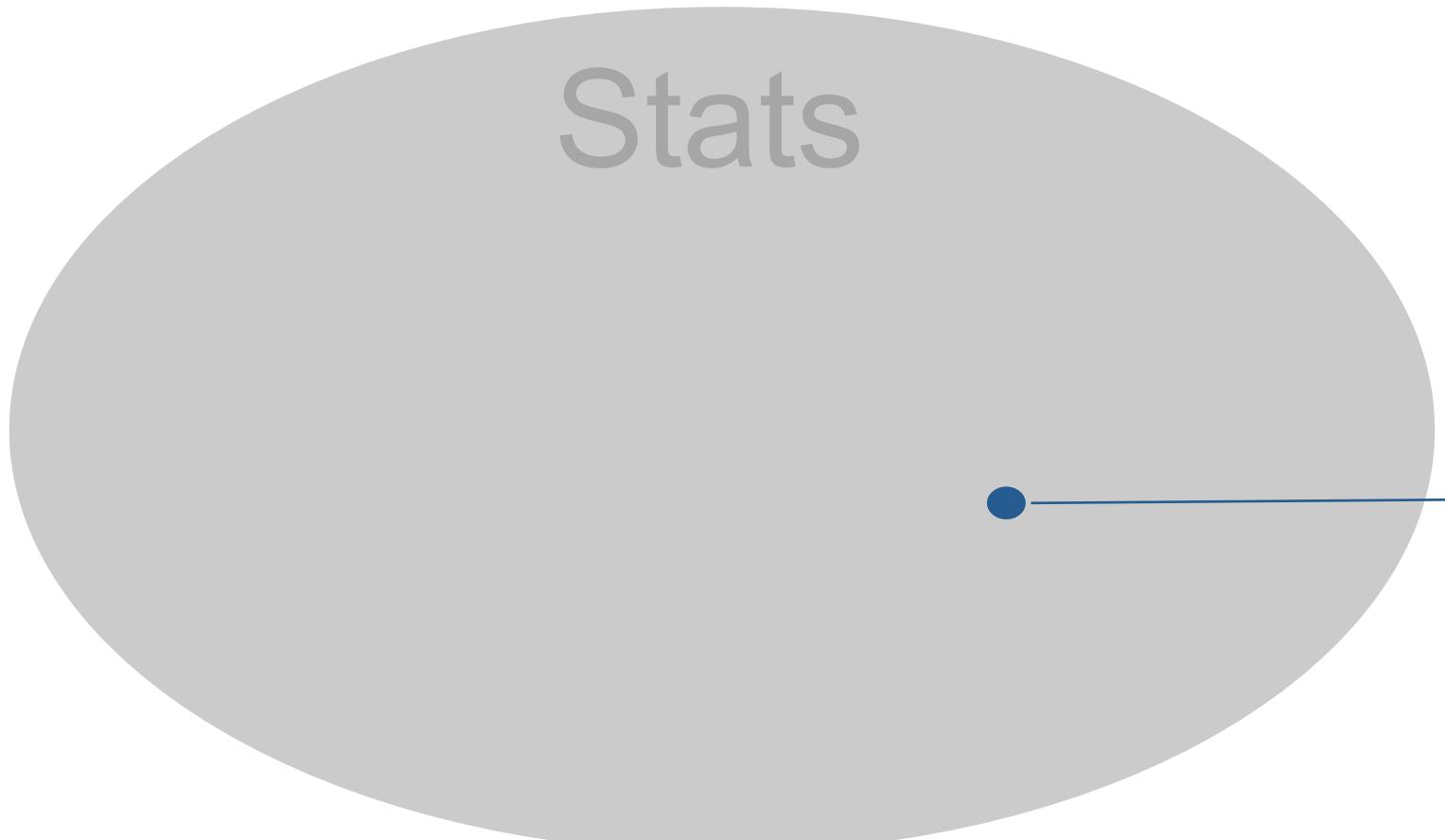


INTRODUCTION TO STATISTICS

LECTURE 4

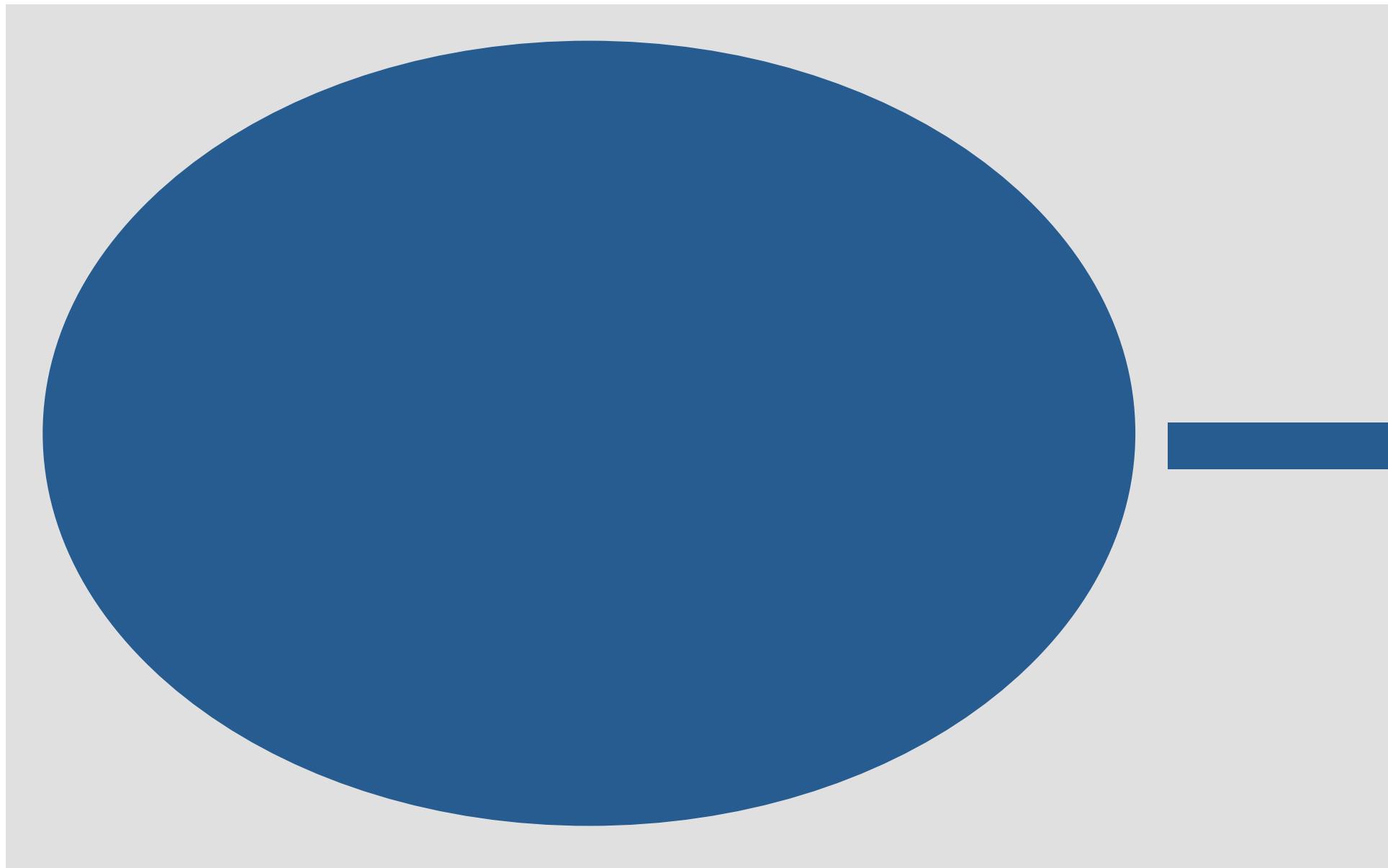
Pierre Dragicevic

WHAT YOU WILL LEARN



Stats

This class



STATISTICS

- **Statistics** is the study of the collection, analysis, interpretation, presentation and organization of data.

Dodge, Y. (2006) The Oxford Dictionary of Statistical Terms, OUP.

STATISTICS

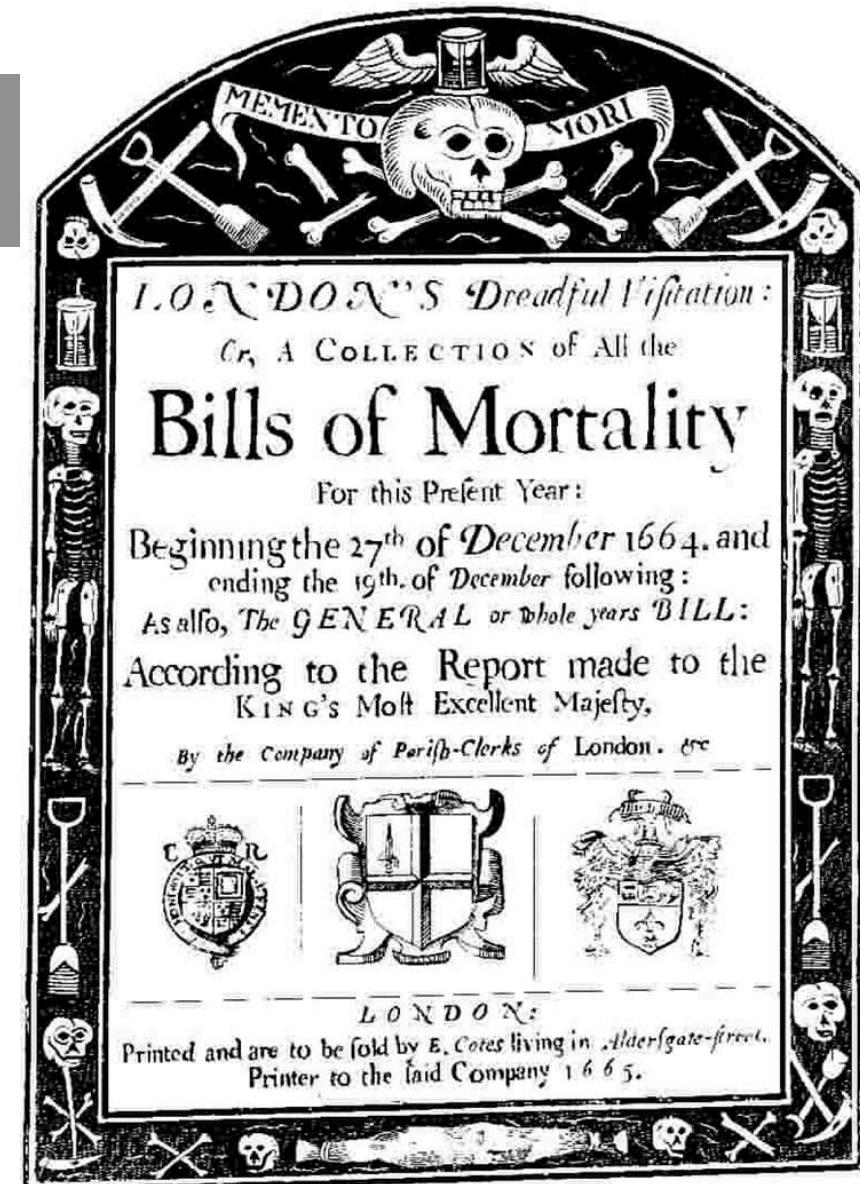
- 1750s German “*Statistik*”
“*analysis of data about the state*”
- Quickly adopted in England
(previously called “*political arithmetics*”)

STATISTICS

- John Graunt, 1662
Observations on the bills of mortality



CAPTAIN JOHN GRAUNT



THE TABLE OF CASUALTIES.

The Years of our Lord	In 20 Years.																		
	1647	1648	1649	1650	1651	1652	1653	1654	1655	1656	1657	1658	1659	1660	1629	1630	1631	1632	1633
Abortive, and stillborn	335	329	327	351	380	381	384	433	483	419	463	467	421	544	499	439	410	445	500
Aged	916	835	839	696	780	834	864	974	743	892	869	1176	909	1095	579	712	661	671	704
Ague, and Fever;	1260	884	751	970	1038	1212	1282	1371	689	875	999	1800	2303	2148	956	1091	1115	1108	953
Apoplexy, and sodainly	68	74	64	74	106	111	118	86	92	102	113	138	91	67	22	36	17	24	35
Bleach																			
Blaifed	4	1																	
Bleeding	3	2	5	1	3	4	3	2	7	3	5	4	7	2	5	2	5	4	3
Bloody Flux, Scouring, and Flux	155	176	802	289	833	762	200	386	168	368	362	233	346	251	449	438	352	348	278
Burnt, and Scalded	3	6	10	5	11	8	5	7	10	5	7	4	6	6	3	10	7	5	1
Calenture	1																		
Cancer, Gangrene, and Fistula	26	29	31	19	31	53	36	37	73	31	24	35	63	52	20	14	23	18	27
Wolf																			
Canker, Sore-mouth, and Thrush	66	28	54	42	68	58	53	72	44	81	19	27	73	68	6	4	4	1	
Childbed	161	106	114	117	206	213	158	192	177	201	236	225	226	194	150	157	112	171	132
Christomes, and Infans	1369	1254	1065	990	1237	1280	1050	1343	1089	1393	1162	1144	858	1123	2590	2378	2035	2208	2130
Colick, and Wind	103	71	85	82	76	102	81	101	85	120	113	179	116	167	48	57			
Cold, and Cough																			
Consumption, and Cough	2423	2200	2388	1988	2350	2410	2216	2868	2606	3184	2757	3610	2982	3414	1827	1910	1713	1797	1754
Convulsion	684	491	510	493	569	653	666	818	702	1027	807	841	742	1031	52	87	18	2.1	221
Cramp																			
Cut of the Stone	2	1	3																
Drophy, and Tympiny	185	434	421	508	444	550	617	704	660	706	631	931	646	872	235	252	279	250	266
Drowned	47	40	30	27	49	50	3	30	43	4%	63	60	57	48	43	33	29	34	37
Excessive drinking																			
Executed	8	17	29	43	24	12	19	21	19	22	20	18	7	18	19	13	12	18	13
Fainted in a Bath																			
Falling-Sicknes	3	2	2	3		3	4	1	4	3	1	4	5	3	10	7	7	2	5
Fox, and small pox	139	400	1150	184	525	1272	139	812	1294	823	835	409	1523	354	72	40	58	531	72
Found dead in the Streets	6	6	9	8	7	9	14	4	3	4	9	11	2	6	18	33	20	6	13
French-Pox	18	29	15	18	21	20	20	20	29	23	25	53	51	31	17	12	12	12	17
Frighted	4	4	1																
Gout	9	5	11	9	7	7	5	6	8	7	8	13	14	2	2	5	3	4	5
Grief	12	13	16	7	17	14	11	17	10	13	10	12	13	4	18	20	22	11	17
Hanged, and made away themselves	11	10	13	14	9	14	11	9	14	16	24	18	11	36	8	8	6	15	3
Jaundice																			
Jaw-salf-	57	35	39	49	41	43	57	71	61	41	46	77	102	76	47	59	35	43	35
Impoistume																			
Itch	75	61	65	59	80	105	79	90	92	122	80	134	105	90	58	76	73	74	50
Killed by several Accidents	27	57	39	94	47	45	57	58	52	43	52	47	55	47	54	55	47	51	60
King's Evil	27	26	22	19	22	20	26	26	27	24	23	28	28	54	16	23	18	38	35
Lethargy	3	4	2	4	4	4	3	10	9	4	6	2	6	4	2	2	3	2	2
Leprosy																			
Livergrown, Spleen, and Rickets	53	46	56	59	65	72	67	65	52	50	38	51	8	15	94	112	99	87	82
Munitione	12	18	6	11	~	11	6	12	6	7	13	5	14	0	11	6	51	4	2

