VISUALIZING MULTI-ATTRIBUTE DATA

DATA TABLES

Petra Isenberg

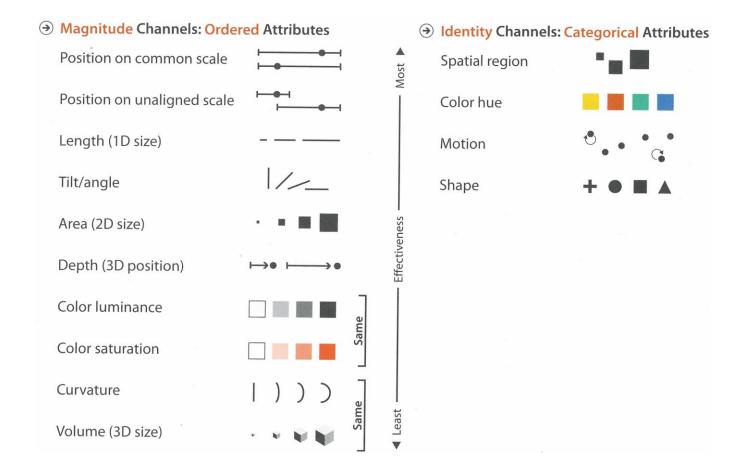


RECAP

you have learned about

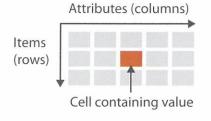
- visual variables and marks
- that their perceptual properties matter

RECAP

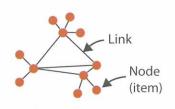


RECAP

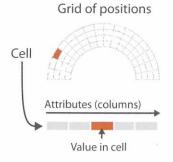
→ Tables



→ Networks



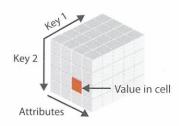
→ Fields (Continuous)



→ Geometry (Spatial)



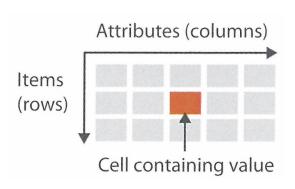
→ Multidimensional Table



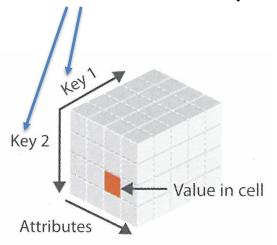
→ Trees



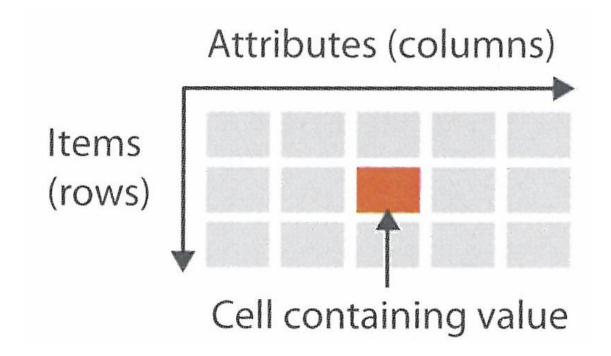
DATA TABLES - TERMINOLOGY



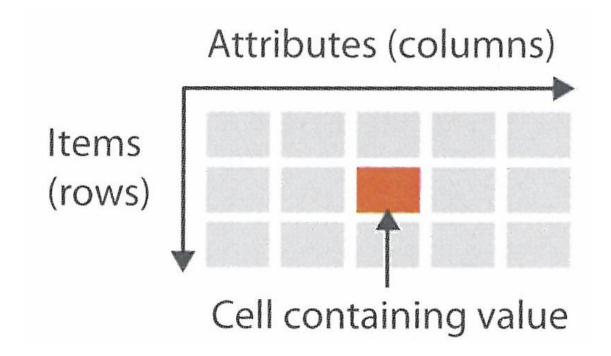
index to look up values



WHAT COULD BE THE KEY HERE?



WHAT DATA TYPE IS SUITABLE FOR A KEY?



KEYS VS. VALUES

key attributes are also sometimes called:

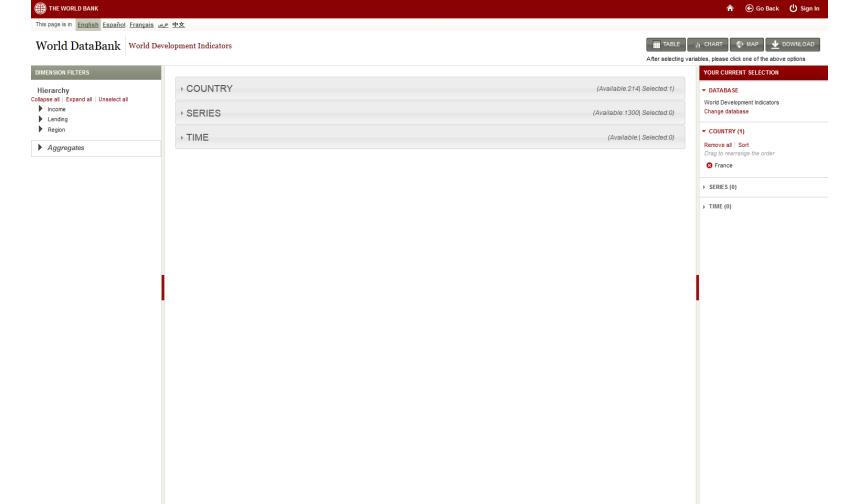
- independent attribute
- dimension

value attributes are also sometimes called:

- dependent attribute
- measure

LEVELS

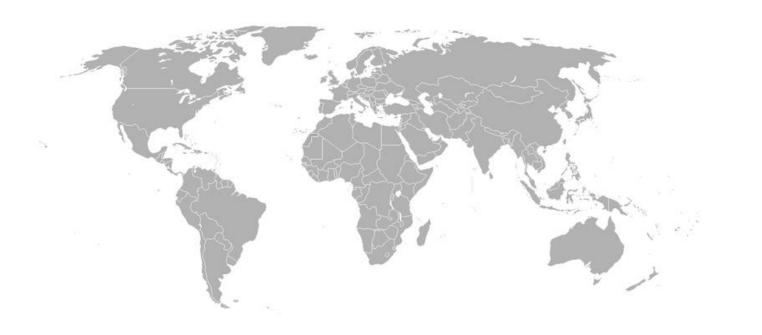
= unique values for a categorical or ordered attribute



Fraud & Corruption Hotline

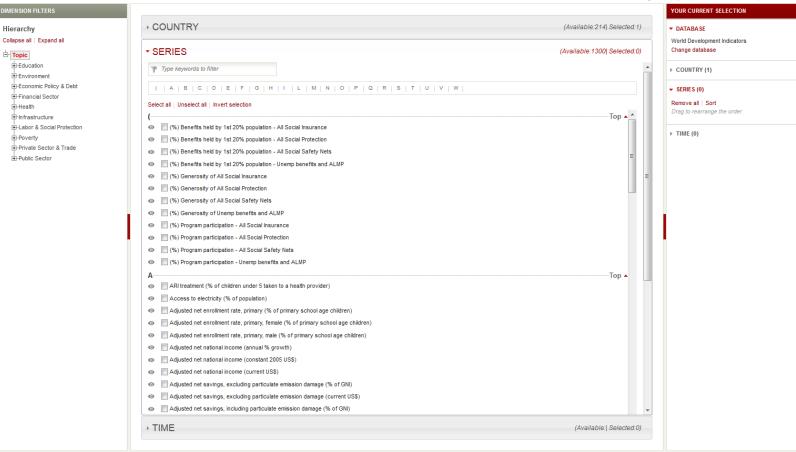
214 countries

Afghanistan	Albania	Algeria	Andorra	Angola	Argentina	Armenia	Aruba	Australia	



World DataBank World Development Indicators





214 countries

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	Afghanistan	Albania	Algeria	Andorra	Angola	Argentina	Armenia	Aruba	Australia	
Benefits										
Generosity										
Participation										
Savings										
Interest										
Bird species										
Birth Rate										
C02 Emissions										









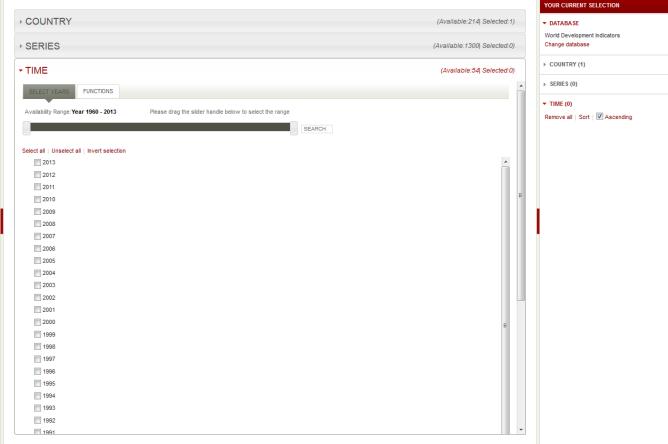
This page is in English Español Français 中文

