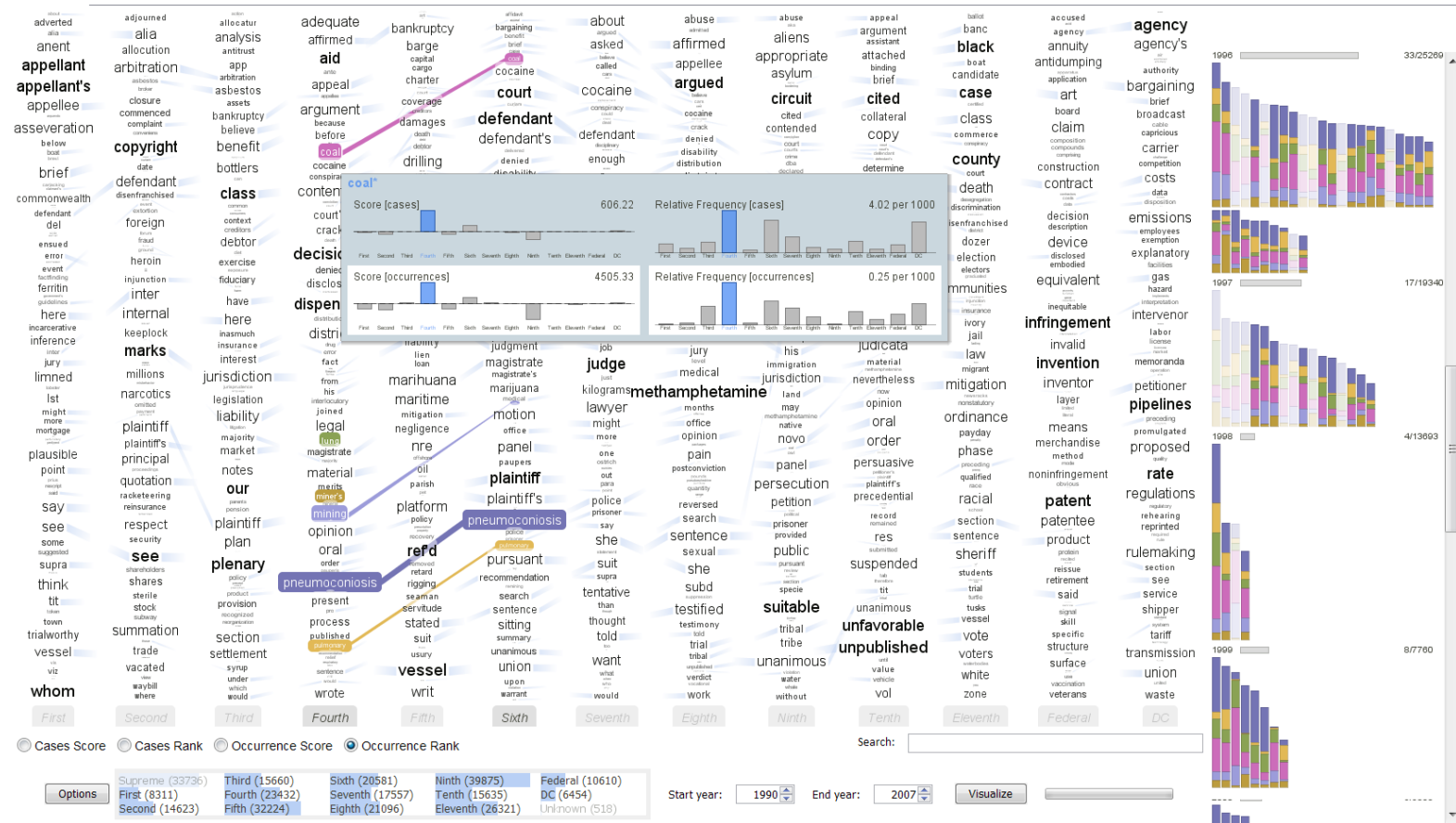
Goal: avoid ambiguity



Eurographics 2013, STAR Report
J. Heinrich, D. Weiskopf

COMBINE WITH OTHER VISUALIZATION TECHNIQUES

Parallel Tag Clouds to Explore Faceted Text Corpora (Collins et al., VAST 2009)



THERE IS MUCH MORE ON THIS...