Cancer, Gangrene, and Fistula	26	29	31	19	31	53	16	37	73	31
Wolf				8						
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Colick, and Wind	103	71	85	82	76	102	8	101	85	120
Cold, and Cough							41	36	21	58
Consumption, and Cough	2423	2200	2388	1988	2350	2410	2216	2868	2606	3184 2
Convulsion				493	569	653	666	828	702	1027
Cramp										
Cut of the Stone		2	1	3		1	1	2	4	1
Dropfy, and Tympiny	185	434	421	508	444	556	617	704	660	706
Drowned	47	40	30	27	49	50	3	30	43	4
Excessive drinking			2							
Executed	8	17	29	43	24	12	19	21	19	22
Fainted in a Bath					1					
Falling-Sickness	3	2	2	3		3	4	1	4	3
Flow, and small Pox	139	400	1190	184	535	1272	139	812	1294	823
Found dead in the Streets	6	6	9	8	7	9	14	4	3	4
French-Pox	18	29	15	18	21	20	20	20	29	23
Frighted	4	4	1		3		2		1	1
Goat	9	5	12	9	7	7	5	6	8	7
Grief	12	13	16	7	17	14	11	17	10	15
Impediment										16

There's a higher-res image here
<http://a7.typepad.com/6a01901d7a04f8970b01a3fc8a61f970b-pi>

STATISTICS

- John Graunt, 1662
Observations on the bills of mortality
 - First “life tables”
 - Dispelled several myths about the plague
 - First analysis of sex ratio
 - First realistic estimate of the population in London

STATISTICS

- Prompted collection of more data
- Parallel developments in probability theory
- Statistics then developed into a more rigorous discipline and was applied to:
 - Business & industry
 - Medicine
 - Science
 - ...

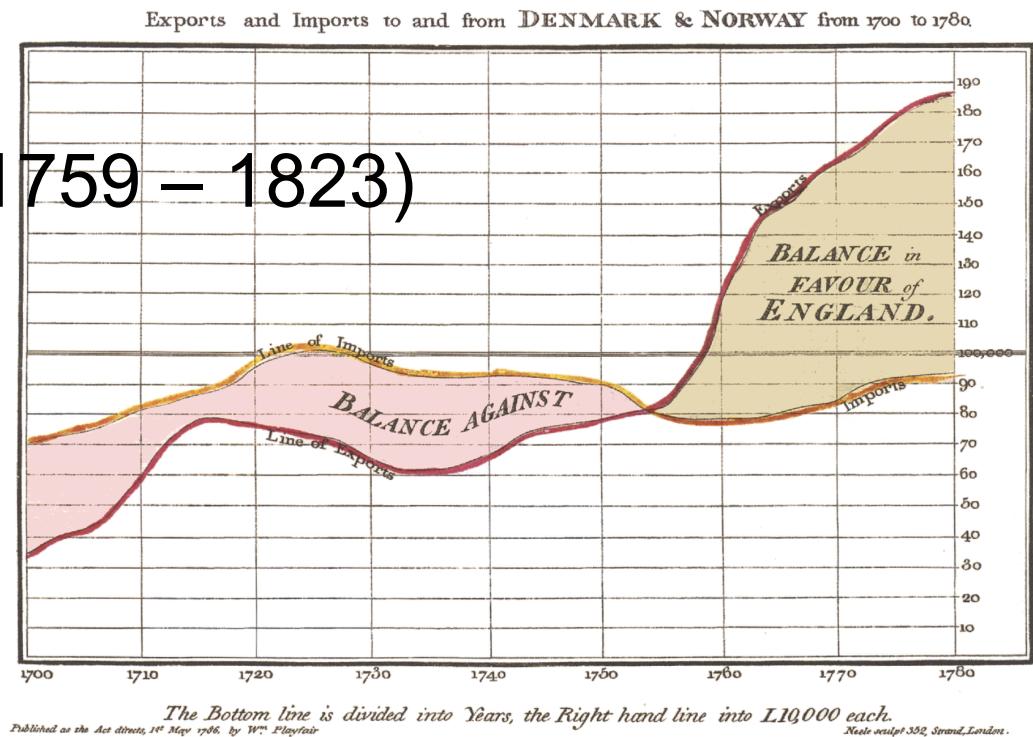
WHAT ARE STATS?

- **Statistics** is the study of the collection, analysis, interpretation, presentation and organization of data **in numerical form**.

Dodge, Y. (2006) The Oxford Dictionary of Statistical Terms, OUP.

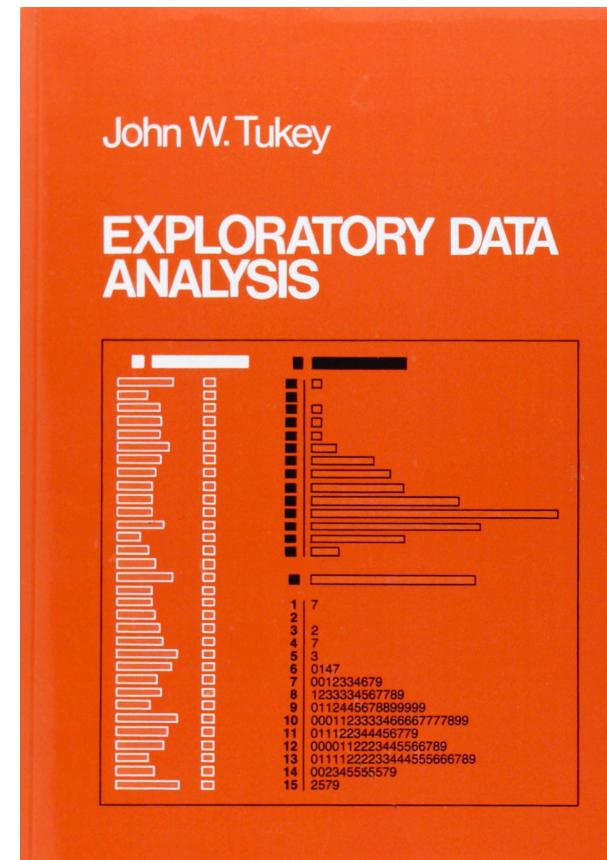
STATS & VISUALIZATION

- Statistical Charts
 - William Playfair (1759 – 1823)



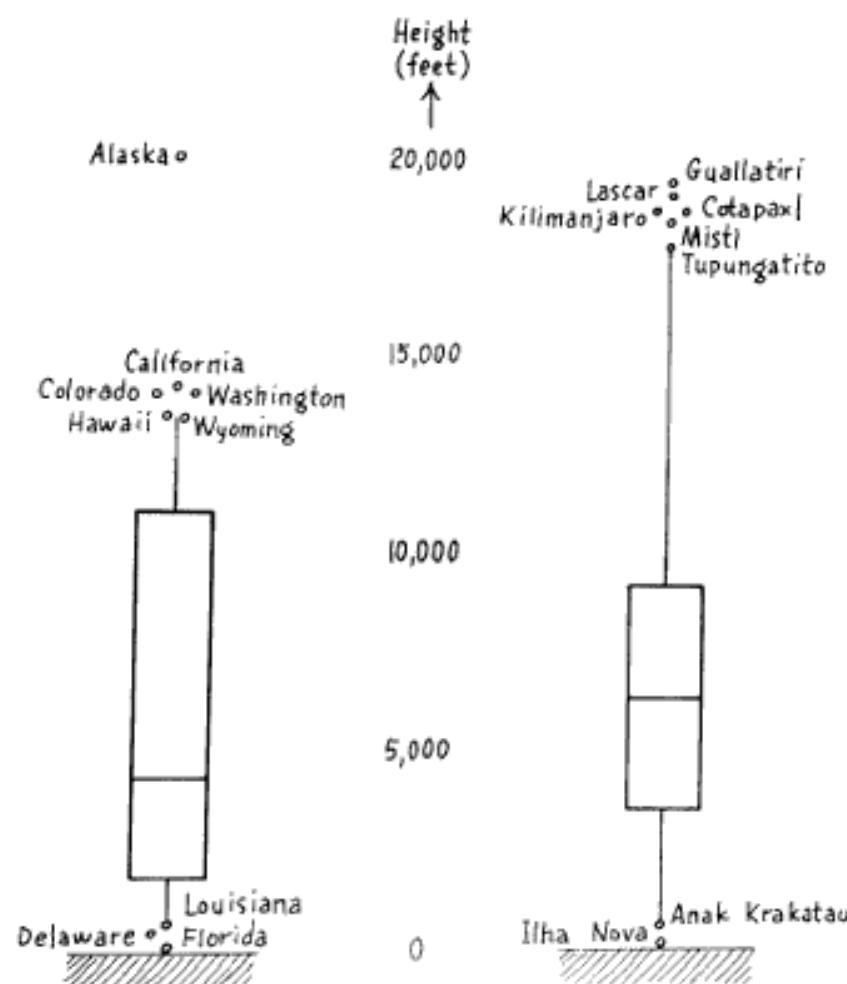
STATS & VISUALIZATION

- Exploratory Data Analysis
 - Tukey, 1977

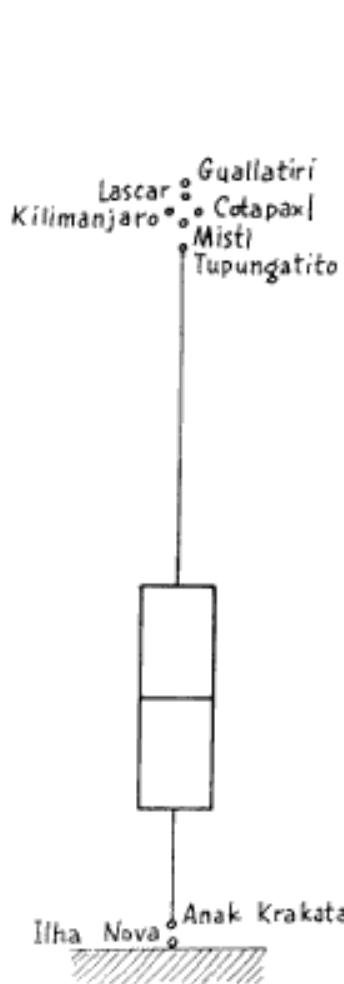


Box-and-whisker plots with end values identified

A) HEIGHTS of 50 STATES



B) HEIGHTS of 219 VOLCANOS



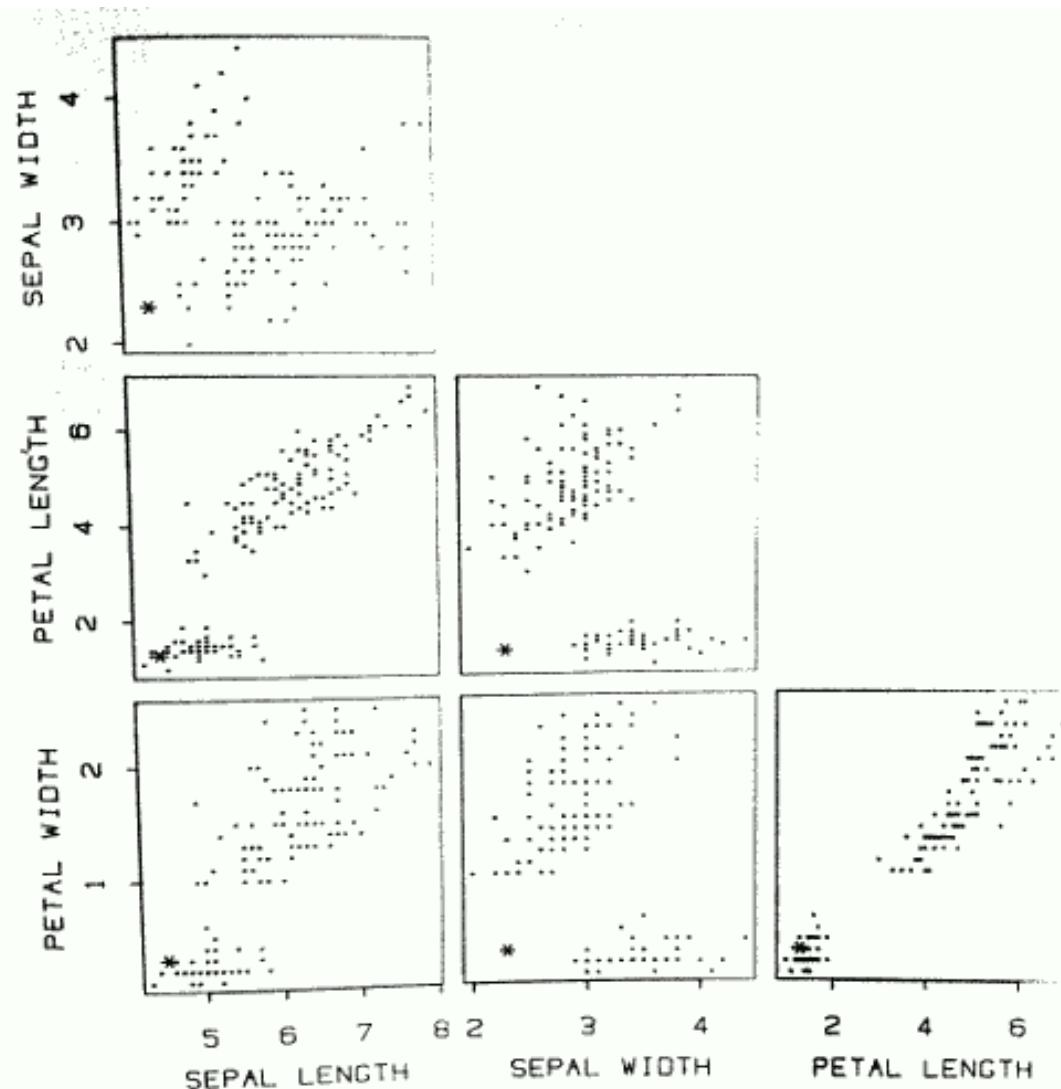


Figure 5.14 Generalized draftsman's display of the four-dimensional iris data (like Figure 5.11), with one flower plotted as an asterisk.