World DataBank | World Development Indicators

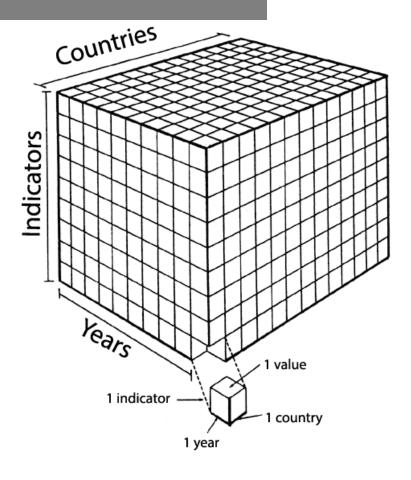


After selecting variables, please click one of the above options

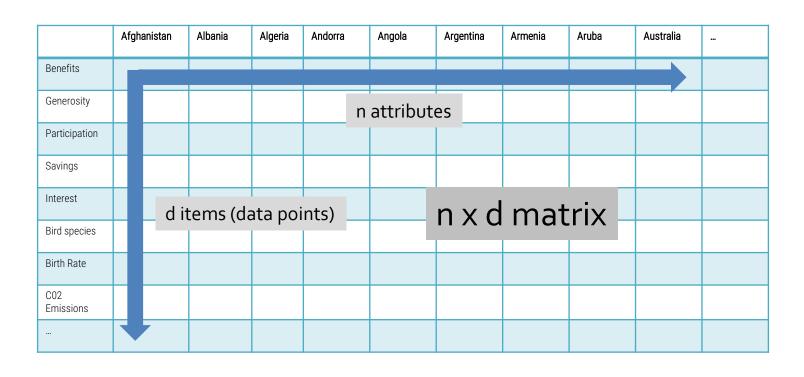




THE DATA CUBE



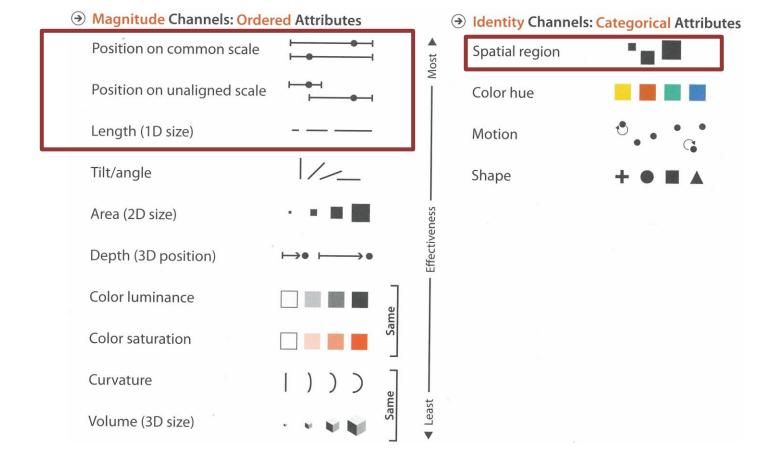
MULTI-ATTRIBUTE DATA – OUR VIEW TODAY



ARRANGING TABULAR DATA

In Space

WHY ARRANGING DATA



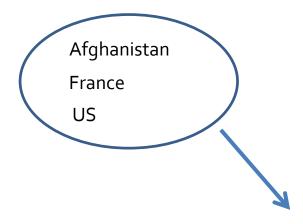
QUANTITATIVE VALUES

APPROACH

 Let's start with two attributes: country & income per person

Country	Income per person
Afghanistan	850
France	29500
US	41000

1. FIND A LAYOUT

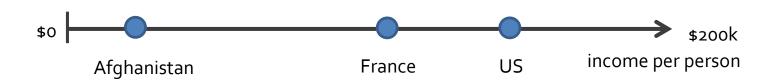


Country	Income per person
Afghanistan	850
France	29500
US	41000

\$0

2. CHOOSE A VISUAL ENCODING & MARK

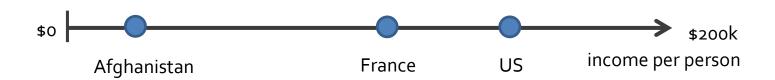
E.g. position + circle



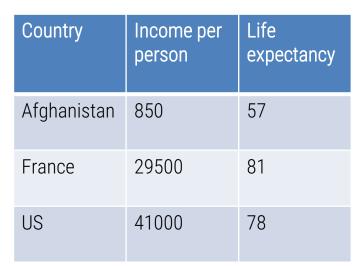
1. FIND A LAYOUT

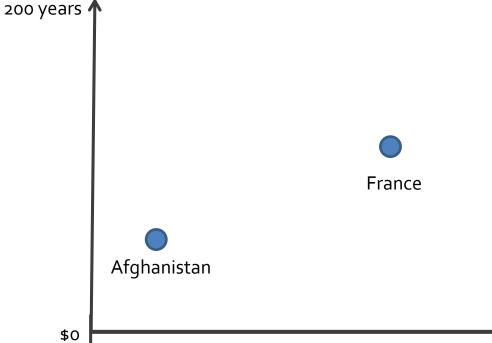
Country	Income per person	Life expectancy
Afghanistan	850	57
France	29500	81
US	41000	78

How do we extend this to 3 data attributes?



1. FIND A LAYOUT



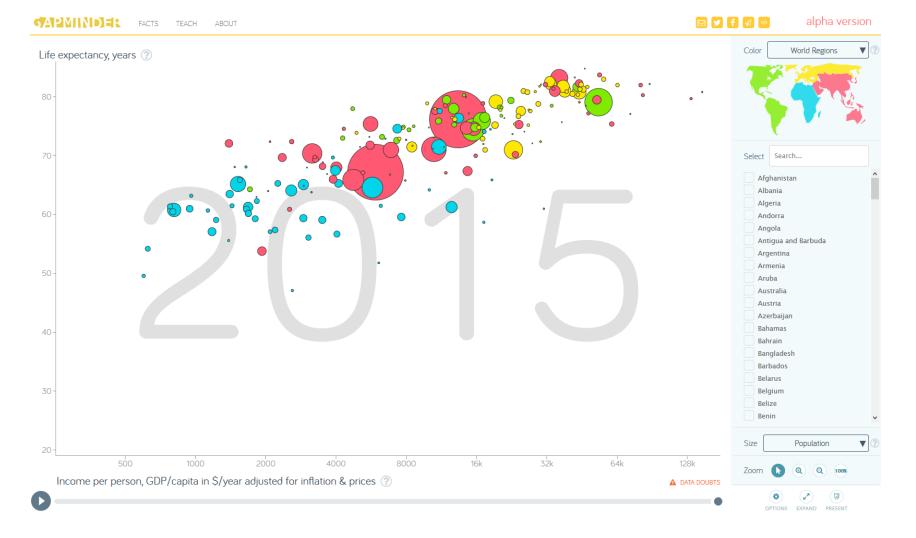




\$200k income per person

SCATTERPLOTS

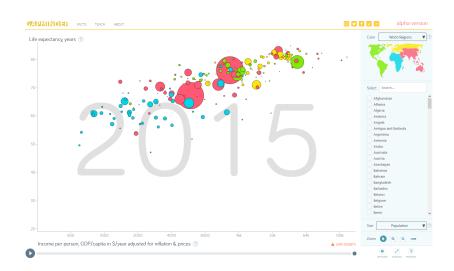
- two quantitative values
- horizontal and vertical spatial dimensions
- mark type = point



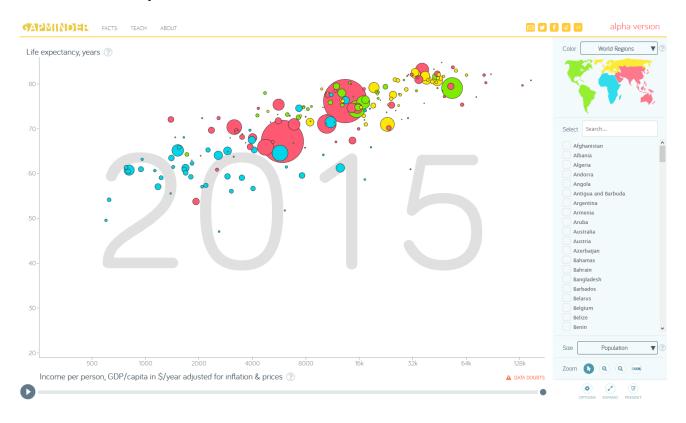
when marks are sized, the chart is often called a bubble chart or bubble plot

TASKS

- find trends
- find outliers
- show distribution
- show correlation
- locate clusters



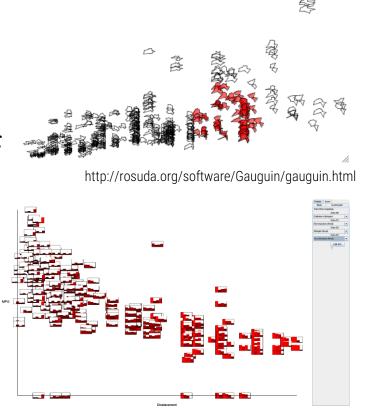
how many items are reasonable to put on a scatterplot?



GLYPHS

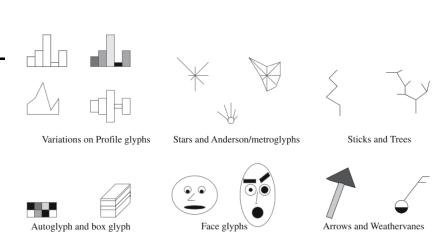
marks can be replaced with glyphs

are themselves composed of multiple marks



GLYPHS

- Small composite visual representations of multidimensional data points
- Characterized generally by lack of reference structures (grid lines, axes labels, ...)



EXAMPLE: CHERNOFF FACES

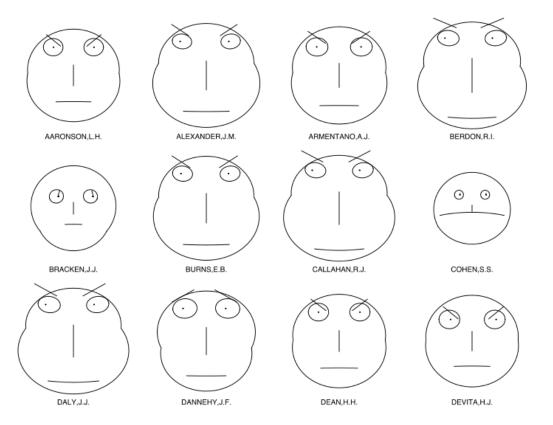
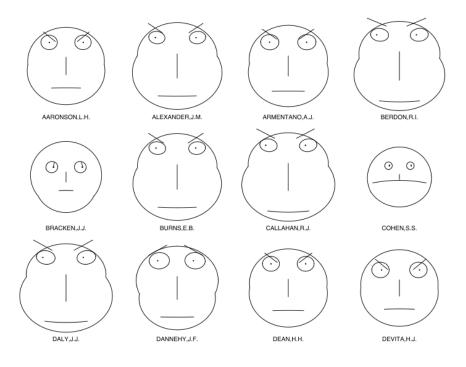


Image source: Wikipedia

Herman Chernoff, The Use of Faces to Represent Points in K-Dimensional Space Graphically, 1973.