Start here if you want more information

EUROGRAPHICS 2013/ M. Sbert, L. Szirmay-Kalos

STAR – State of The Art Report

State of the Art of Parallel Coordinates

J. Heinrich and D. Weiskopf

Visualization Research Center, University of Stuttgart

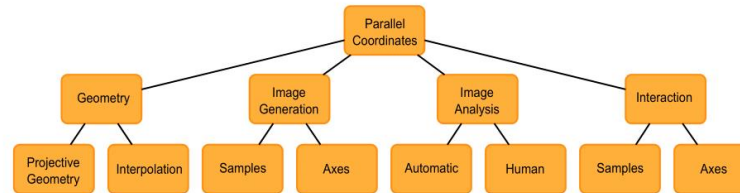


Figure 1: Taxonomy of topics for parallel coordinates in the scientific literature. The first-level nodes each represent a section in this paper, where the scope and definition of each topic will be explained.

Abstract

This work presents a survey of the current state of the art of visualization techniques for parallel coordinates. It covers geometric models for constructing parallel coordinates and reviews methods for creating and understanding visual representations of parallel coordinates. The classification of these methods is based on a taxonomy that was established from the literature and is aimed at guiding researchers to find existing techniques and identifying white spots that require further research. The techniques covered in this survey are further related to an established taxonomy of knowledge-discovery tasks to support users of parallel coordinates in choosing a technique for their problem at hand. Finally, we discuss the challenges in constructing and understanding parallel-coordinates plots and provide some examples from different application domains.

Categories and Subject Descriptors (according to ACM CCS): I.3.3 [Computer Graphics]: Picture/Image Generation—Line and curve generation

Scattering Points in Parallel Coordinates

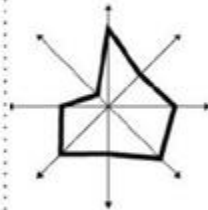
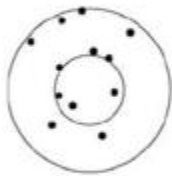
Xiaoru Yuan¹, Peihong Guo¹, He Xiao¹, Hong Zhou², Huamin Qu²

1. Key Laboratory of Machine Perception (MOE), School of EECS, Peking University

2. Department of Computer Science and Engineering at Hong Kong University of Science and Technology,
Clear Water Bay, Kowloon, Hong Kong

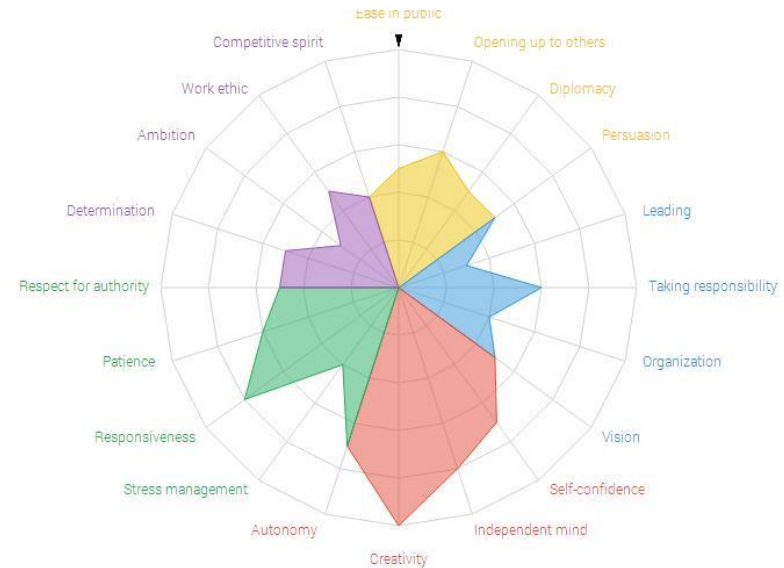
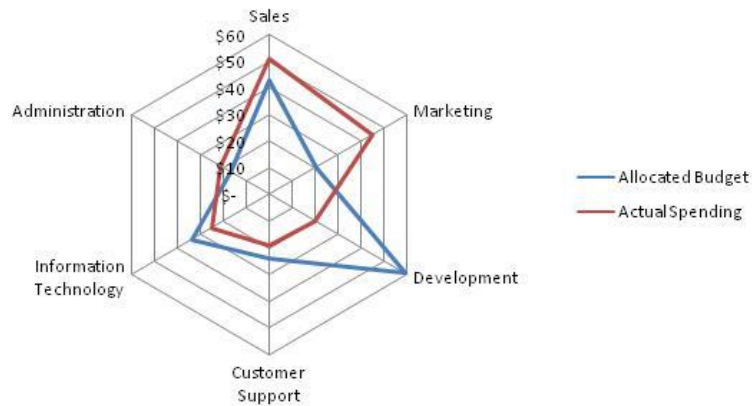
RADIAL AXES