STATS & VISUALIZATION

- Statistical Graphics

STATS & VISUALIZATION

- Statistical Graphics

Gelman and Unwin (2012) *Infovis and Statistical Graphics: Different Goals, Different Looks*

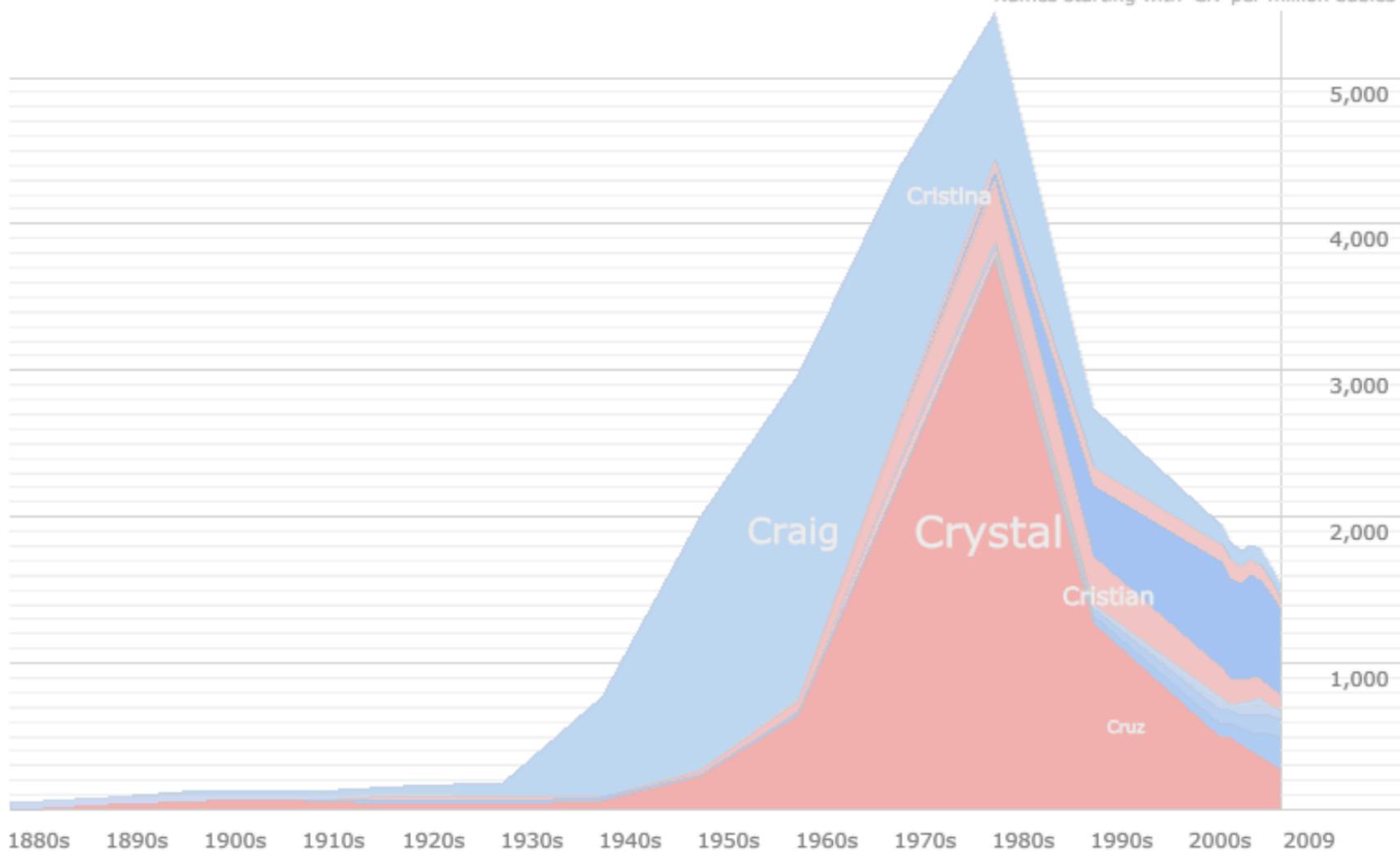
Baby Name > cr

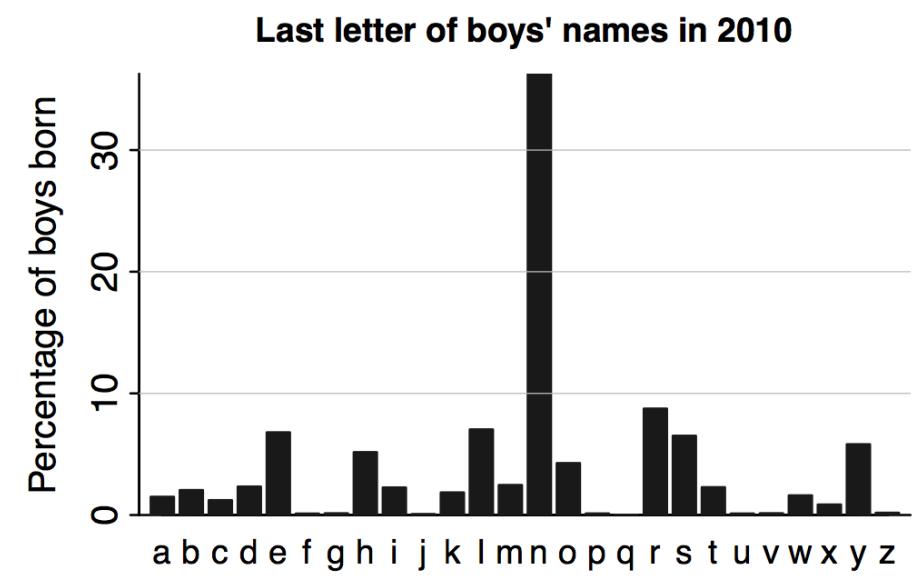
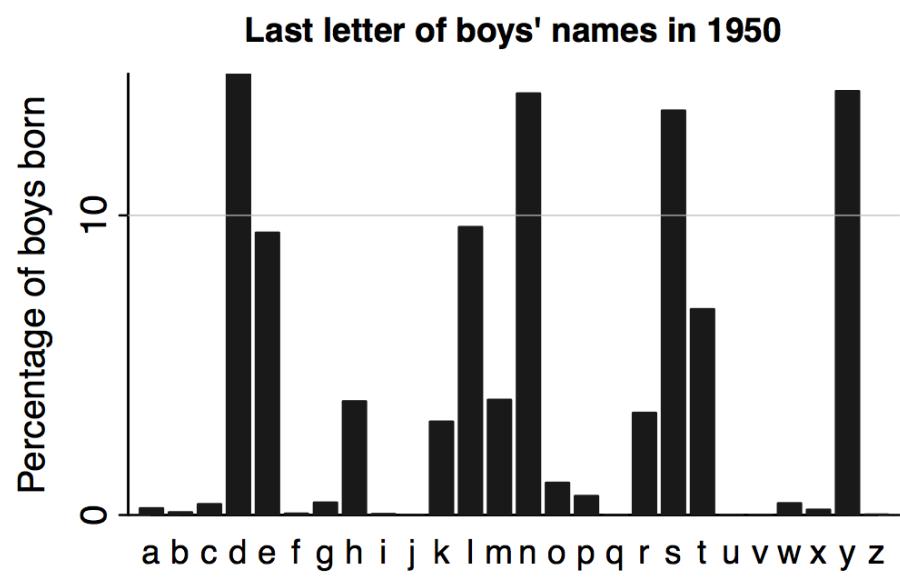


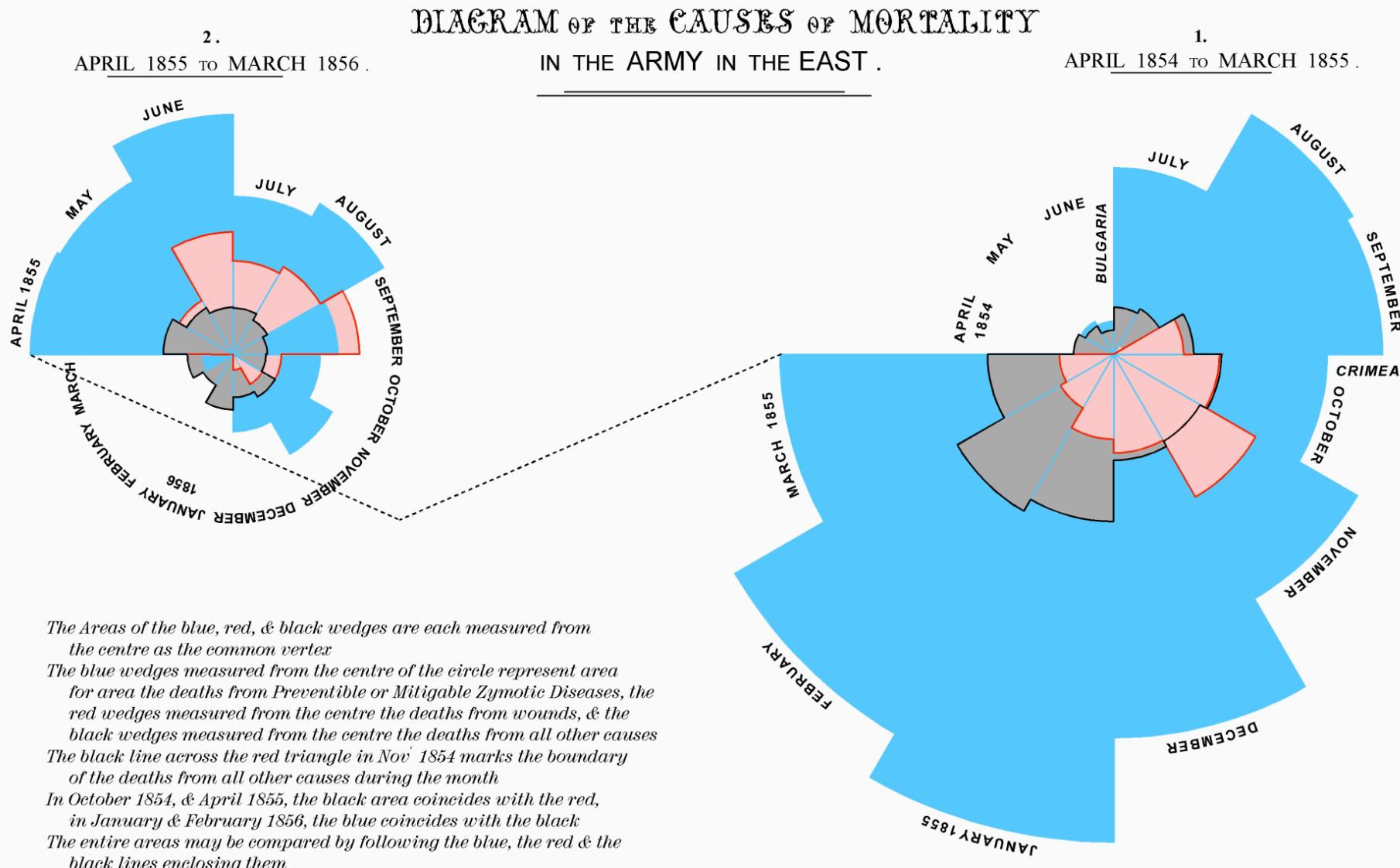
Both Boys Girls

2009 rank: boys 1000 500 100 25 1
girls 1000 500 100 25 1

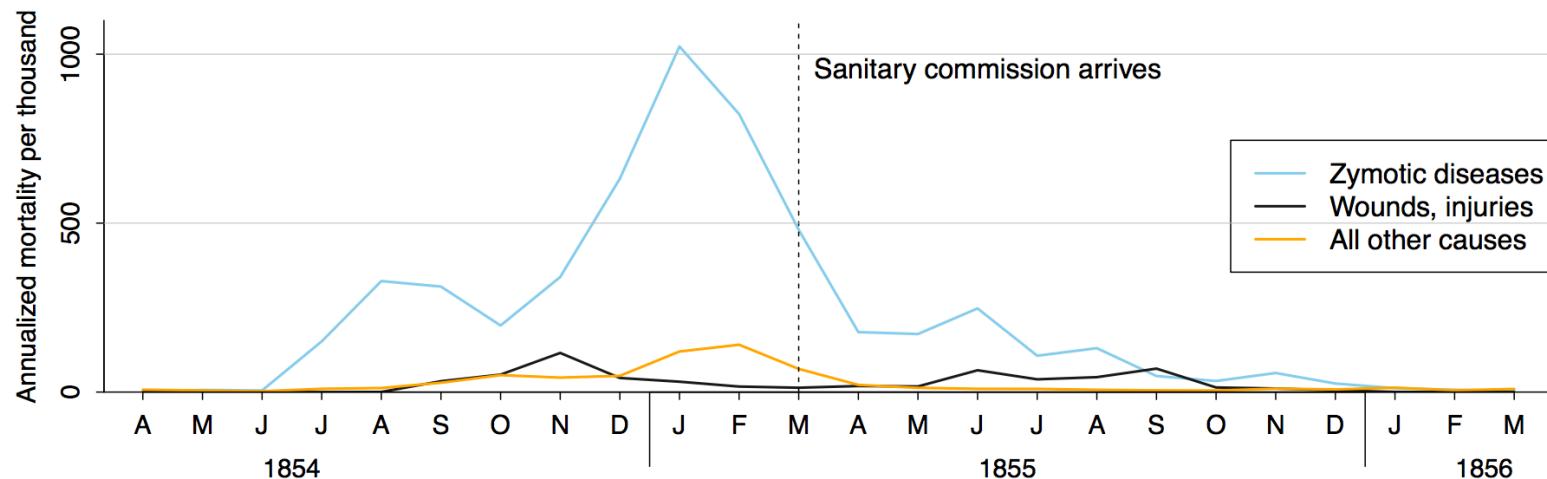
Names starting with 'CR' per million babies