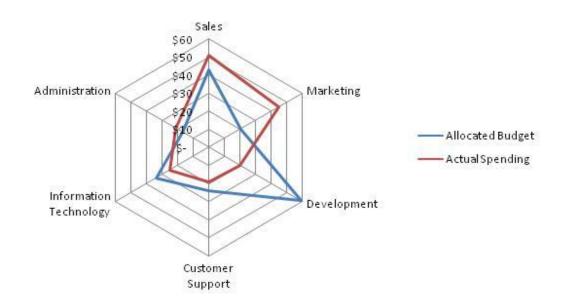
CHERNOFF FACES

- features of a human face encode data values (e.g. slant of eye brows, size of eyes, ...)
- reasoning: humans are good at differentiating faces and reading face features
- problem: chernoff faces have generally been found not to be very effective

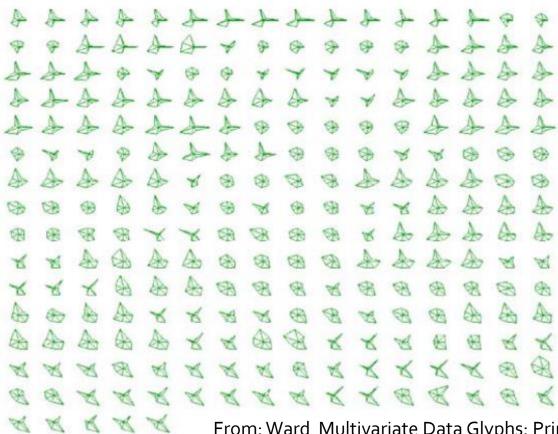


EXAMPLE: STAR GLYPHS

- Lay out dimension in radial fashion
- Draw each point as a ring



STAR GLYPHS



From: Ward Multivariate Data Glyphs: Principles and Practice. Handbook of Data Visualization (2008)

SHOW CATEGORICAL REGIONS

Separate, Order, and Align

CATEGORICAL

- spatial position is an ordered magnitude visual channel
- categorical attributes are unordered identities (no magnitude)
- cannot be encoded with spatial position
- BUT: can be expressed with a spatial region

REGIONS

- contiguous bounded areas
- distinct from one another
- need to be separated, ordered, and aligned

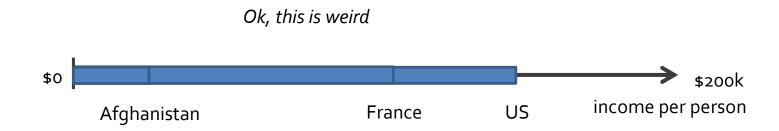
LIST ALIGNMENT

ONE KEY

LIST ALIGNMENT

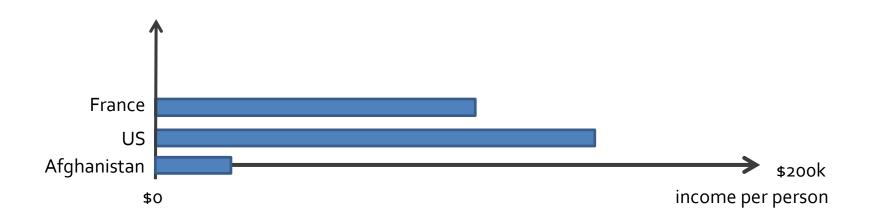
separate into regions by key

E.g. length + rectangle



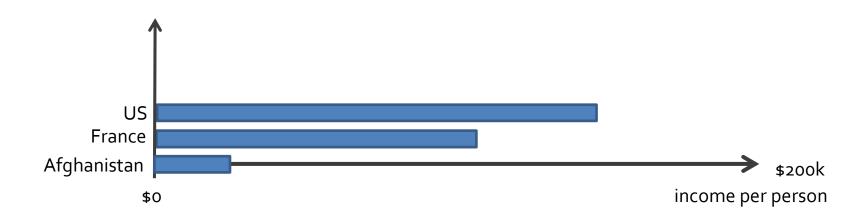
ALIGN

align regions of key categorical values along one axis in a common frame



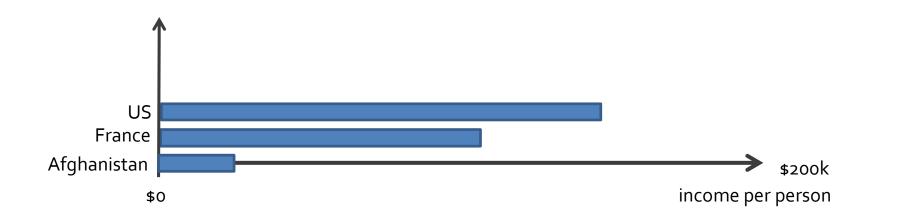
ORDER

- using a derived attribute such as alphabet
- and/or using dependent data values

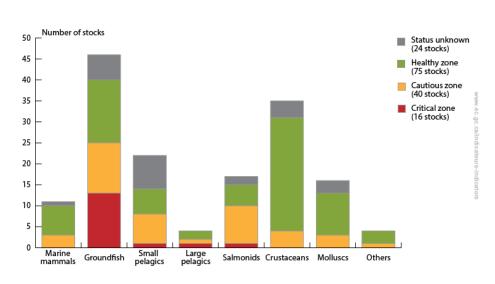


BAR CHARTS

DATA	one quantitative value attribute, one categorical key attribute
ENCODE	line marks, express value attribute with aligned vertical position (length), separate key attribute with horizontal position
TASK	lookup and compare values
SCALE	key attribute: dozens to hundreds of levels



ALTERNATIVE

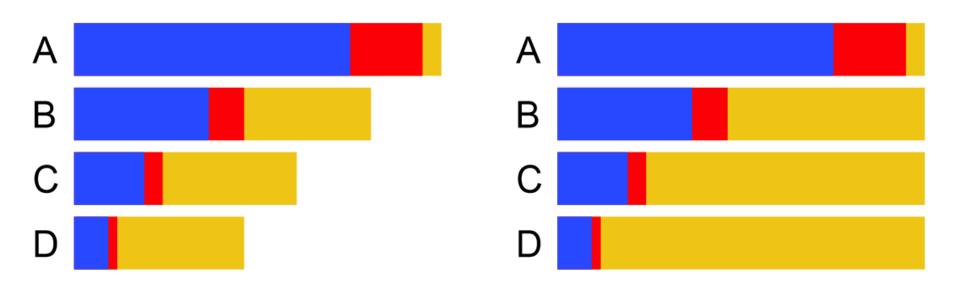


https://www.ec.gc.ca/indicateurs-indicators/default.asp?lang=en&n=1BCD421B-1

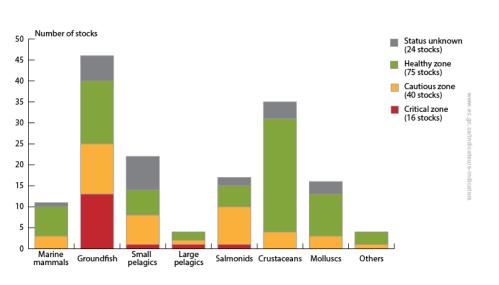
Stacked bar chart

- each bar is a composite glyph
- each bar part encodes a value
- composite glyphs arranged as a list according to primary key
- color used to distinguish secondary key
- typically used for absolute values (use a normalized stacked bar for proportions)

STACKED BARS VS. NORMALIZED STACKED BARS



STACKED BARS



ADVANTAGE

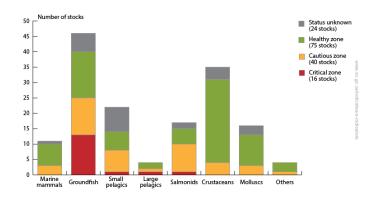
 can compare totals and lowest level well

DISADVANTAGE

 upper levels of secondary key require comparison against non-aligned scale

STACKED BARS

DATA	MD table; one quantitative value attribute, two categorical key attributes
ENCODE	bar glyph: length-encoded subcomponents for each level of secondary key attribute separate bars by category of primary key
TASK	part-to-whole relationship, lookup values, find trends
SCALE	key attribute (main axis): dozens to hundreds of levels key attribute (stacked glyph axis): several to one dozen



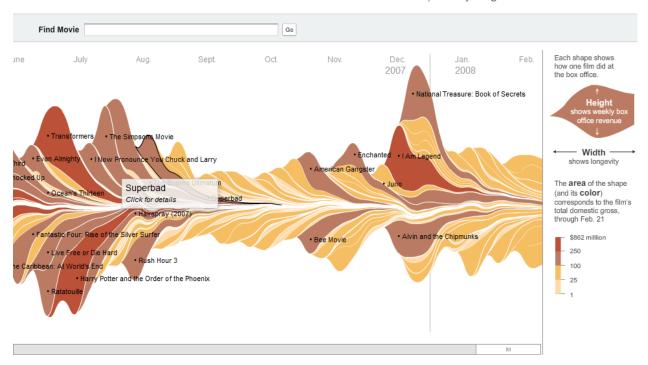
STREAMGRAPH

February 23, 2008

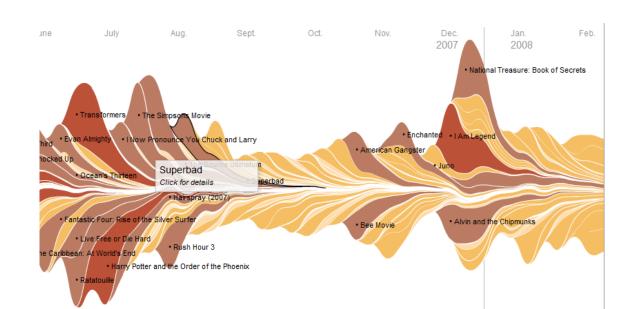
SIGN IN TO E-MAIL OR SAVE THIS FEEDBACK

The Ebb and Flow of Movies: Box Office Receipts 1986 - 2008

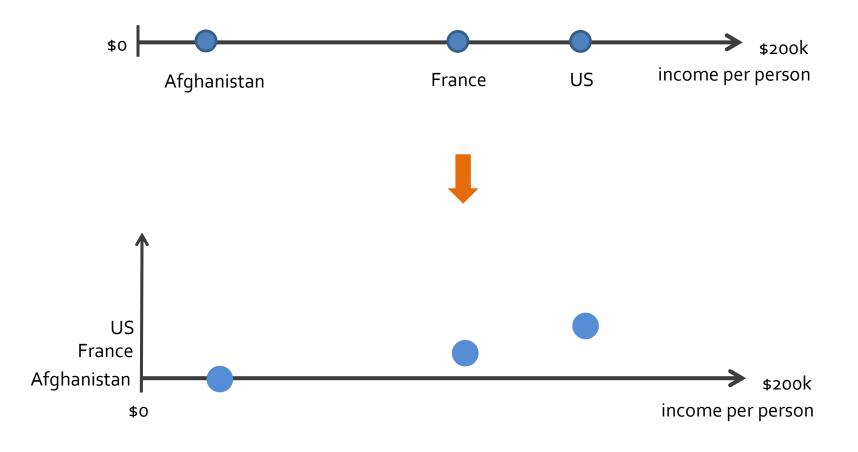
Summer blockbusters and holiday hits make up the bulk of box office revenue each year, while contenders for the Oscars tend to attract smaller audiences that build over time. Here's a look at how movies have fared at the box office, after adjusting for inflation.