Polar

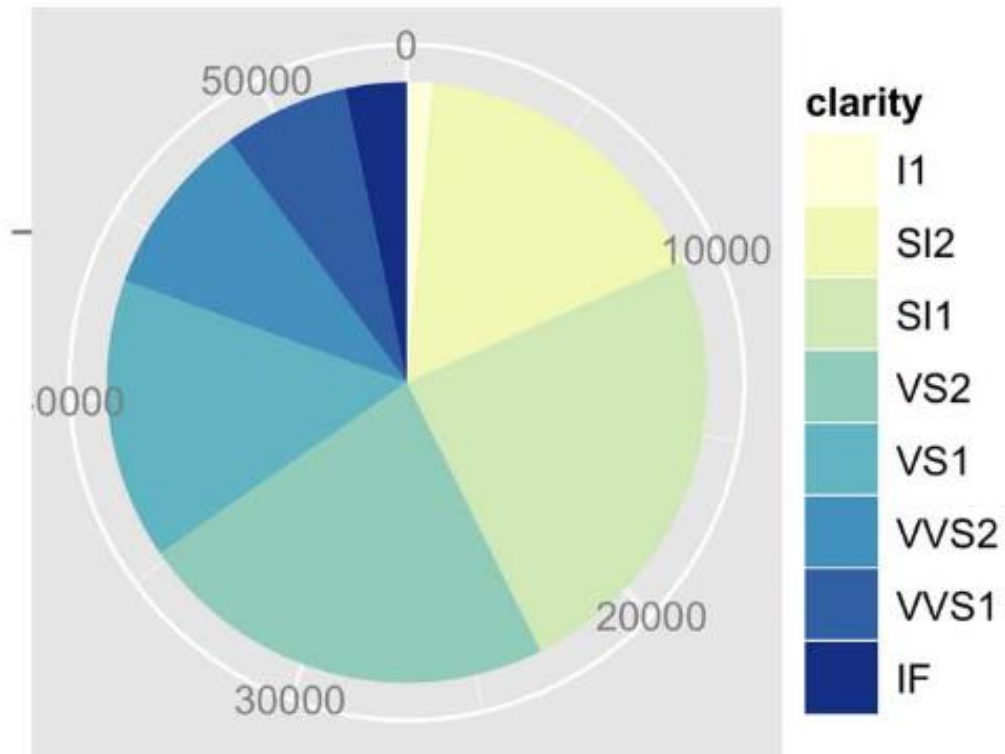


EXAMPLE: STAR PLOT

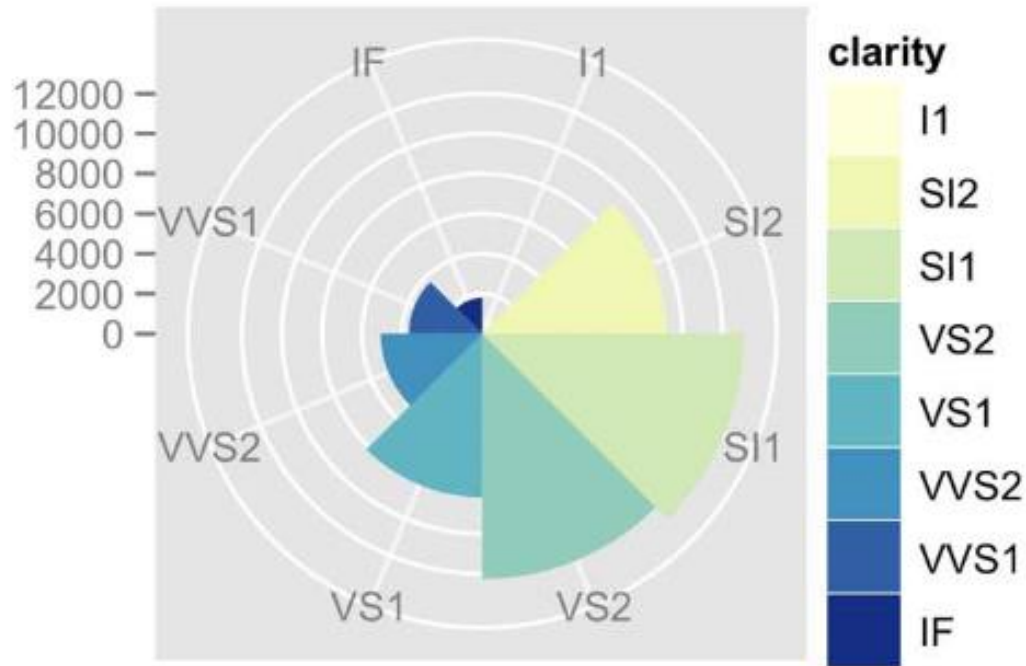
- = radial line chart



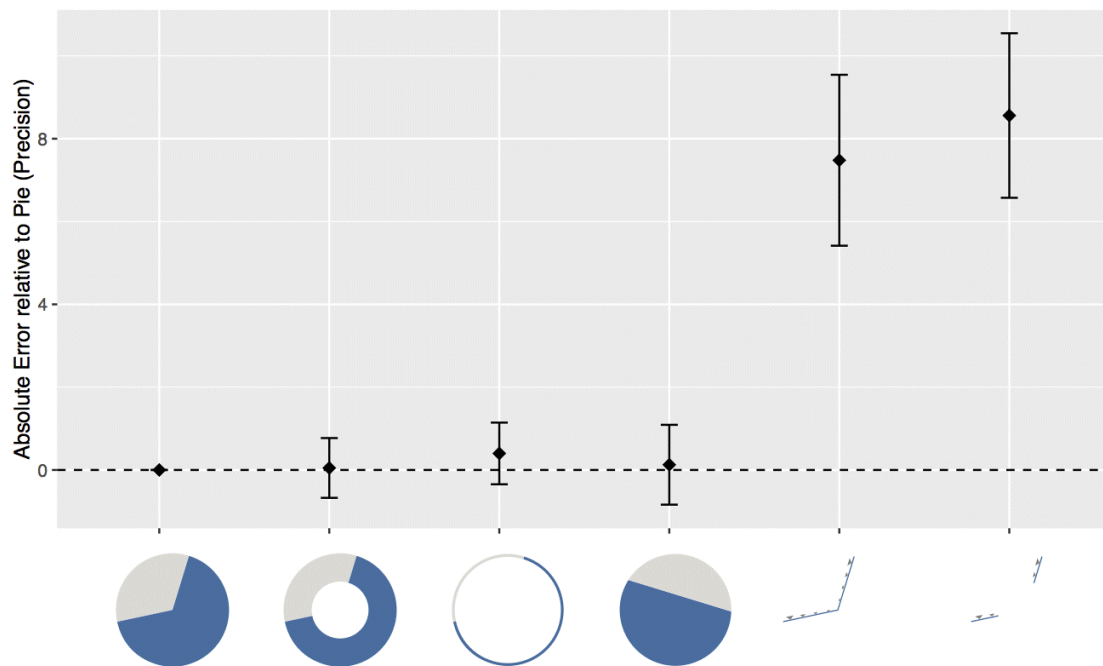
PIE CHARTS