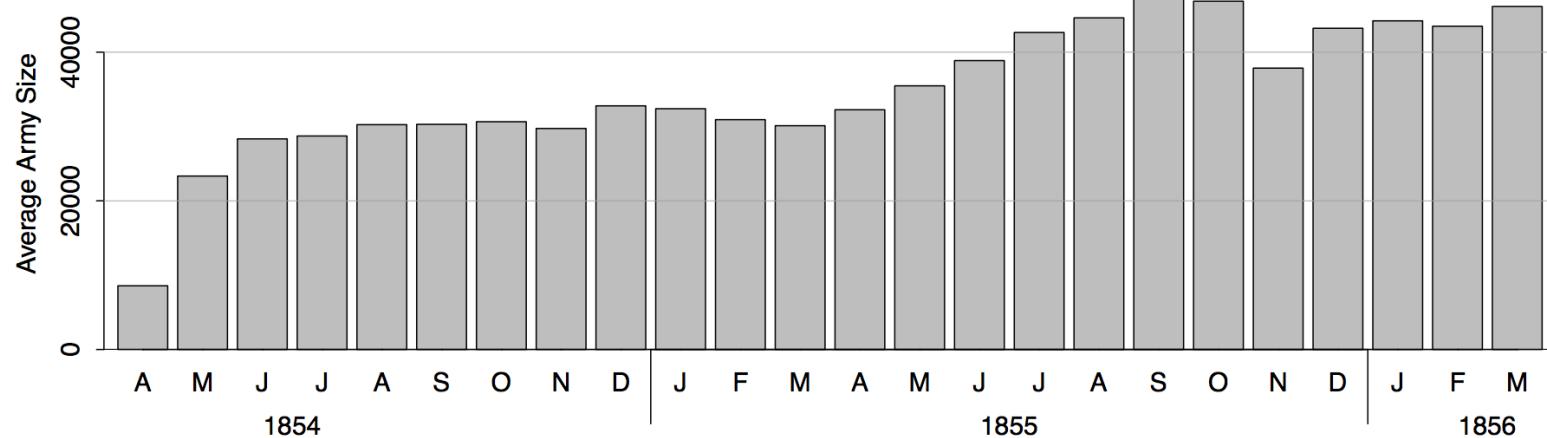




Mortality rates in the Crimean War from April 1854 to March 1856



British Army Size in the Crimean War from April 1854 to March 1856



46 64 54 77 67 68 62 56 38 Population
N = 9

Random
Sample

n = 4 [38 62 67 62]

$$\bar{X} = \frac{\sum x}{n} = \frac{229}{4} = 57.25$$

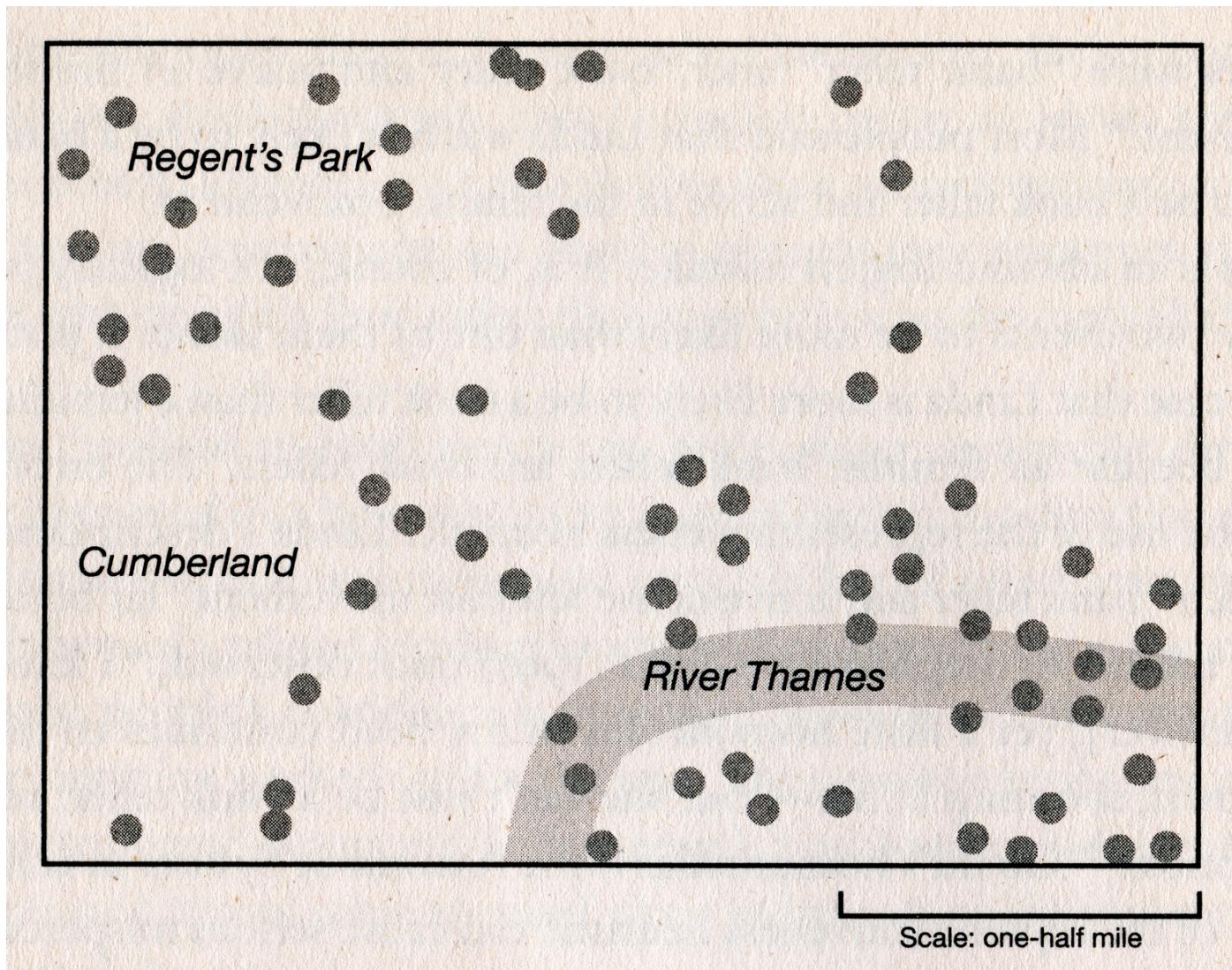
The mean of this Random Sample
equals 57.25 (i.e. $\bar{X} = 57.25$)

$$\mu_x = \frac{\sum x}{N} = \frac{532}{9} = 59.11$$

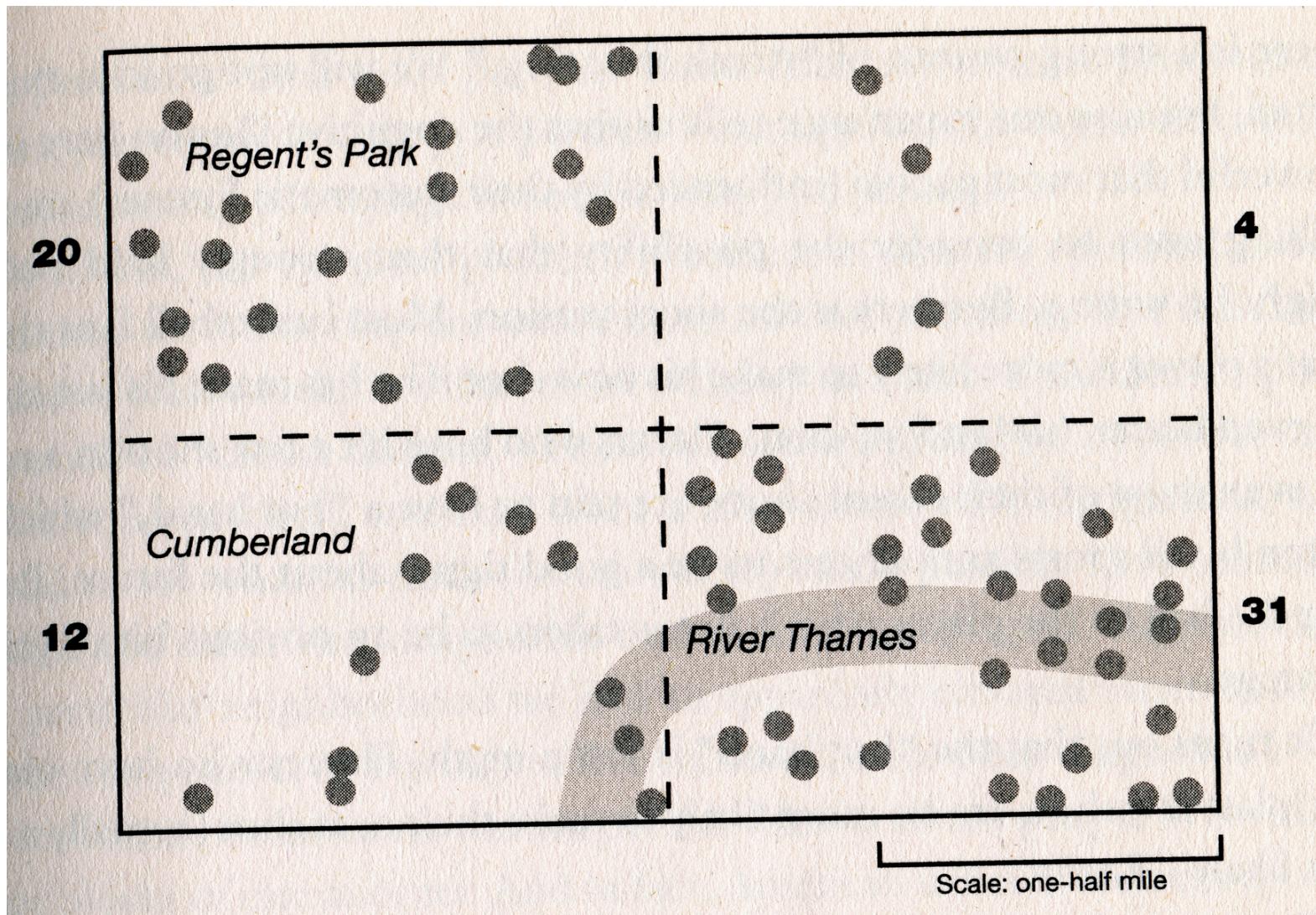
The Mean of this Population (μ_x)
equals 59.11 (i.e. $\mu_x = 59.11$)

The Central Limit Theorem tells us
that \bar{X} is an unbiased estimate
of μ_x . (i.e. $\bar{X} \rightarrow \mu_x$)

In short, with only one random sample to go on, the mean of the
sample ($\bar{X} = 57.25$) is our best estimate of the population mean (μ_x)



German bombings in London during WWII



German bombings in London during WWII

STATS & VISUALIZATION

- Confirmatory Analysis
 - Testing hypotheses
 - Example: is this new drug effective?
 - Strong focus on automatic procedures, computation and objectivity
 - Looking at data can impair objectivity:
 - Data dredging, snooping, fishing, mining

STATS & VISUALIZATION

Exploratory data analysis is sometimes compared to **detective work**: it is the process of gathering evidence.

Confirmatory data analysis is comparable to a **court trial**: it is the process of evaluating evidence.

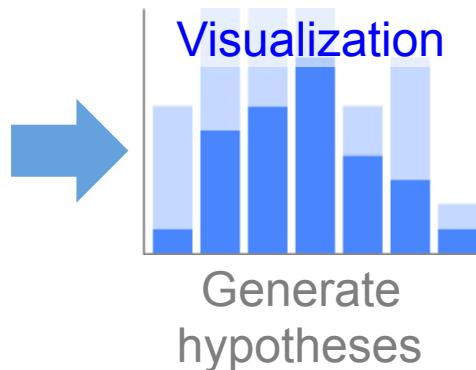
Exploratory analysis and confirmatory analysis “can —and should—proceed side by side” (Tukey; 1977).