DATA	MD table; one quantitative value attribute (e.g. counts), one ordered key attribute (e.g. time), one categorical key attribute (e.g. film)
DERIVE	order of layers is derived from a quantitative attribute
ENCODE	use derived geometry to show layers across time, layer height encodes count
SCALE	key attributes (time, main axis): hundreds of time points key attributes (short axis): dozens to hundreds

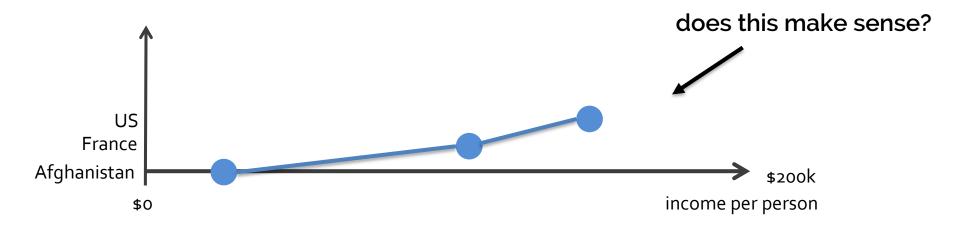


DOT CHART/PLOT

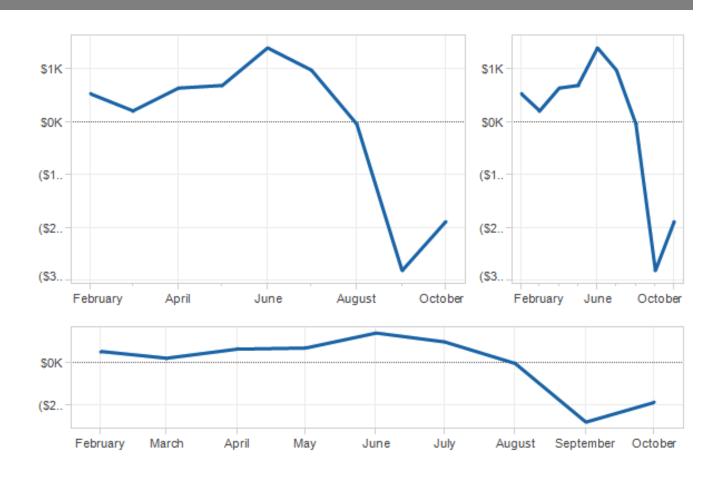


LINE CHART

augment with line connection marks emphasize the ordering and show trends should not be used with categorical keys

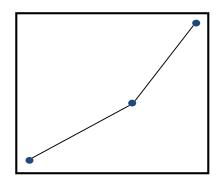


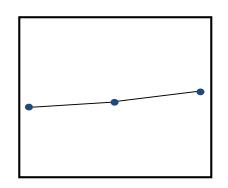
ASPECT RATIO SELECTION

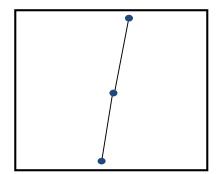


[Cleveland]

TO FACILITATE PERCEPTION OF TRENDS,
MAXIMIZE THE DISCRIMINABILITY OF LINE
SEGMENT ORIENTATIONS

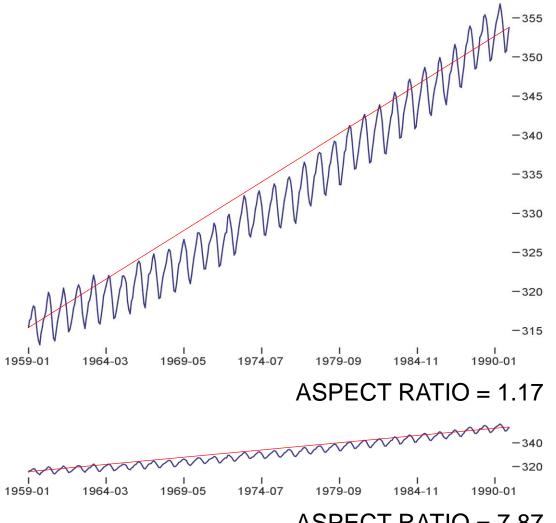






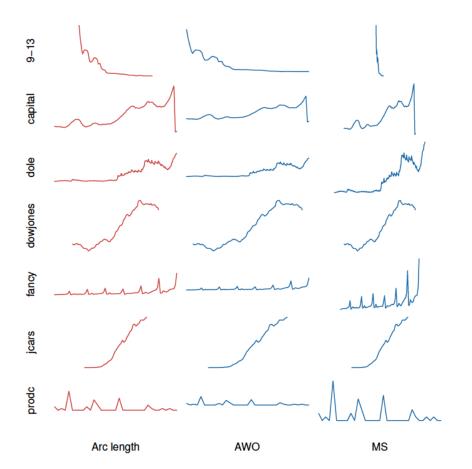
TWO SEGMENTS ARE MAXIMALLY DISCRIMINABLE WHEN THEIR AVG ABSOLUTE ANGLE IS 45°

OPTIMIZE THE ASPECT RATIO TO BANK TO 45°



ASPECT RATIO = 7.87

ALTERNATIVE METHODS



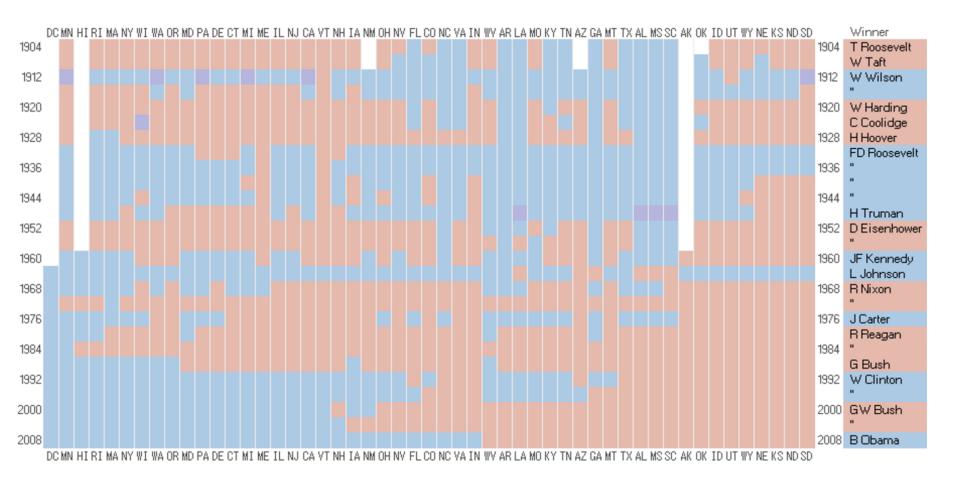
Practical advice:

CHOOSE AN ASPECT RATIO THAT EMPHASIZES THE IMPORTANT DETAILS FOR YOUR TASK

[TALBOT ET AL, 2011]

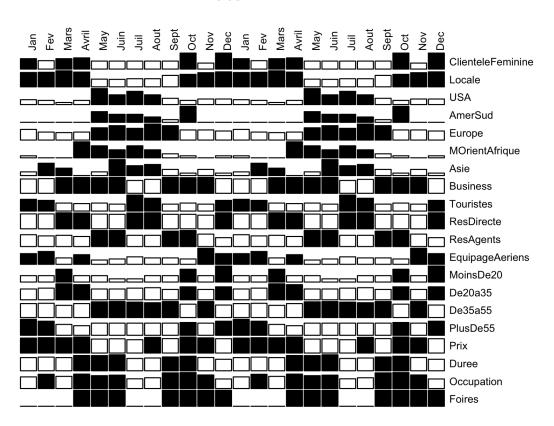
MATRIX ALIGNMENT

Two keys

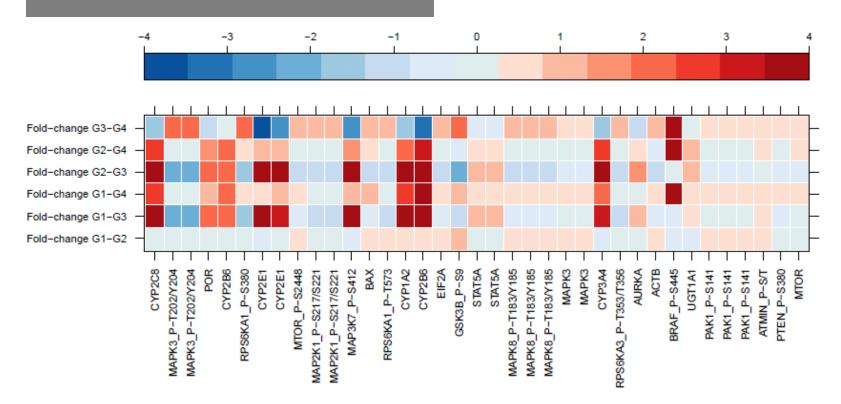


HEATMAP

Hotel 2

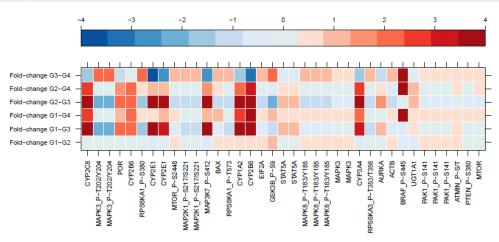


HEATMAP

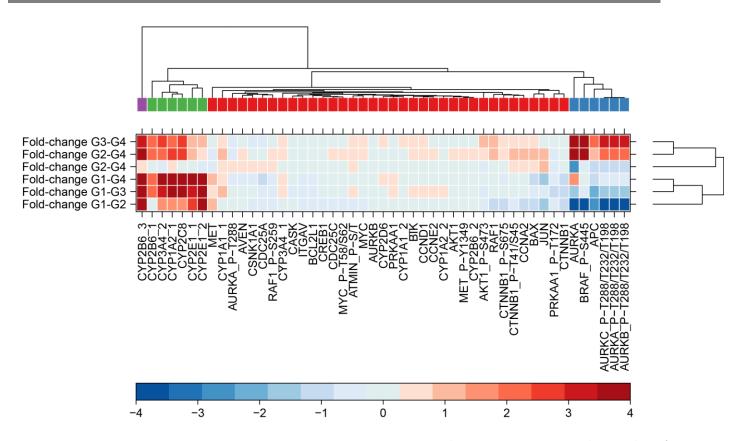


HEATMAP

DATA	Table; two categorical key attributes, one quantitative value attribute
ENCODE	2D matrix alignment of area marks, e.g. with diverging color map
TASK	find clusters, outliers; summarize
SCALE	items: ~1 million (on 1000x1000px), categorical attribute levels: hundreds, quantitative attribute levels: 3-11