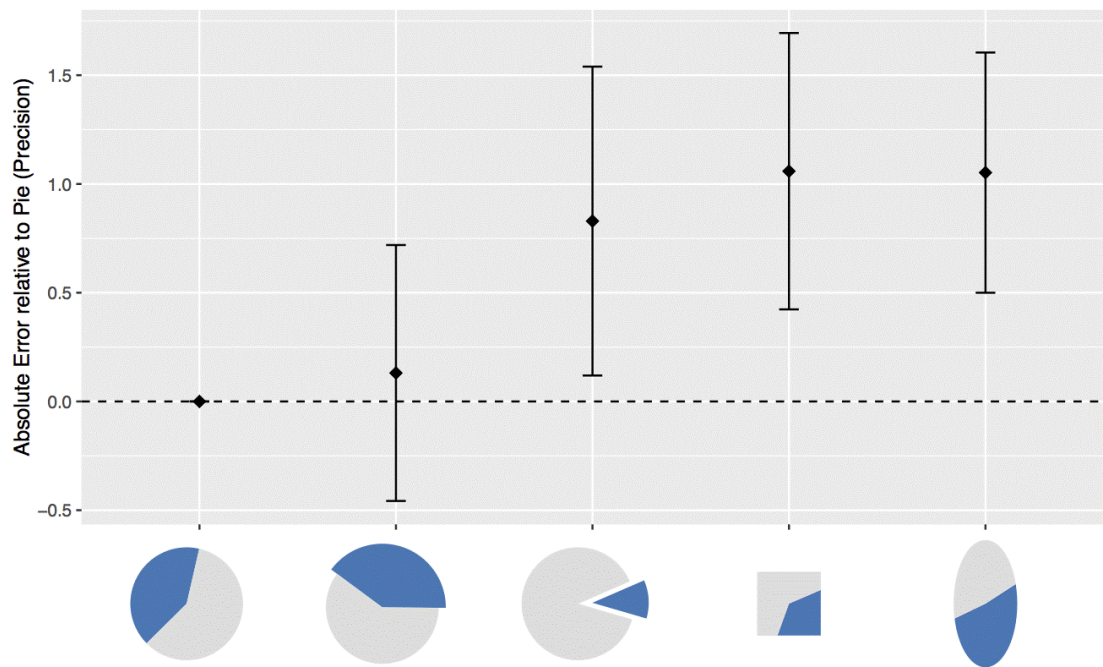
POLAR AREA CHARTS



HOW DO PEOPLE READ PIE CHARTS?

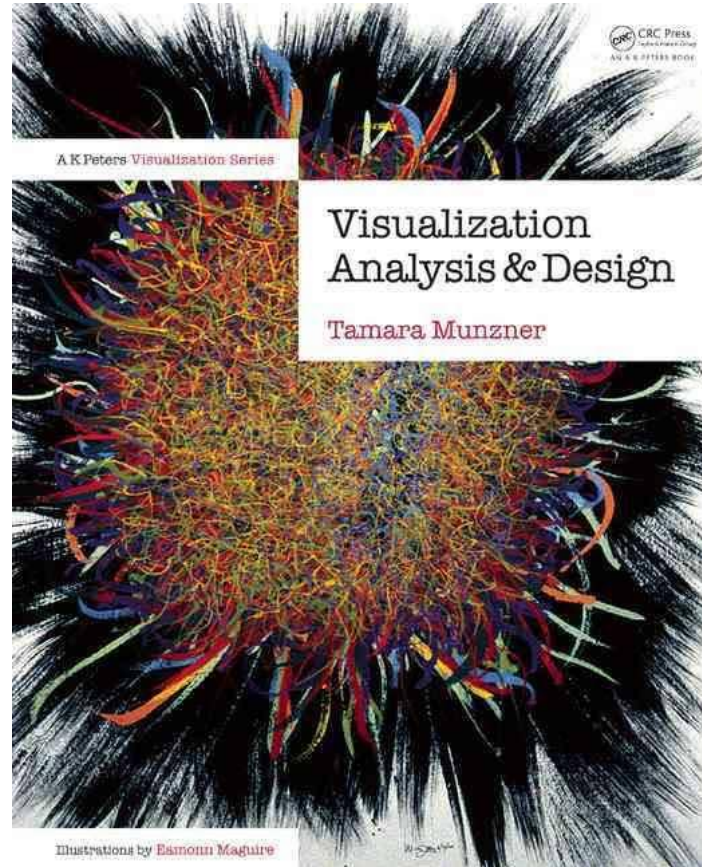


HOW DO PEOPLE READ PIE CHARTS?



WHAT IF ONE DIMENSION IS TIME?

READINGS



ACKNOWLEDGEMENTS

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- Wesley Willett (University of Calgary)
- Pierre Dragicevic (Inria)
- Uta Hinrichs (University of St. Andrews)