Quoted from the SAS Institute

STATS & VISUALIZATION

Workflows

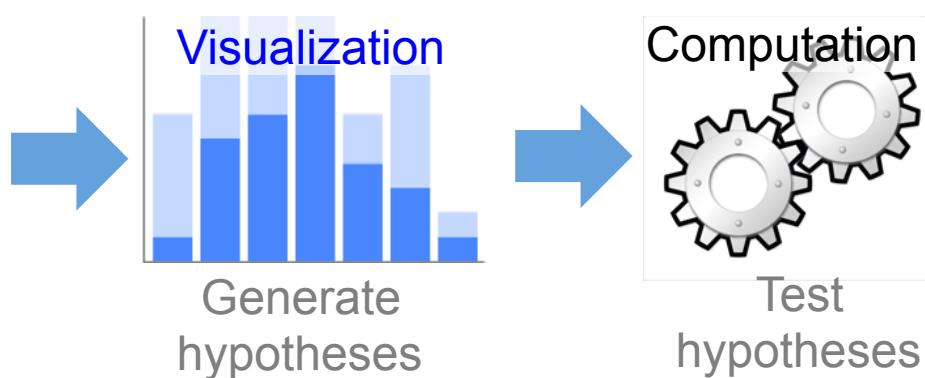
From Block	To Block	Request Time	Start Time	End Time	Seek Time
4	36	2.230	2.230	4.330	2.100
36	33	4.230	4.330	5.030	0.700
33	117	3.123	5.030	9.730	4.700
117	38	6.230	9.730	14.130	4.400
38	39	10.230	14.130	14.130	0.000
39	36	8.230	14.130	14.730	0.600
36	37	14.230	14.730	14.730	0.000
37	35	12.230	14.730	15.330	0.600
35	191	16.123	16.123	24.423	8.300
191	198	21.123	24.423	25.323	0.900
198	39	16.230	25.323	33.823	8.500
39	39	30.230	33.823	33.823	0.000
39	36	20.230	33.823	34.423	0.600

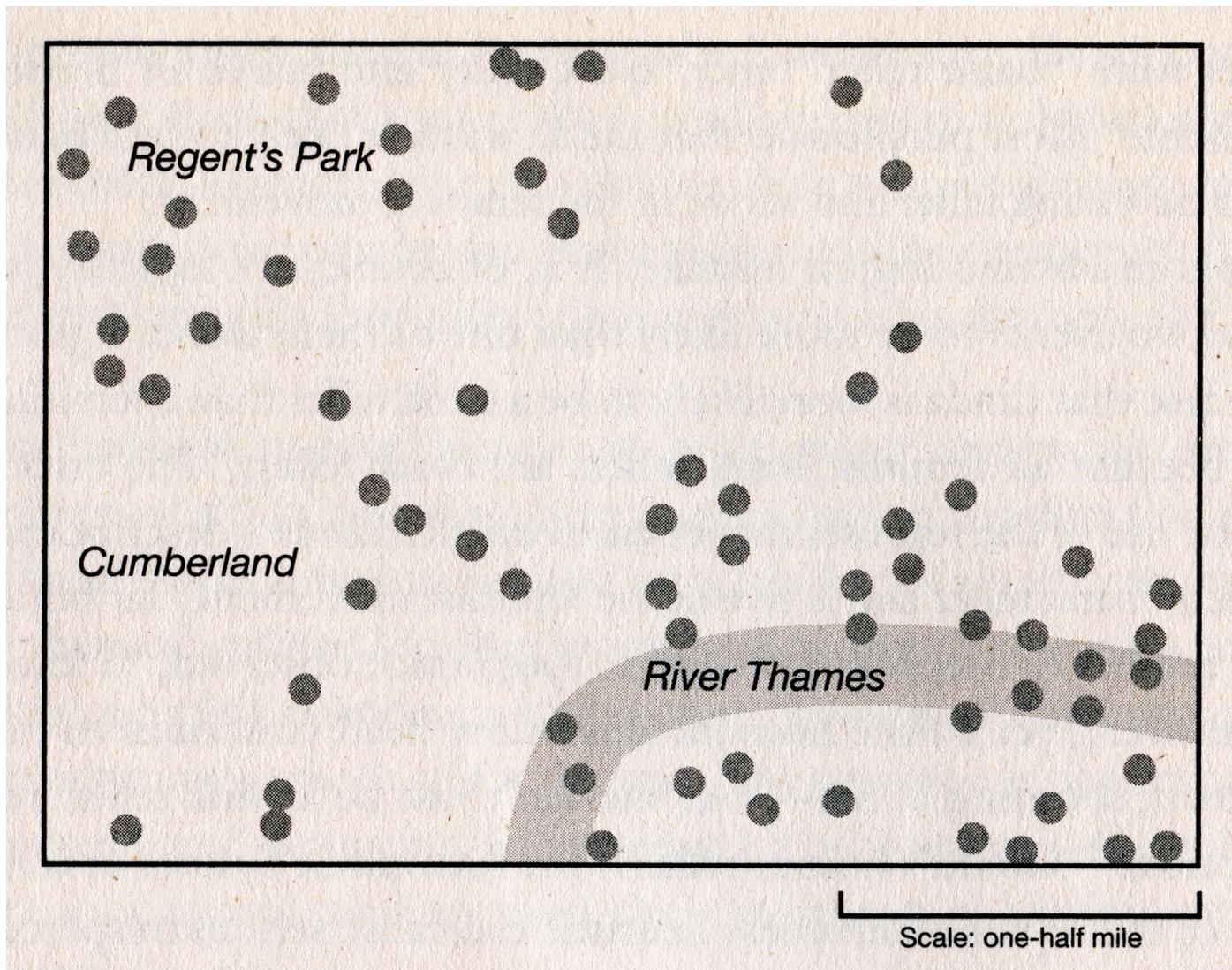


STATS & VISUALIZATION

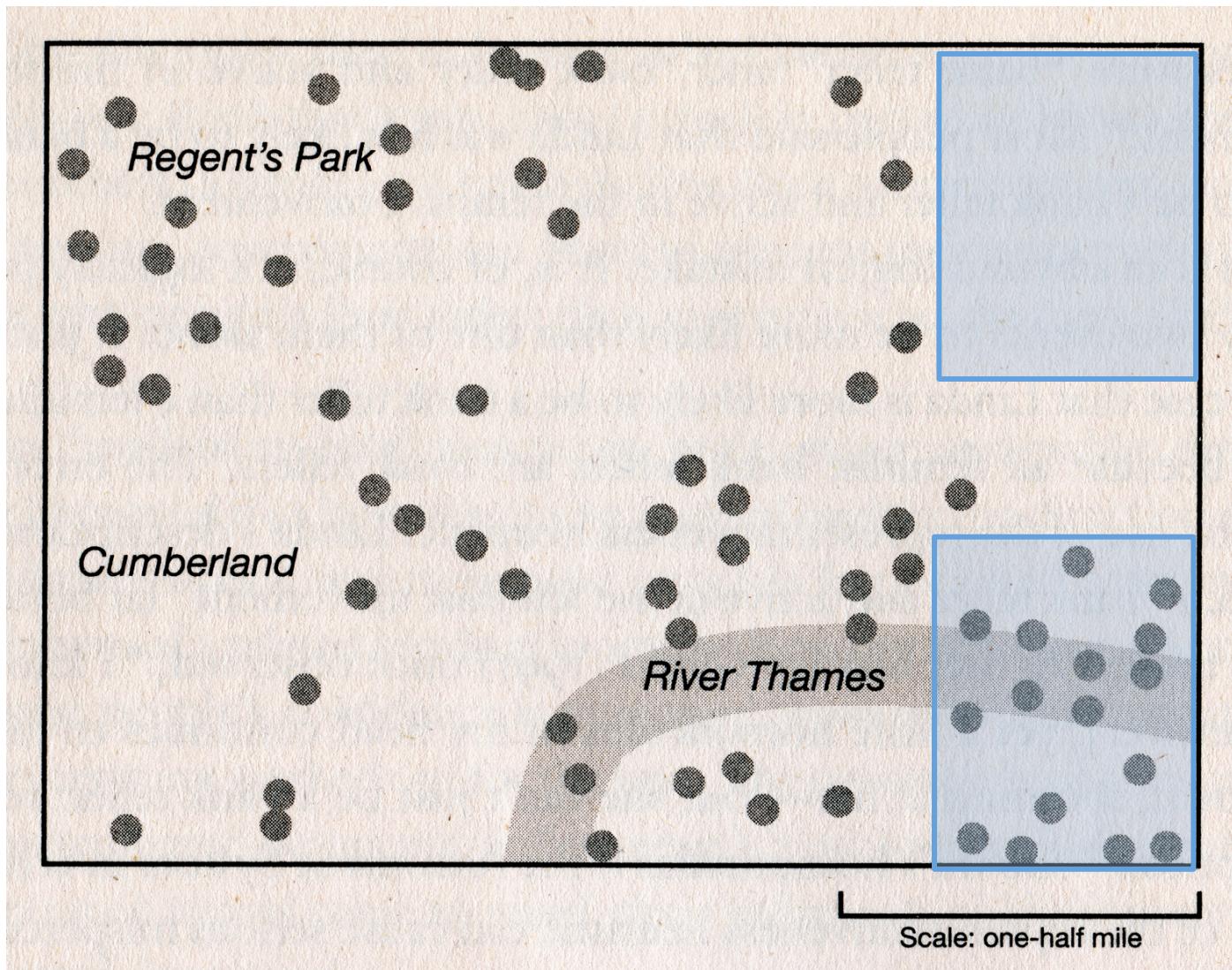
Workflows

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German bombings in London during WWII

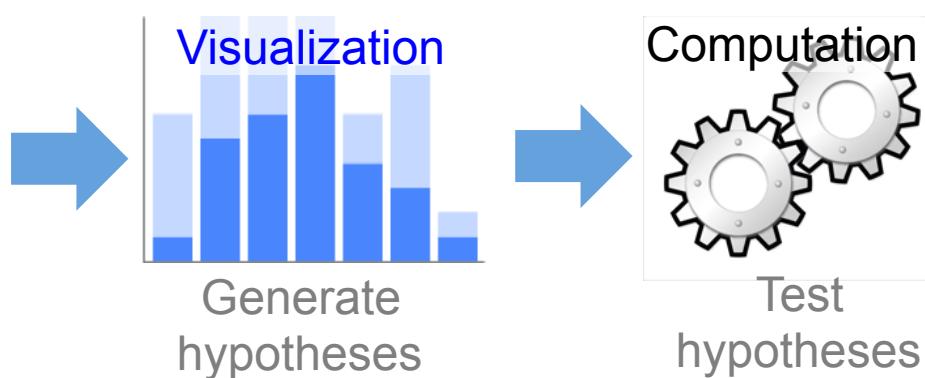


German bombings in London during WWII

STATS & VISUALIZATION

Workflows

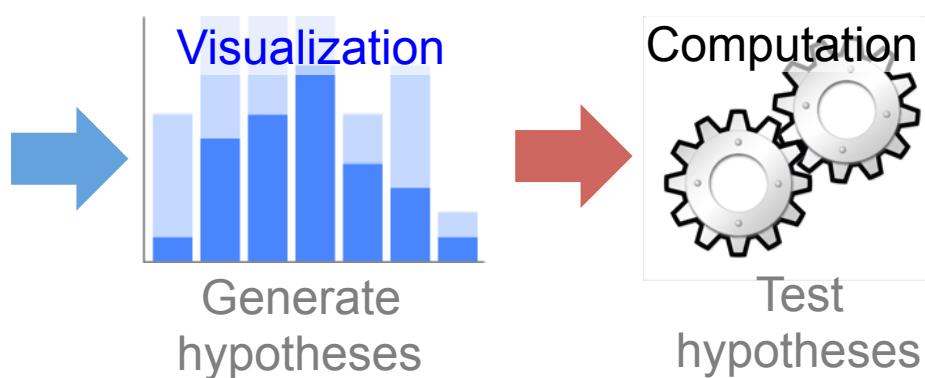
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STATS & VISUALIZATION

Workflows

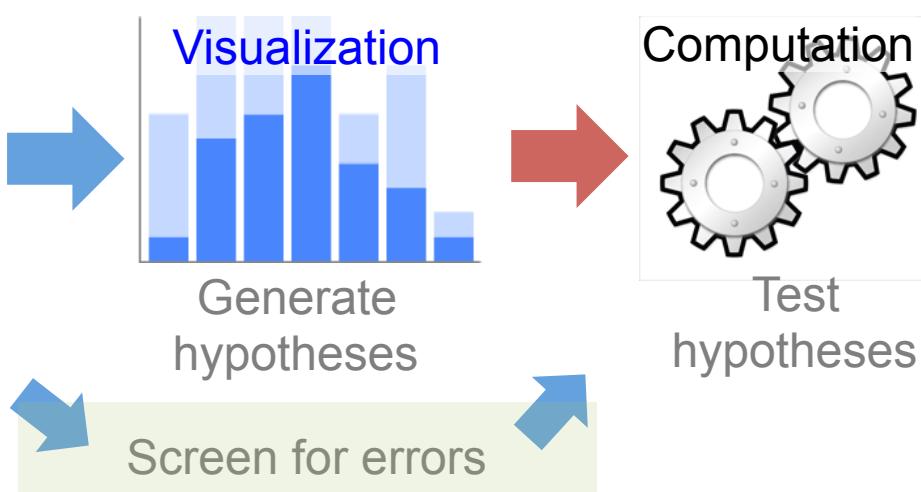
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STATS & VISUALIZATION

Workflows

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STATS & VISUALIZATION

[...] the type of "atheoretical" search for patterns that we are sometimes warned against in graduate school **can save us from the humiliation of having to retract conclusions we might ultimately make on the basis of contaminated data.**

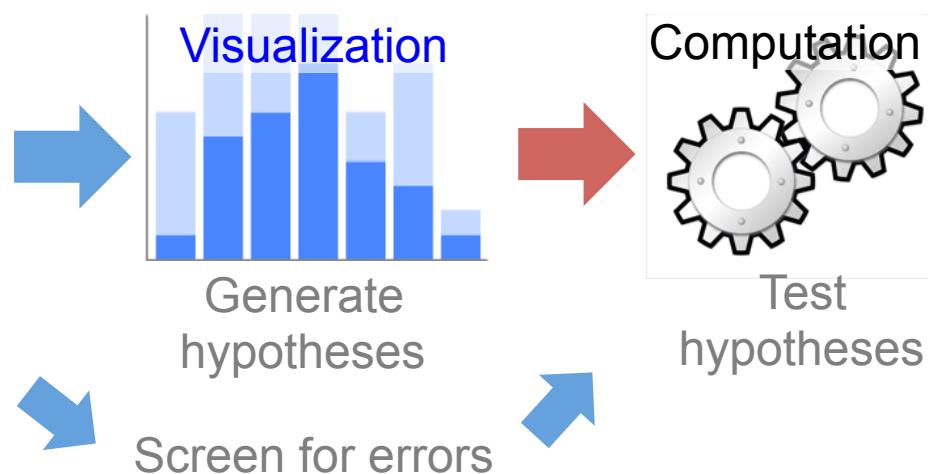
We are warned against fishing expeditions for understandable reasons, but **blind application of models without screening our data is a far graver error.**

(Wilkinson, 1999)