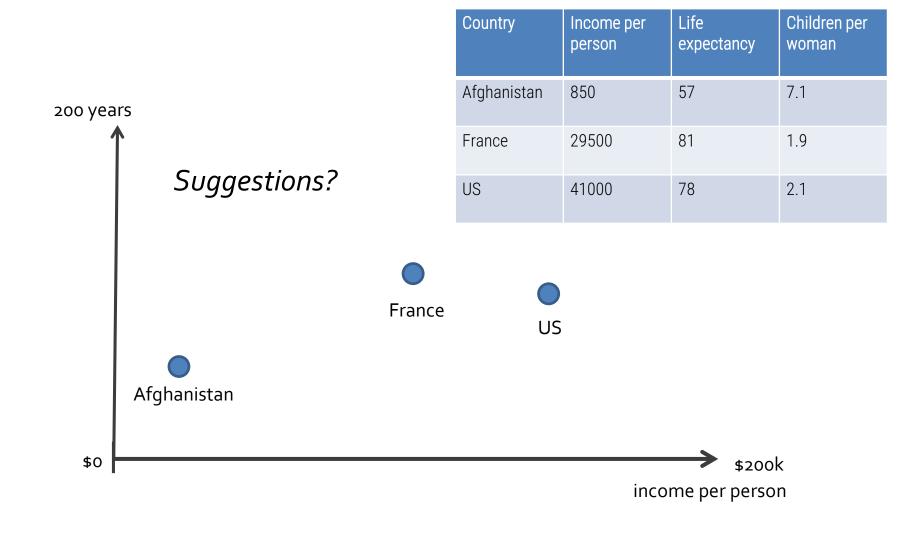
CLUSTERED HEATMAP



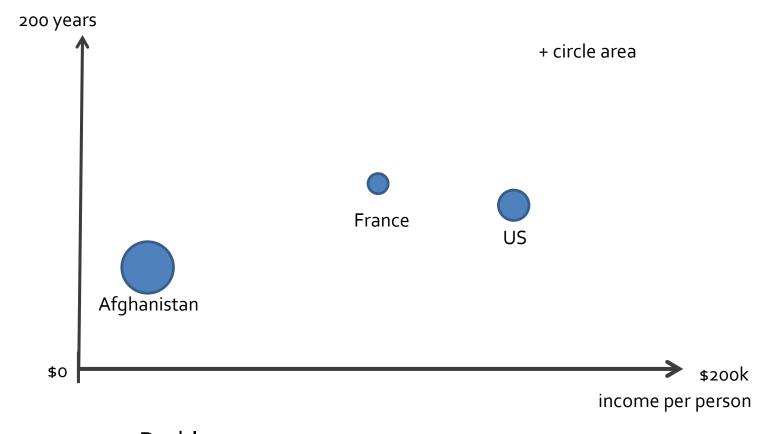
BACK TO OUR ORIGINAL EXAMPLE

Country	Income per person	Life expectancy	Children per woman
Afghanistan	850	57	7.1
France	29500	81	1.9
US	41000	78	2.1

now with 4 attributes



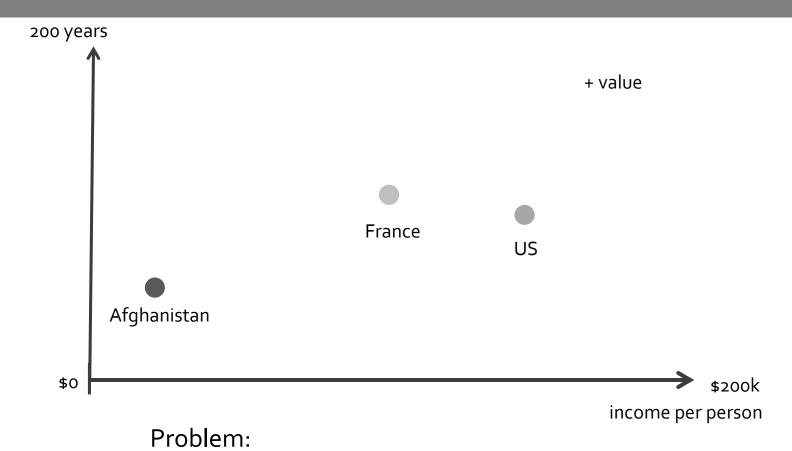
ADD ANOTHER VISUAL ENCODING



Problem:

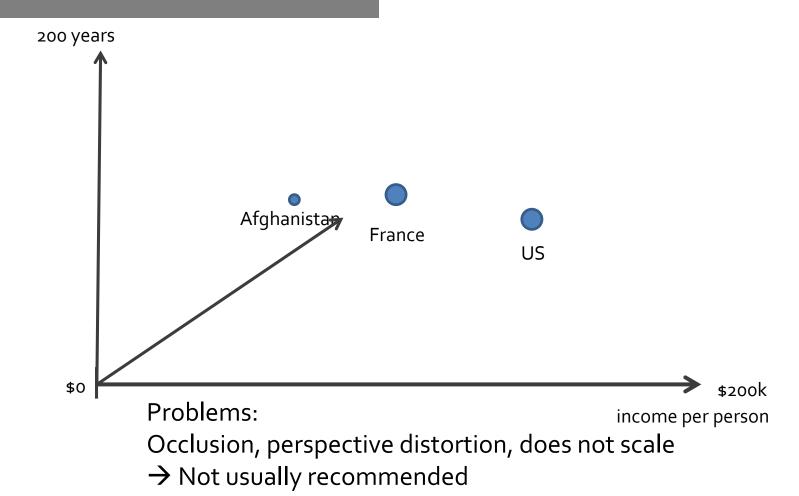
Does not scale well to more attributes

ADD ANOTHER VISUAL ENCODING

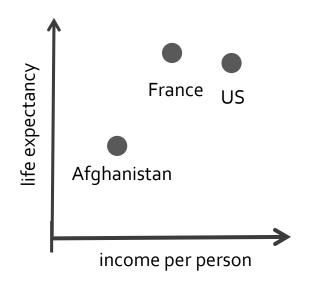


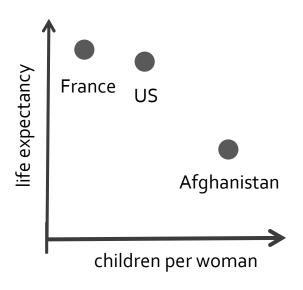
Does not scale well to more attributes

ADD AN AXIS



ADD AN AXIS





SCATTERPLOT MATRIX

This idea scales relatively well

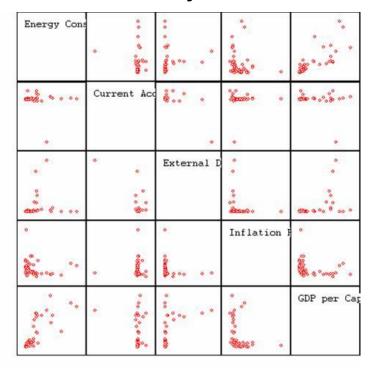


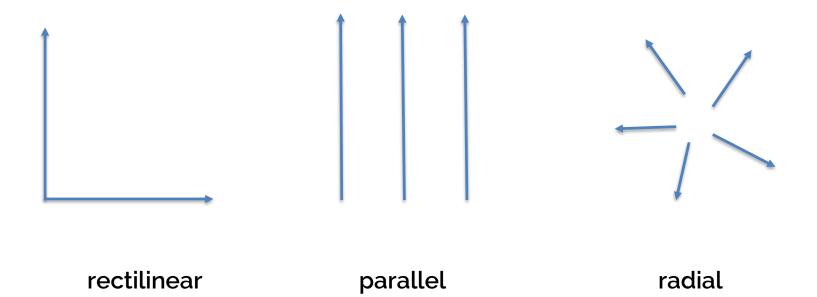
Image Source: Wikipedia

SCATTERPLOT MATRIX

movie IMDB ID		Actor	Actor	Directo	Writer	Writer	rodude	rodude	roduc	mpos	B udjet	Genre	Genre	Genre	Genre
tt1430132 Load	1	Hugh Jackman	Will Yun	James Mangold	Mark Bomback	Scott Frank	Hugh Jackman	Stan Lee	Hutch Parker	Marco Beltrami	120000000	Action	Adventure	Fantasy	Sci-Fi
The Wolverine		20	6	6	6	8	2	27	1	40	238	779	563	366	350
2013 - 2 h 6 min Actors Hugh Jackman (20)	Actor Hugh Jackman	20	0	1	1	0	2	5	0	0	10	9	10	4	8
Will Yun Lee (6) Tao Okamoto (0)	Actor Will Yun 6	0	6	0	1	0	0	2	0	0	3	6	3	2	1
Rila Fukushima (0) Directors James Mangold (6) Writers	Directo James Mangold 6	r =	0	6	0	0	0	0	0	1	1	2	0	1	0
Mark Bomback (6) Scott Frank (8) Genres	Writer Mark Bomback 6	1	_	0	6	0	1	0	0	1	3	4	2	1	3
Action (779) Adventure (563) Fantasy (366)	Writer	0	0	0	0	8	0	0	0	1	1	3	1	0	1
Sci-Fi (350) Budjets 120000000 (238)	roduce Hugh Jackman	7	•	0	T	0	2	1	0	0	1	1	1	1	1
Producers Hugh Jackman (2) Tom Cohen (0)	Stan Lee	9	ี	0	0	0		27	0	1	18	27	17	16	18
Stan Lee (27) Hutch Parker (1) Costume_Designers Composers	roduce Hutch Parker	0	•	0	0	0	•	0	1	0	0	1	0	0	1
Marco Beltrami (40) Cinematographers	Marco Beltrami 40	er •	•	=	T	=	0	T	0	40	3	14	4	4	11
Additional Informations Composer	Budjet 120000000 238	01	e —		 3	 		81	0	e	238	158	165	92	73
Marco Beltrami Add	Genre	6	9	ผ	4	es ===		27	1	41	158	779	312	140	226
	Genre Adventure 563	10	3	0	2	1		17	0	4	165	312	563	184	156
	Genre Fantasy 366	4	<u>ч</u>	_	1	0	_	91	0	4	92	140	184	366	63
	Genre Sci-Fi 350	8	-	0	3			18	1 —	=	73	226	156	63	350

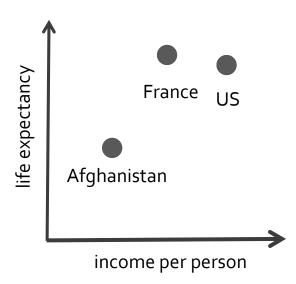
SPATIAL AXIS ORIENTATION

An additional design choice

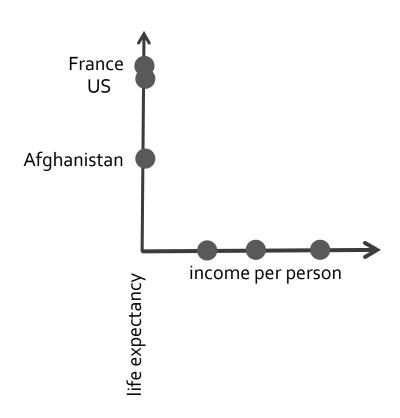


parallel coordinates

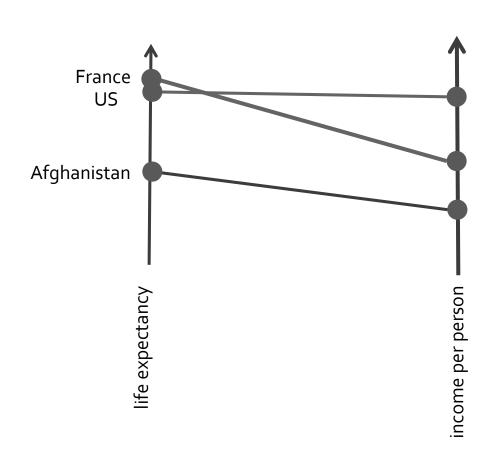
Back to our original example



Parallel Coordinates



parallel coordinates



 show correlations between neighboring axes

MULTIDIMENSIONAL DETECTIVE

Alfred Inselberg*, Multidimensional Graphs Ltd†
&
Computer Science Department
Tel Aviv University, Israel
aiisreal@math.tau.ac.il

Abstract

The display of multivariate datasets in parallel coordinates, transforms the search for relations among the variables into a 2-D pattern recognition problem. This is the basis for the application to Visual Data Mining. The Knowledge Discovery process together with some general guidelines are illustrated on a dataset from the production of a VLSI chip. The special strength of parallel coordinates is in modeling relations. As an example, a simplified Economic Model is constructed with data from various economic sectors of a real country. The visual model shows the interelationship and dependencies between the sectors, circumstances where there is competition for the same resource, and feasible economic policies. Interactively, the model can be used to do trade-off analyses, discover sensitivities, do approximate optimization, monitor (as in a Process) and Decision Support.

Introduction

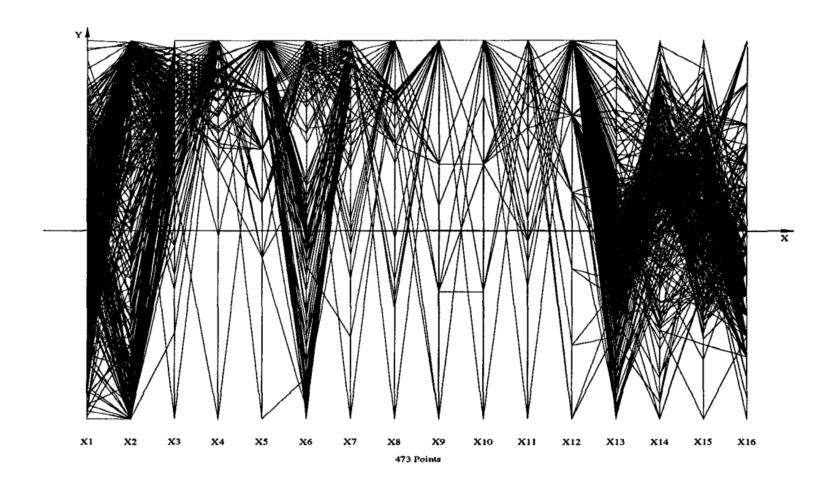
In Geometry parallelism, which does not require a notion of angle, rather than orthogonality is the more fundamental concept. This, together with the fact that orthogonality "uses-up" the plane very

fast, was the inspiration in 1959 for "Parallel" Coordinates. The systematic development began in 1977 [4]. The goals of the program were and still are (see [6] and [5] for short reviews) the visualization of multivariate/multidimensional problems without loss of information and having the properties:

- 1. Low representational complexity. Since the number of axes, N equals the number of dimensions (variables) the complexity is O(N),
- Works for any N,
- Every variable is treated uniformly (unlike "Chernoff Faces" and various types of "glyphs"),
- The displayed object can be recognized under projective transformations (i.e. rotation, translation, scaling, perspective),
- The display easily/intuitively conveys information on the properties of the Ndimensional object it represents,
- The methodology is based on rigorous mathematical and algorithmic results.

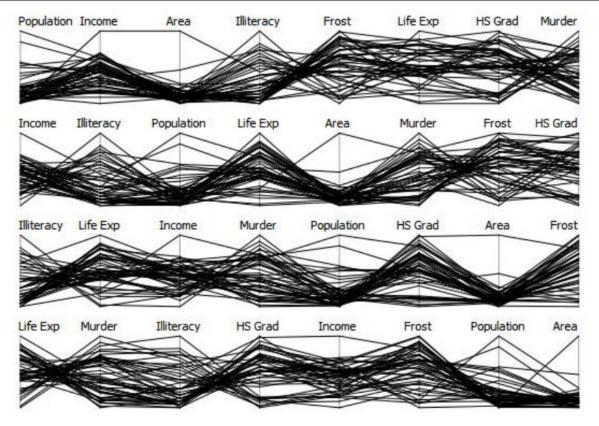
Parallel coordinates (abbr.||-coords) transform multivariate relations into 2-D patterns, a property that is well suited for Visual Data Mining.

^{*}Senior Fellow San Diego SuperComputing Center †36A Yehuda Halevy Street, Raanana 43556, Israel



Original Example from Inselberg 1997

THE ORDER OF AXES MATTERS



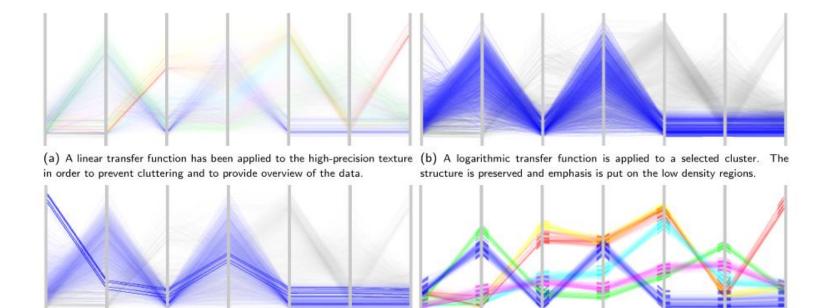
Eurographics 2013, STAR Report J. Heinrich, D. Weiskopf

REDUCE CLUTTER - HIGHLIGHT CLUSTERS

Lots of work on this. For example:

(c) Local cluster outliers are enhanced. A square root transfer function is

used and the outliers are visible even through high-density regions.



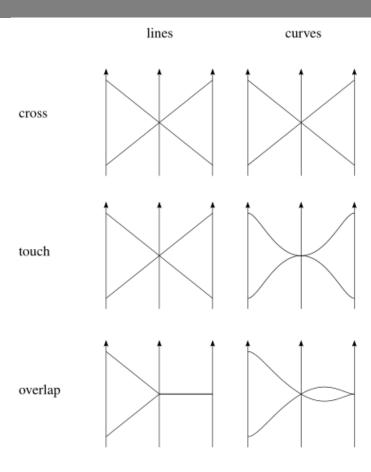
Revealing Structure within Clustered Parallel Coordinates Displays, InfoVis 2005

(d) A complementary view of the clusters with uniform bands. 'Feature

animation' presents statistics about the clusters and acts as a guidance.

HOW TO DRAW THE LINES

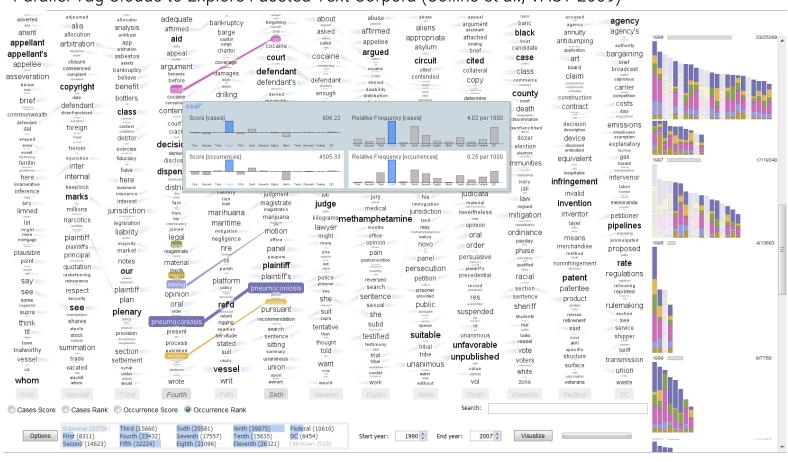
Goal: avoid ambiguity



Eurographics 2013, STAR Report J. Heinrich, D. Weiskopf

COMBINE WITH OTHER VISUALIZATION TECHNIQUES

Parallel Tag Clouds to Explore Faceted Text Corpora (Collins et al., VAST 2009)



THERE IS MUCH MORE ON THIS...