STATS & VISUALIZATION

Workflows

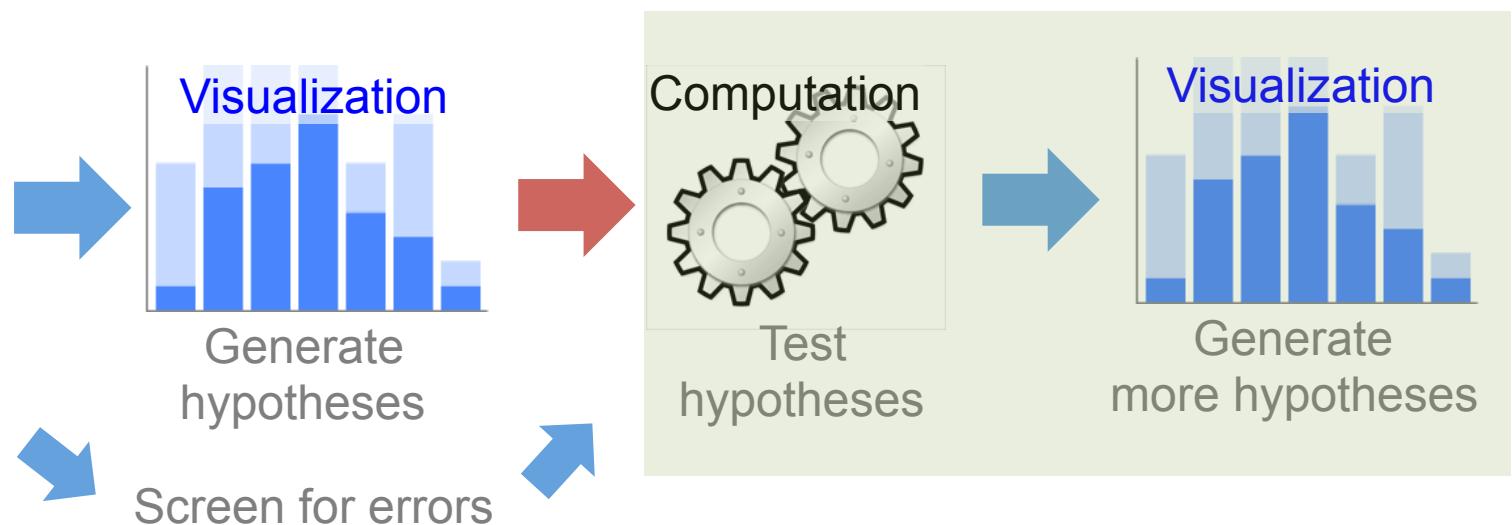
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STATS & VISUALIZATION

Workflows

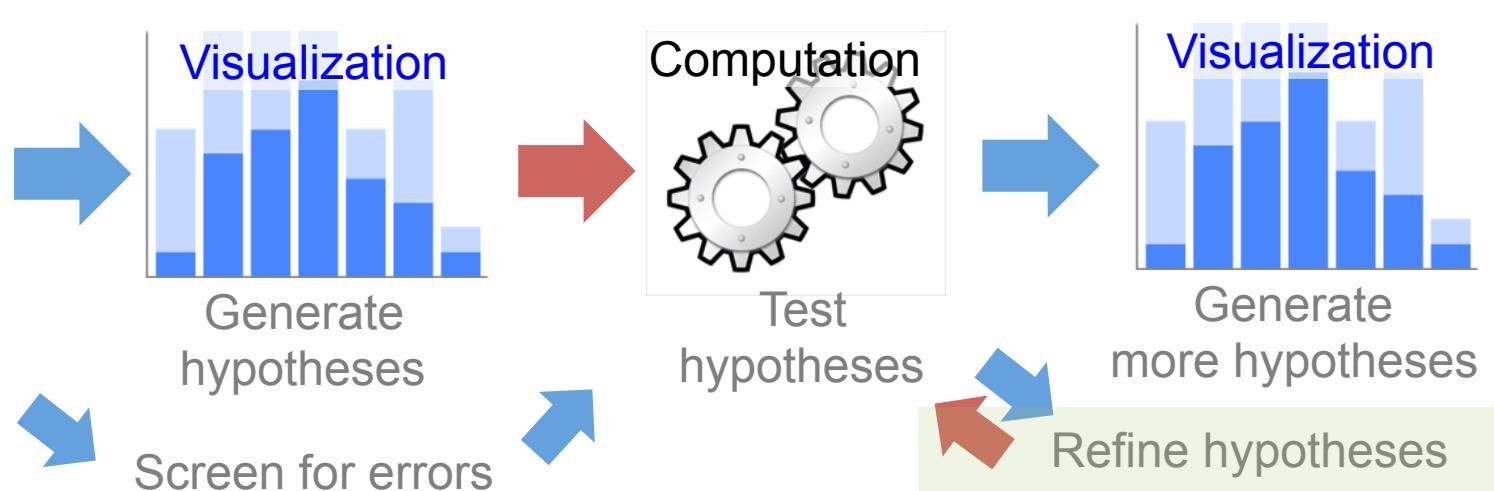
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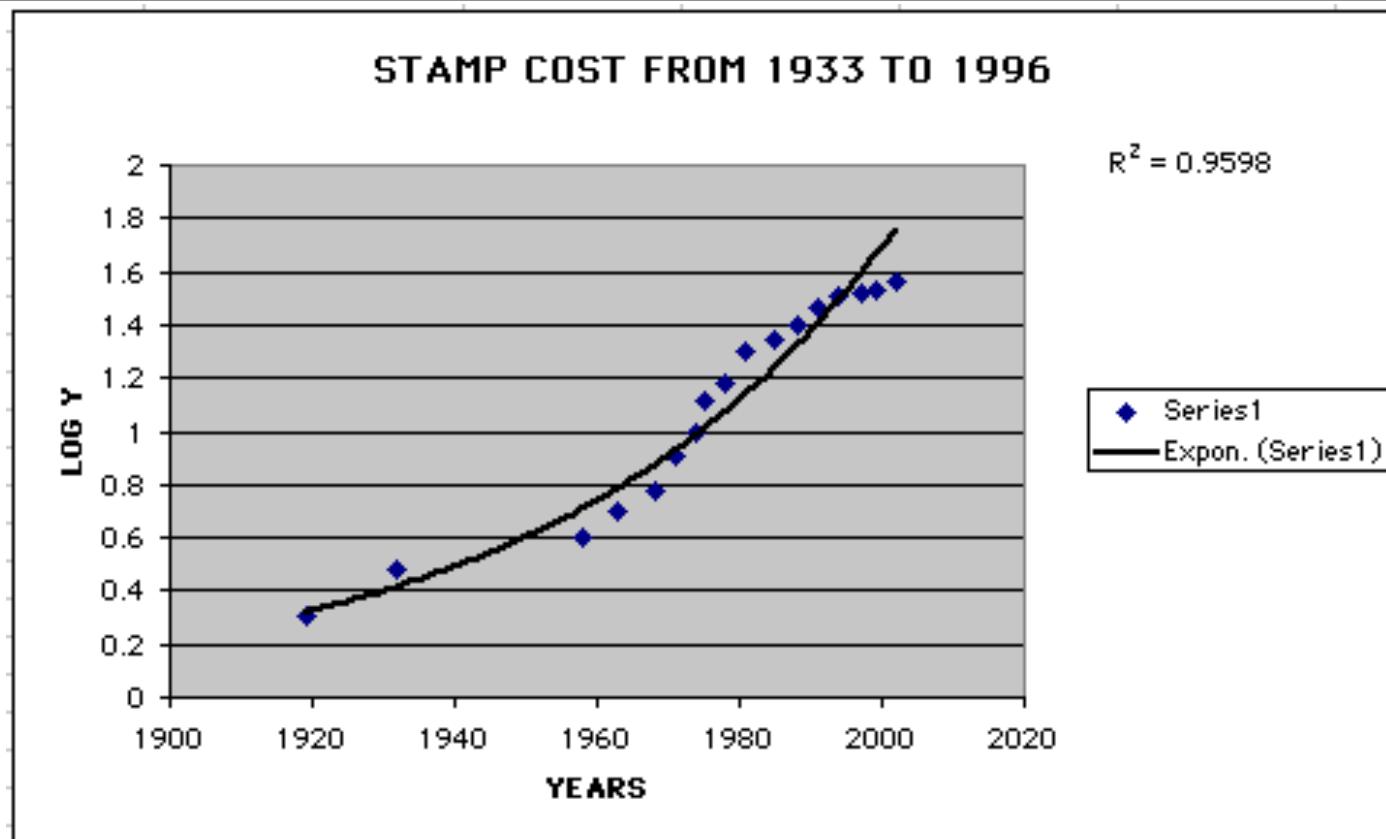
STATS & VISUALIZATION

Workflows

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38	39	10.230	14.130	14.130	0.000
39	36	8.230	14.130	14.730	0.600
36	37	14.230	14.730	14.730	0.000
37	35	12.230	14.730	15.330	0.600
35	191	16.123	16.123	24.423	8.300
191	198	21.123	24.423	25.323	0.900
198	39	16.230	25.323	33.823	8.500
39	39	30.230	33.823	33.823	0.000
39	36	20.230	33.823	34.423	0.600



STATS & VISUALIZATION

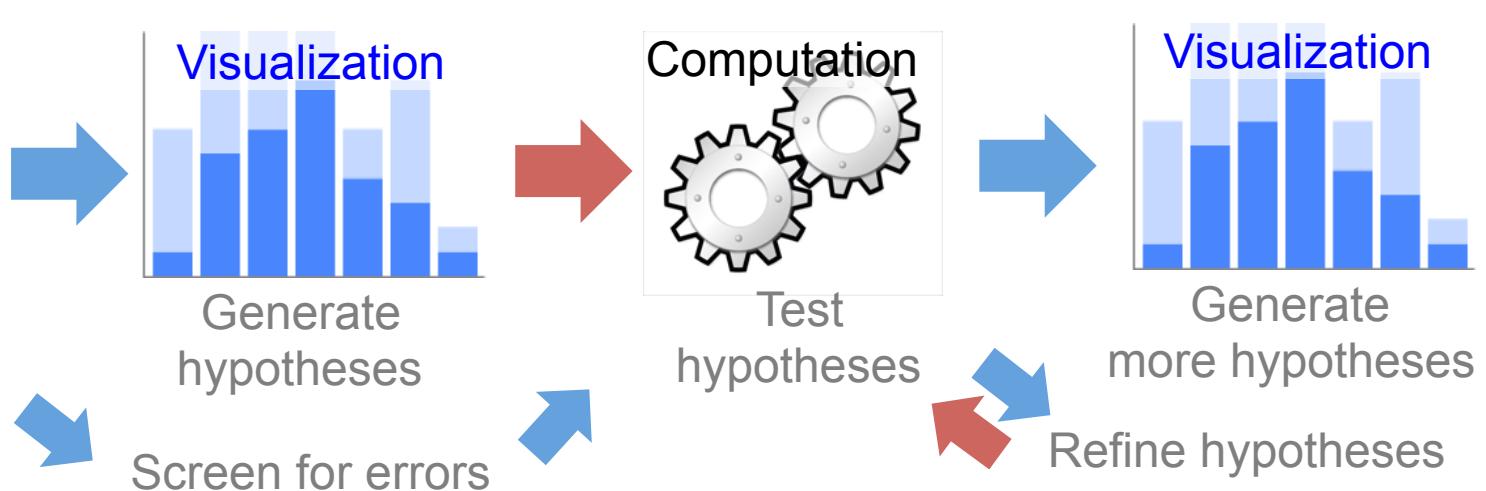


Example from Jenny Weaver

STATS & VISUALIZATION

Workflows

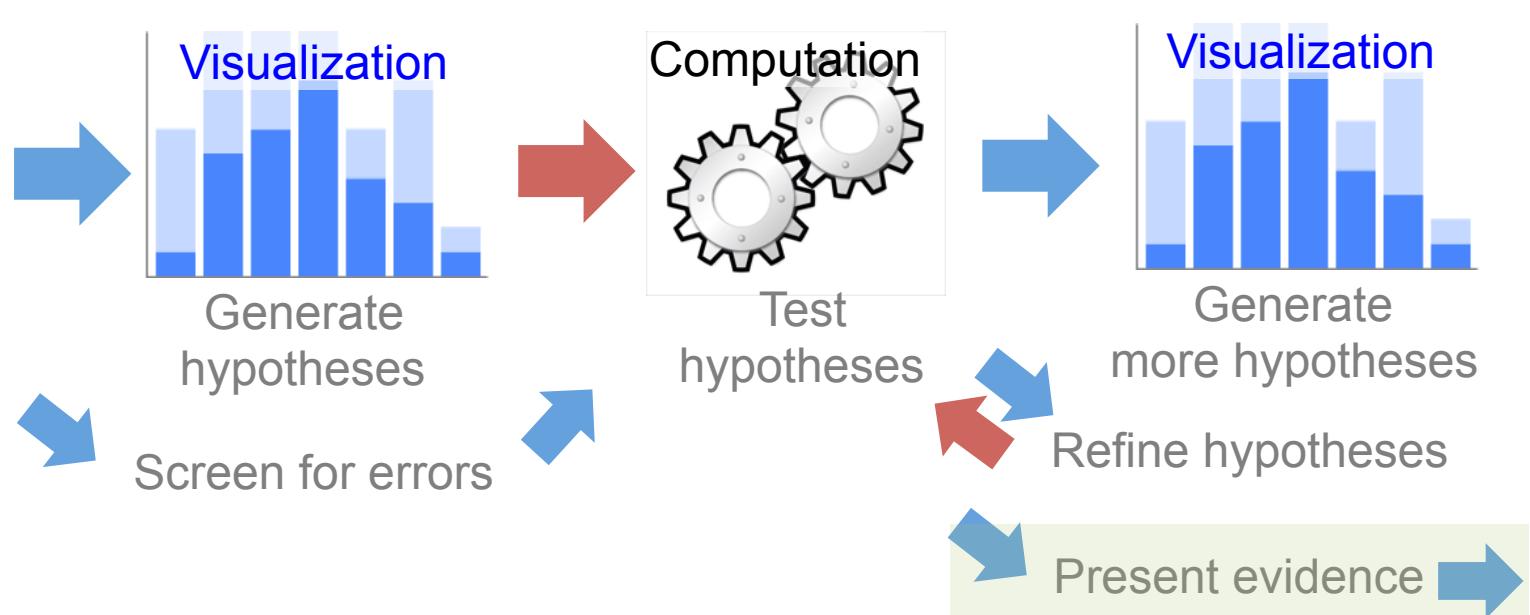
From Block	To Block	Request Time	Start Time	End Time	Seek Time
4	36	2.230	2.230	4.330	2.100
36	33	4.230	4.330	5.030	0.700
33	117	3.123	5.030	9.730	4.700
117	38	6.230	9.730	14.130	4.400
38	39	10.230	14.130	14.130	0.000
39	36	8.230	14.130	14.730	0.600
36	37	14.230	14.730	14.730	0.000
37	35	12.230	14.730	15.330	0.600
35	191	16.123	16.123	24.423	8.300
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39	36	20.230	33.823	34.423	0.600