Start here if you want more information

EUROGRAPHICS 2013/ M. Sbert, L. Szirmay-Kalos

STAR - State of The Art Report

State of the Art of Parallel Coordinates

J. Heinrich and D. Weiskopf

Visualization Research Center, University of Stuttgart

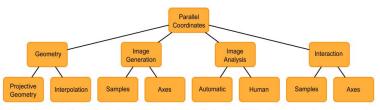


Figure 1: Taxonomy of topics for parallel coordinates in the scientific literature. The first-level nodes each represent a section in this paper, where the scope and definition of each topic will be explained.

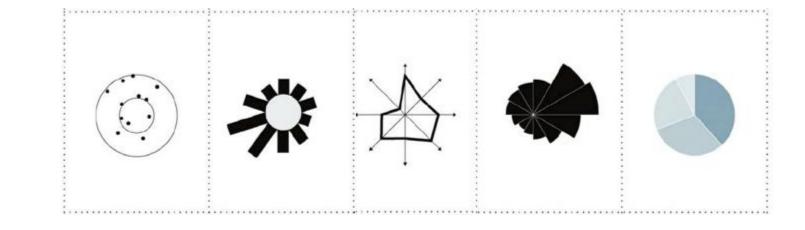
Abstract

This work presents a survey of the current state of the art of visualization techniques for parallel coordinates. It covers geometric models for constructing parallel coordinates and reviews methods for creating and understanding visual representations of parallel coordinates. The classification of these methods is based on a taxonomy that was established from the literature and is aimed at guiding researchers to find existing techniques and identifying white spots that require further research. The techniques covered in this survey are further related to an established taxonomy of knowledge-discovery tasks to support users of parallel coordinates in choosing a technique for their problem at hand. Finally, we discuss the challenges in constructing and understanding parallel-coordinates plots and provide some examples from different application domains.

Categories and Subject Descriptors (according to ACM CCS): 1.3.3 [Computer Graphics]: Picture/Image Generation—Line and curve generation

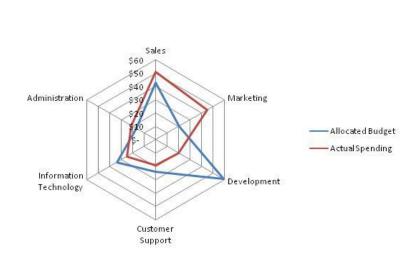
RADIAL AXES

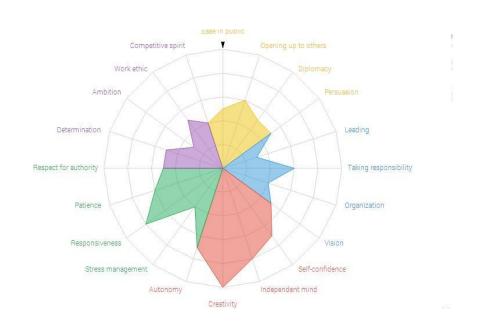
Polar



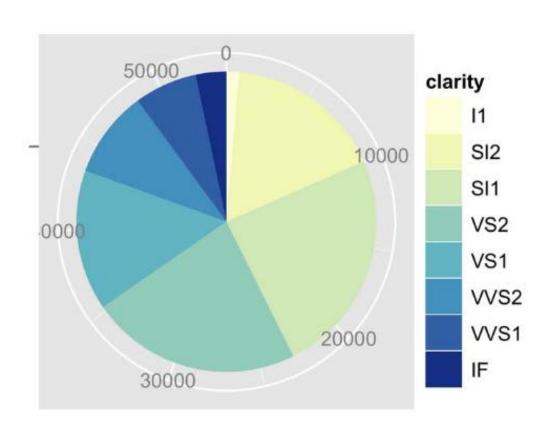
EXAMPLE: STAR PLOT

• = radial line chart

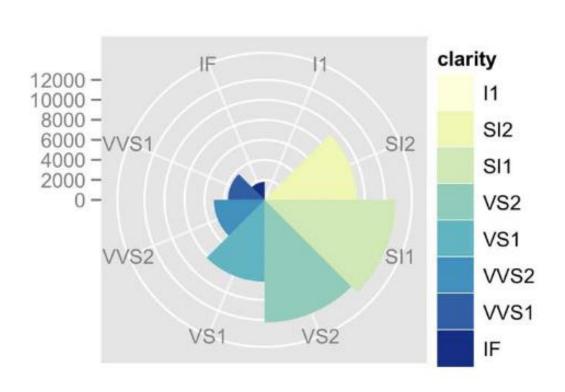




PIE CHARTS



POLAR AREA CHARTS



SPATIAL LAYOUT DENSITY

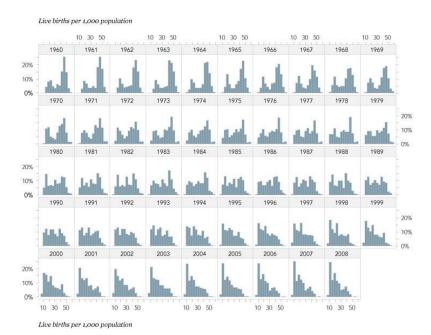
DATA DENSITY

MAXIMIZE THE RATIO OF:

(NUMBER OF ENTRIES IN DATA) (AREA OF THE GRAPHIC)

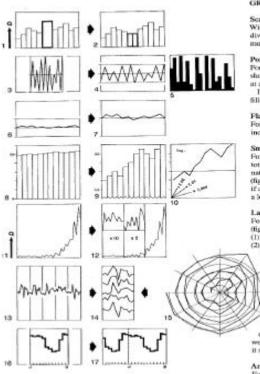
DATA DENSITY – SHRINK THE GRAPHICS

Annual Worldwide Distributions of Live Births



"SMALL MULTIPLES"

DATA DENSITY - SHRINK THE



GRAPHIC PROBLEMS POSED BY TIME SERIES

Scale in years

With a scale in years, a two-year total (figure 1) should be divided by 2 (figure 2). A total for six months should be multiplied by 2.

Pointed curves

For overly pointed curves (figure 3), the scale of the Q should be reduced; optimum angular perceptibility occurs at acoust 20 degrees (figure 4).

If the curve is not reducible (large and small variations), filled columns can be used (figure 5).

Flat curves

For overly flat curves (figure 6), the scale of the Q should be increased (figure 7).

Small variations

For small variations in relation to the total (figure 8), the total loses its importance, and the zero point can be eliminated, provided the reader is made aware of this elimination (figure 9). The graphic can be interpreted as an acceleration if a precise study of the variations is necessary, here, we use a logarithmic scale (figure 10). (See also page 240)

Large range

For a very large range between the extreme numbers (figure 11), we must either:

- (1) leave out the smallest variations;
- (2) be concerned only with relative differences (logarithmic scale), without knowing the absolute quantities;
 - (3) select different parts (periods) within the ordered component and treat them on different scales above the common scale (figure 12).

Obvious periodicity

If there is obvious periodicity (figure 13), and the study involves a comparison of the phases of each cycle, it is preferable to break up the cycles in order to superimpose them (figure 14). A point construction can be used, preferably in a spiral shape (figure 15), but we should not begin with too small a circle. As striking as it seems, it is less efficient than an orthogonal construction.

Annual curves

For annual curves of rainfall or temperature, if a cycle has two phases (figure 17), why depict only one (figure 16)?

contrast.

Unlike what we see in figure 18, the pertinent or "sees" information must be separated from the background or reference" information. The background involves (a) the isystem, highlighted by a heading (Post St. Michel); (b) the highly visible identification of each component (tomings and dates). The new information (the curve) must stand out from the background (figure 19).

Reference points

it is impossible to utilize a graphic such as figure 20, except is a general manner. There is confusion concerning the position of the points, and no potential comparison is possible, as it is in figure 21.

Precision reading

A precision reading (utilization on the elementary level, as in figure 24) is difficult in figure 22, which results in a point reading of the order of the points, and in figure 23, where there is ambiguity concerning the position of the points. On the other hand, figure 22 does favor overall vision (correlation).

Null boxe

Curves accommodate rull boxes poorly (figure 25). Columns (figure 26) are preferable.

Unknown boxes

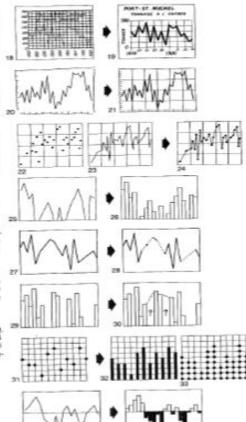
The drawing must indicate the unknowns of the information in an unambiguous way (figures 28 and 30). The reader might interpret figure 27 as a change in the structure of the curve and figure 29 as involving mill values.

Very small quantities

Except in seeking a correlation (quite improbable here) the number of ships entering into a port is represented better by figure 33 than by figure 31 or 32. The reader can perceive the numerical values at first glance.

Positive-negative variation

This is in fact a problem involving three components O. Q. ≠ (+ -), and it must be visually treated as such. Figure 34 can be improved by utilizing a retiral variable (in figure 25 a value difference: black—adite) in differentiate the ≠ component and thus highlight positive-negative variation.



DATA DENSITY – SHRINK THE GRAPHICS

Placed in the relevant context, a single number gains meaning. Thus the most recent measurement of glucose should be compared with earlier measurements for the patient. This data-line shows the path of the last 80 readings of glucose:

Lacking a scale of measurement, this free-floating line is dequantified. At least we do know the value of the line's right-most data point, which corresponds to the most recent value of glucose, the number recorded at far right. Both representations of the most recent reading are tied together with a color accent:

Some useful context is provided by showing the *normal range* of glucose, here as a gray band. Compared to normal limits, readings above the band horizon are elevated, those below reduced:

SPARKLINES

Science fiction

From Wikipedia, the free encyclopedia

For other uses, see Science fiction (disambiguation).

33k visits in last 30 days

Science fiction is a genre of fiction dealing with imaginatic content such as futuristic settings, futuristic science and technology, space travel, time travel, parallel universes, and extraterrestrial life. It often explores the potential consequence

SPARKLINES

EASTERN EUROPE

Soviet cult and pragmatism in Transnistria

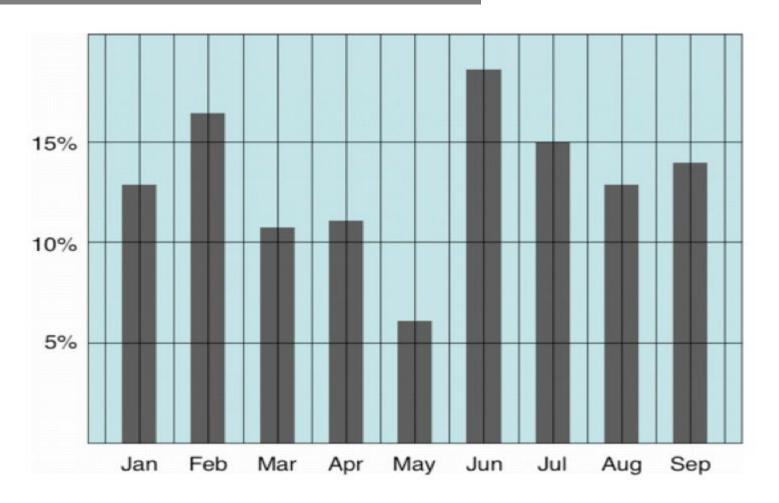
Experts worry that the next
"Crimea" could be the
breakaway region of Transnistria
Many locals there don't share that far,
and if the last referendum holds, a large
majority would welcome a Russian
annexation.

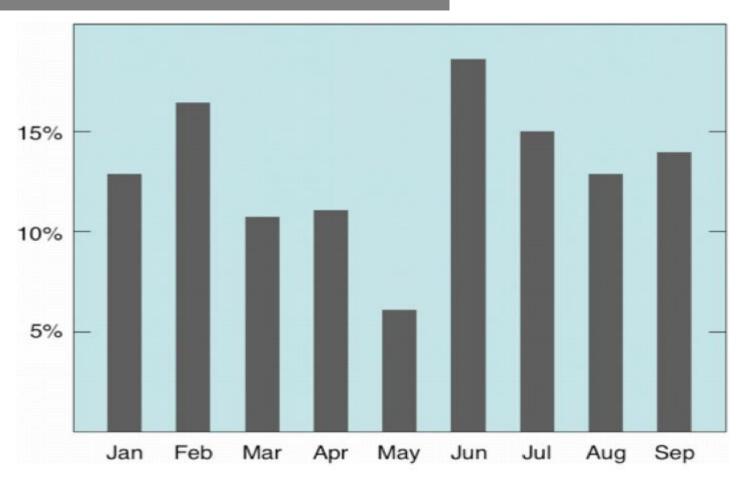
SPARKLINES

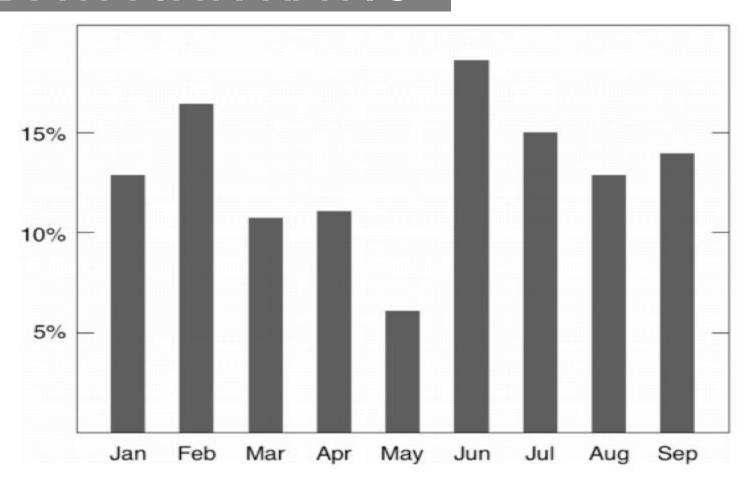
Gonzalo Higuain slides a cross in from the right and Ronaldo, at the front post, shoots off target.

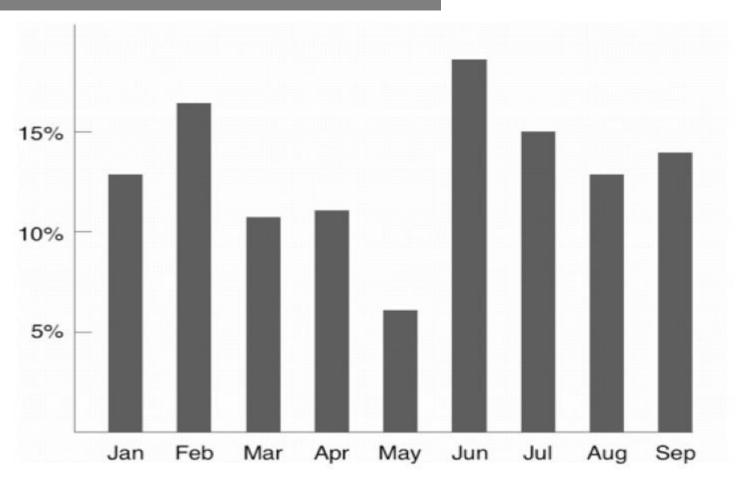
MAXIMIZE THE RATIO OF

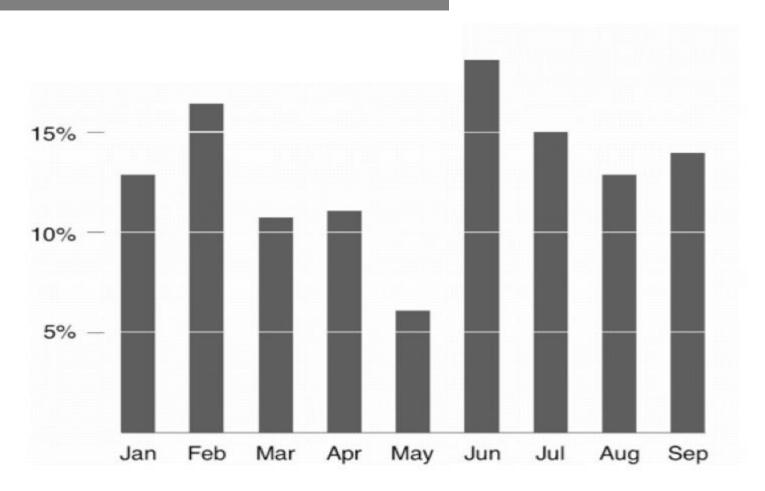
(INK USED TO SHOW DATA) (TOTAL INK USED)

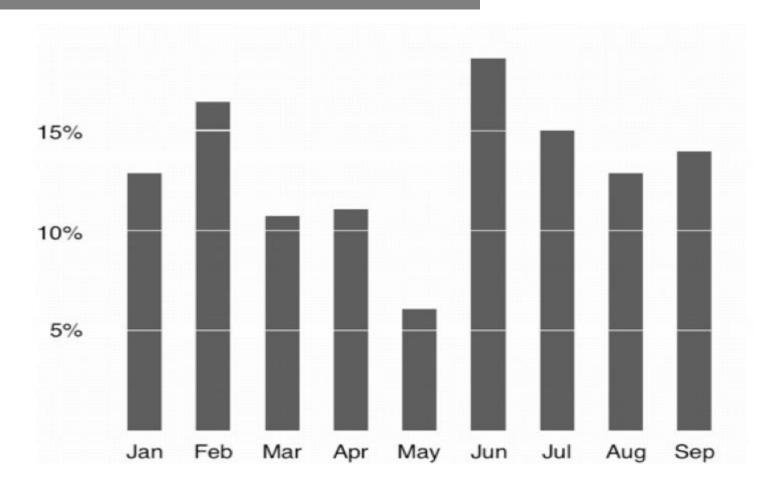






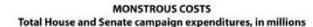


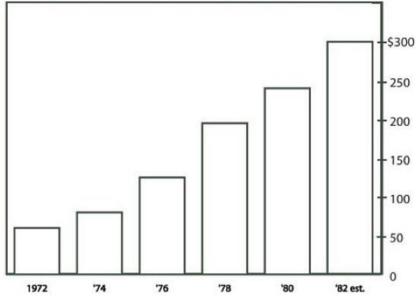




MINIMIZE CHART JUNK







Wayne Lytle

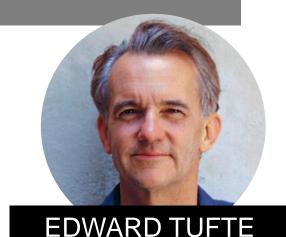
The Dangers of

GLITZIIVESS

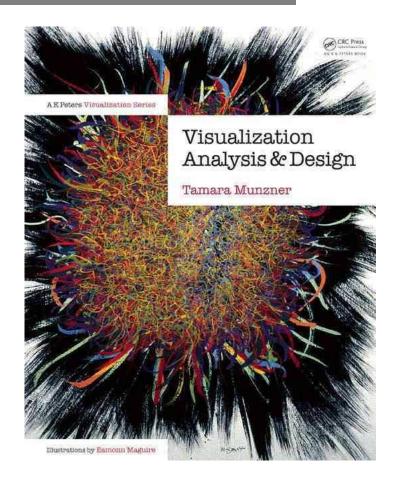
and other
Visualization Faux Pas

TUFTE'S INTEGRITY PRINCIPLES

- MAXIMIZE THE DATA-INK RATIO
- AVOID CHART JUNK (SOMETIMES)
- LAYER INFORMATION
- MAXIMIZE THE DATA DENSITY
 - SHRINK THE GRAPHICS
 - MAXIMIZE THE AMOUNT OF DATA SHOWN (SOMETIMES)



READINGS



ACKNOWLEDGEMENTS

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- Nicolai Marquardt (University College London)
- Uta Hinrichs (University of St. Andrews)
- Saul Greenberg (University of Calgary)