STATS & VISUALIZATION

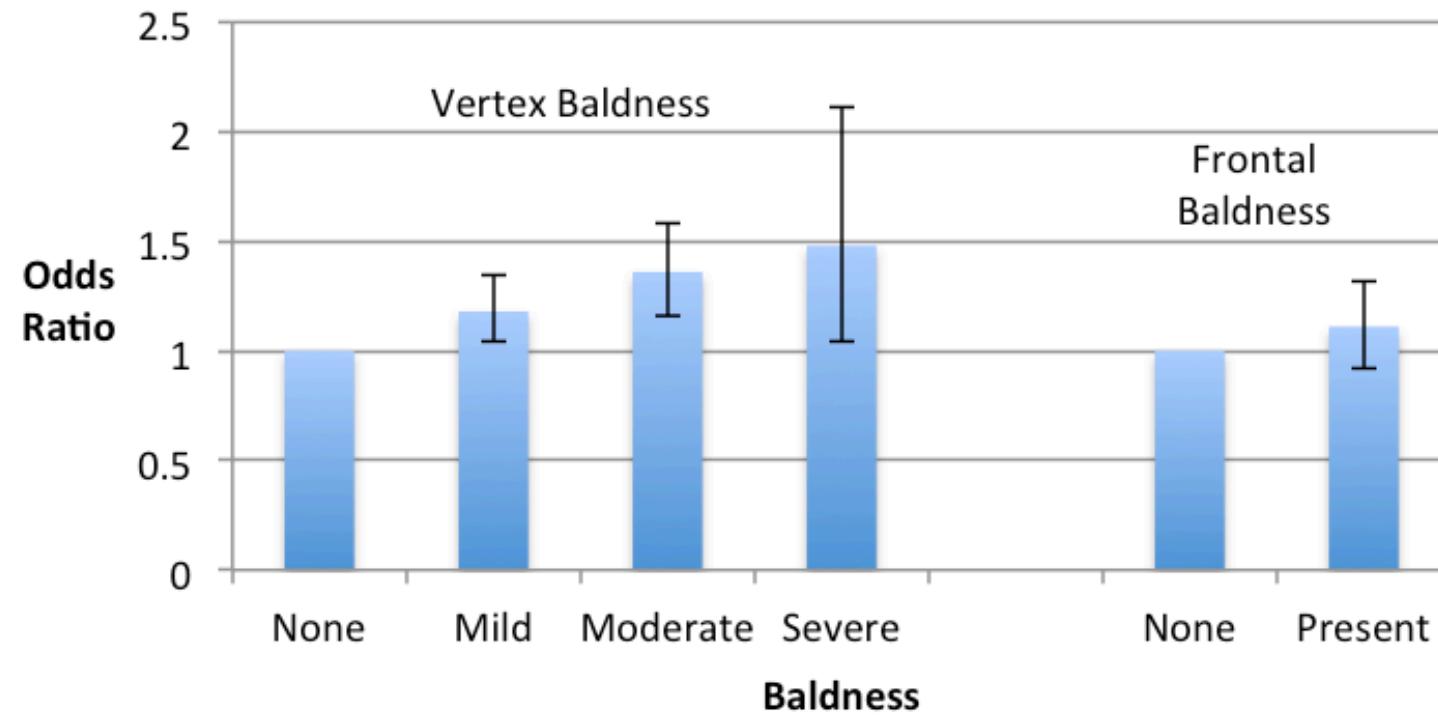
Workflows

From Block	To Block	Request Time	Start Time	End Time	Seek Time
4	36	2.230	2.230	4.330	2.100
36	33	4.230	4.330	5.030	0.700
33	117	3.123	5.030	9.730	4.700
117	38	6.230	9.730	14.130	4.400
38	39	10.230	14.130	14.130	0.000
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39	39	30.230	33.823	33.823	0.000
39	36	20.230	33.823	34.423	0.600



STATS & VISUALIZATION

Odds of Coronary Heart Disease by Baldness

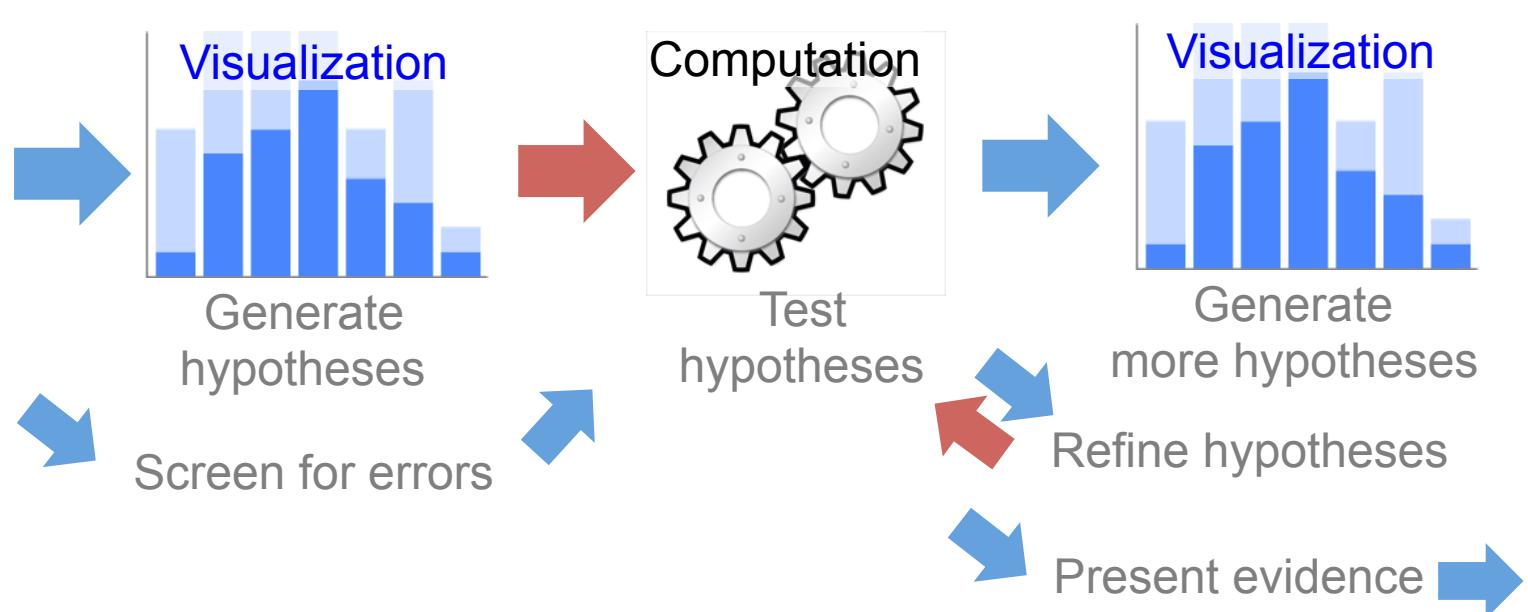


From agrippastake.blogspot.dk

STATS & VISUALIZATION

Workflows

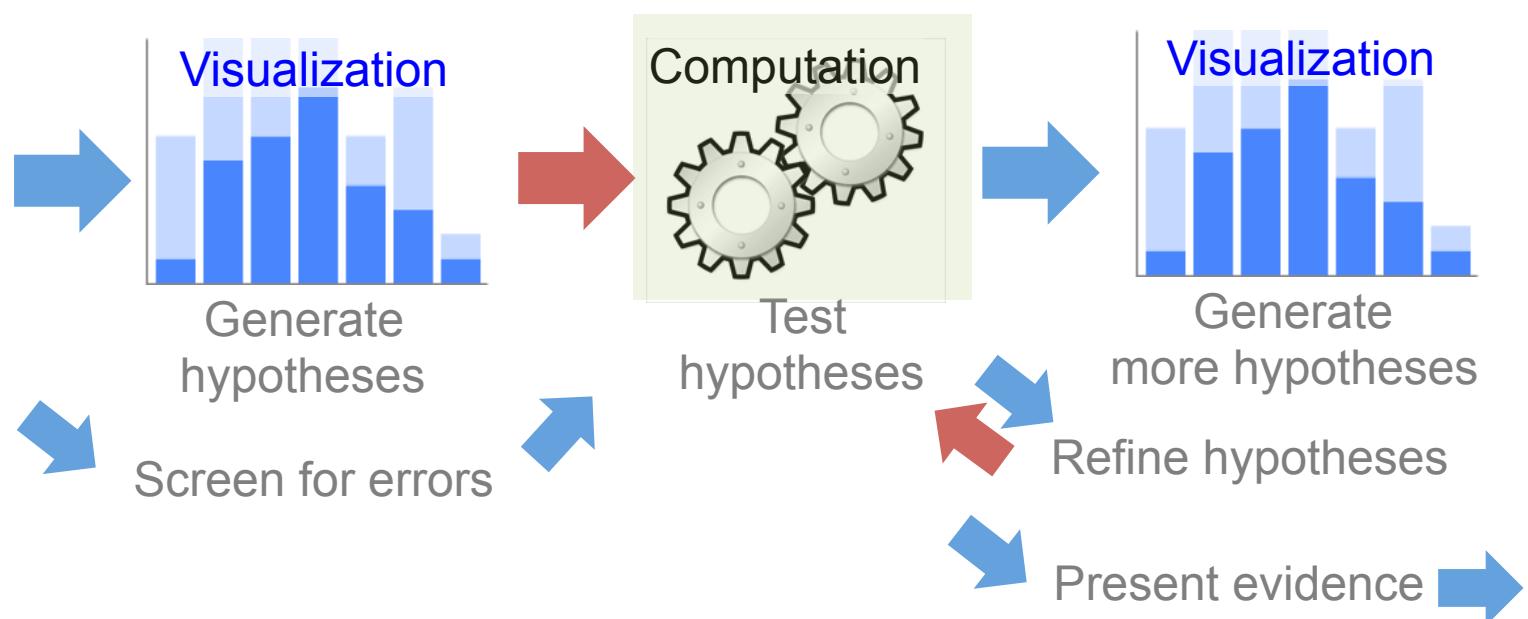
From Block	To Block	Request Time	Start Time	End Time	Seek Time
4	36	2.230	2.230	4.330	2.100
36	33	4.230	4.330	5.030	0.700
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STATS & VISUALIZATION

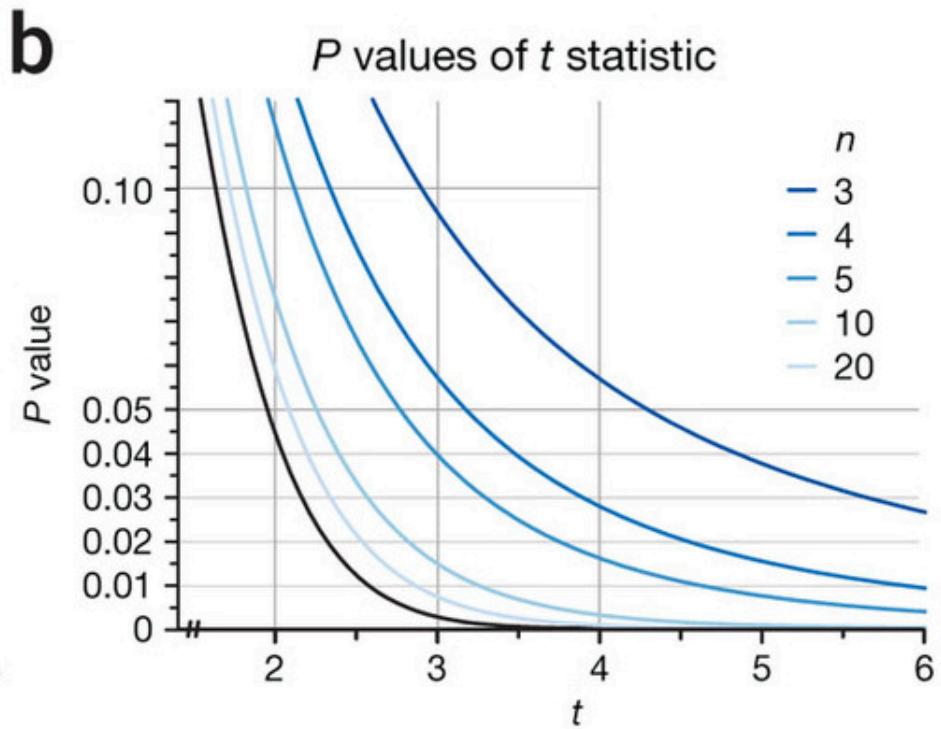
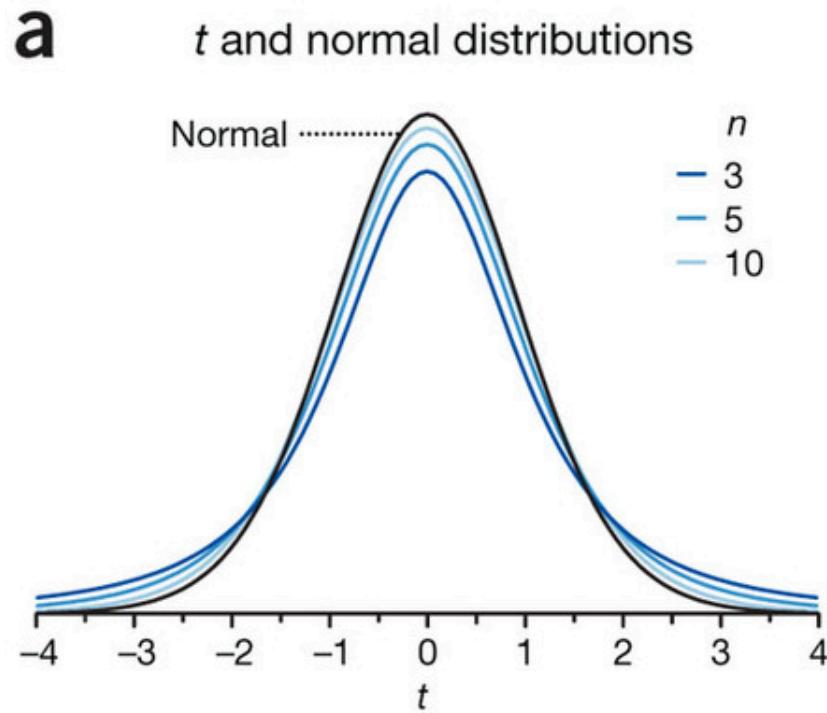
Workflows

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39	39	30.230	33.823	33.823	0.000
39	36	20.230	33.823	34.423	0.600



STATS & VISUALIZATION

- In Teaching

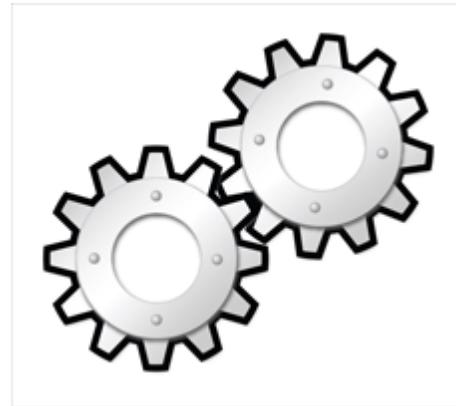


WHAT ARE STATS?

- A set of tools and methods
- Old tradition:
 - Draws from mathematics & probability theory
 - A (generally) strong focus on (computationally cheap) numerical calculations
- Good for:
 - Summarizing data for presentation
 - Rigorously testing hypotheses
 - Making predictions
 - Helping make rational decisions

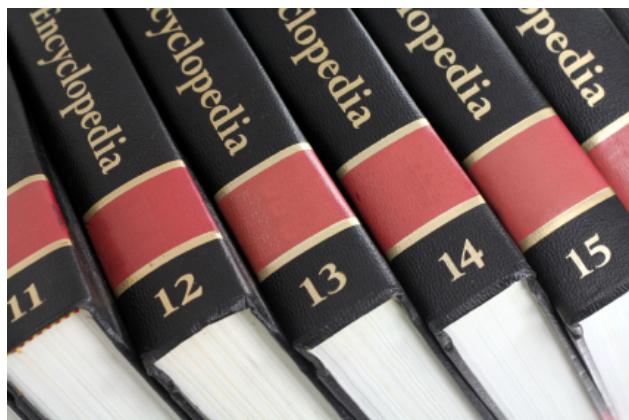
STATISTICAL TOOLS

DESCRIPTIVE STATISTICS



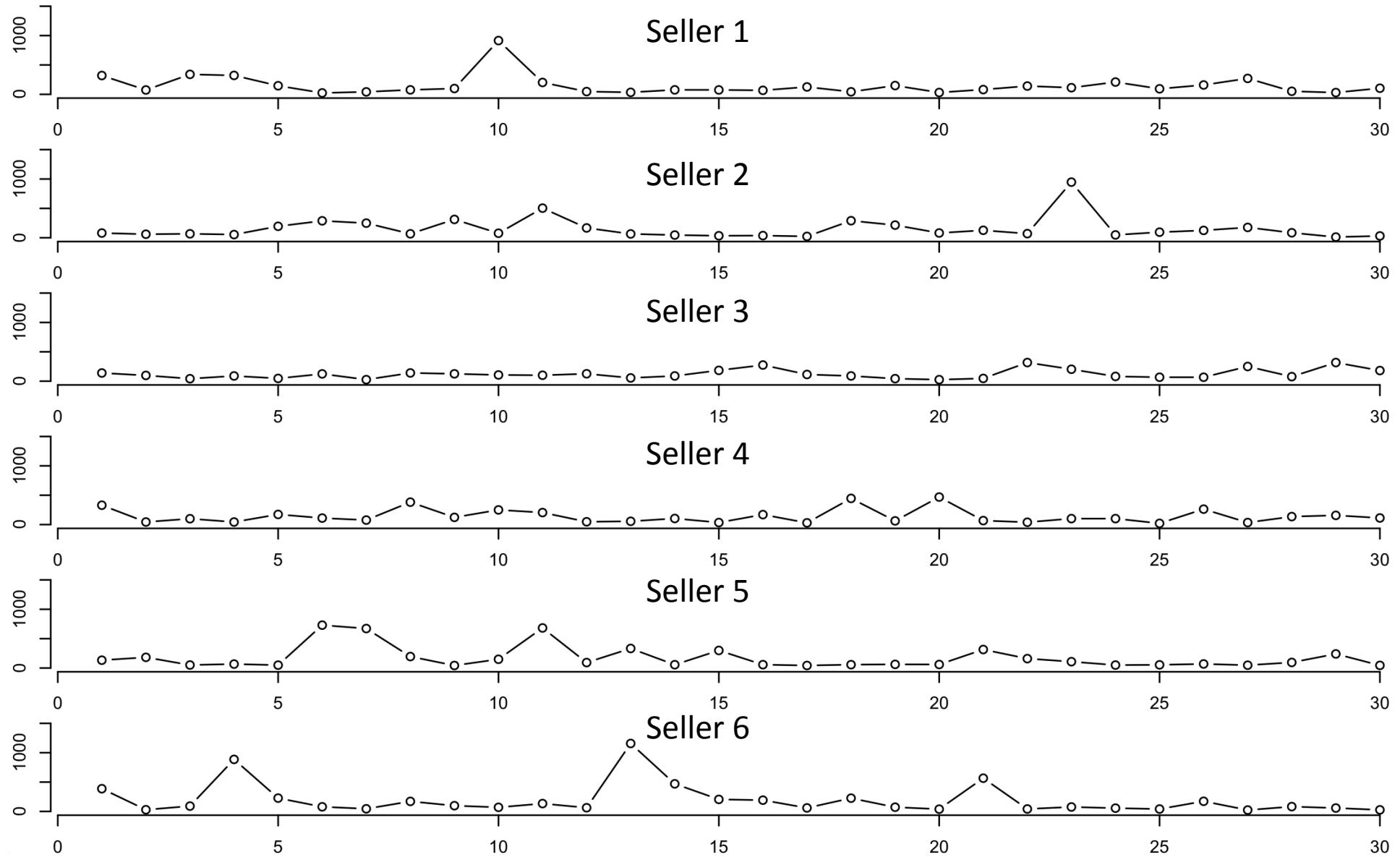
AN EXAMPLE

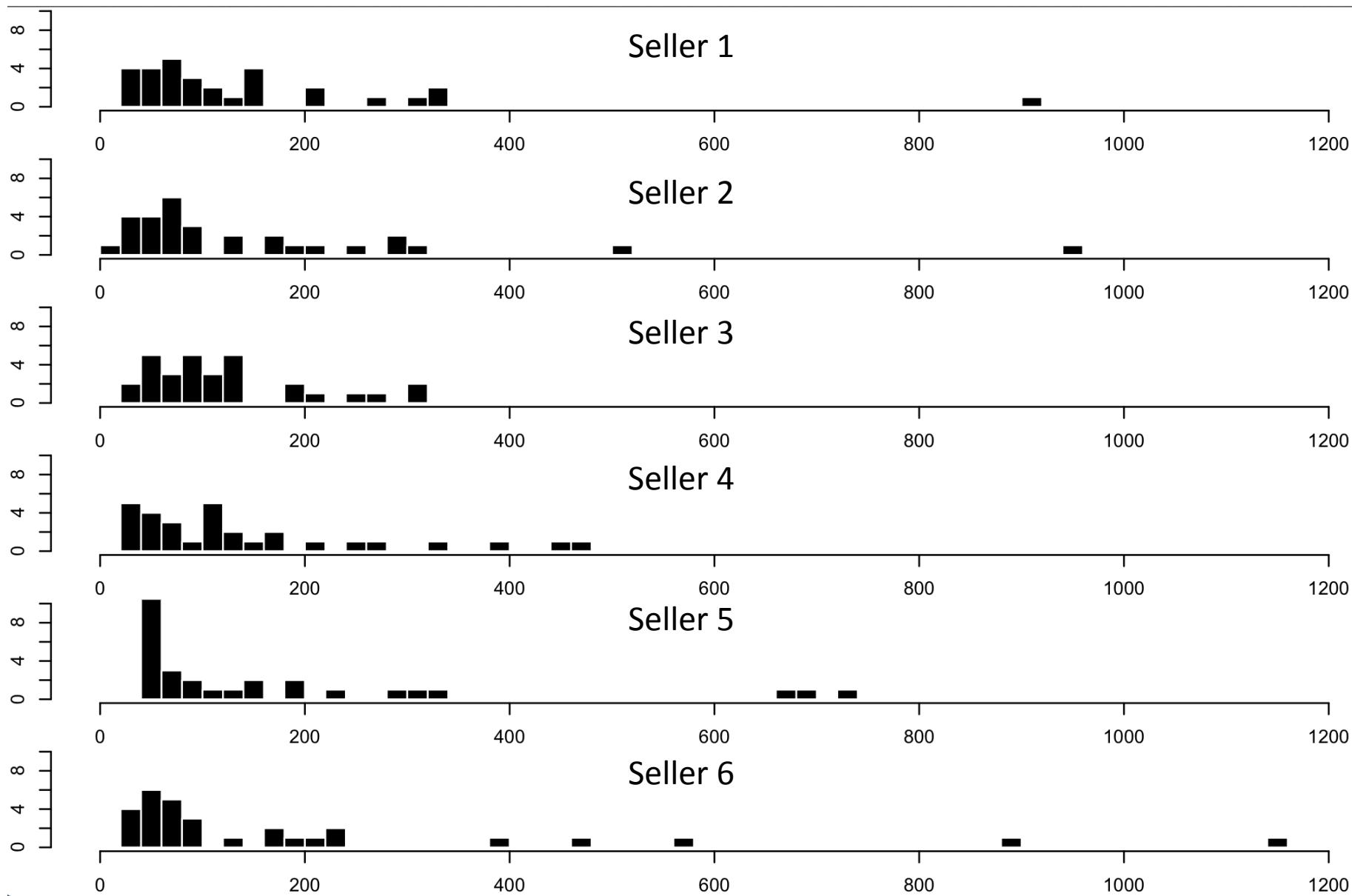
- Selling encyclopedias



day	Seller 1	Seller 2	Seller 3	Seller 4	Seller 5	Seller 6
1	€320	€80	€139	€330	€133	€387
2	€74	€60	€98	€44	€182	€29
3	€340	€67	€42	€100	€51	€91
4	€322	€54	€89	€44	€67	€886
5	€146	€195	€47	€173	€49	€227
6	€24	€288	€124	€111	€730	€79
7	€42	€249	€26	€77	€672	€45
8	€76	€67	€140	€382	€195	€171
9	€99	€312	€125	€123	€43	€98
10	€915	€77	€106	€250	€149	€70
11	€202	€504	€101	€205	€682	€134
12	€47	€167	€126	€48	€93	€63
13	€34	€65	€55	€56	€333	€1,157
14	€76	€46	€89	€104	€56	€470
15	€75	€34	€184	€35	€299	€205
16	€68	€37	€275	€170	€57	€192

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13	€34	€65	€55	€56	€333	€1,157
14	€76	€46	€89	€104	€56	€470
15	€75	€34	€184	€35	€299	€205
16	€68	€37	€275	€170	€57	€192
17	€126	€23	€114	€30	€43	€60
18	€43	€290	€89	€446	€57	€226
19	€149	€215	€43	€63	€62	€72
20	€31	€81	€26	€469	€60	€39
21	€81	€127	€47	€68	€315	€566
22	€141	€70	€317	€40	€160	€42
23	€113	€947	€203	€102	€108	€76
24	€209	€48	€81	€102	€50	€56
25	€94	€95	€67	€21	€54	€41
26	€159	€125	€67	€263	€69	€173
27	€271	€176	€250	€35	€48	€24
28	€52	€85	€77	€136	€95	€82
29	€30	€12	€317	€157	€240	€58
30	€104	€31	€181	€113	€45	€27



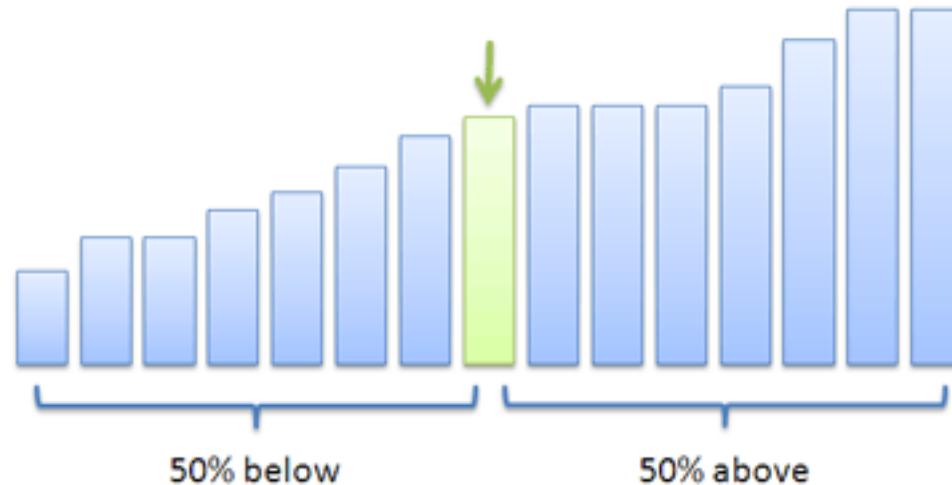


CENTRAL TENDENCY

Name & Meaning	Formula / Example	Used for
Arithmetic Mean [average]	$\frac{\text{sum}}{\text{size}} = \frac{a+b+c}{3}$	Most situations ("average item")
Median [middle value]	Middle of sorted list (2 middles? Average 'em)	Wildly varying samples (houses, incomes)
Mode [most popular]	Most popular value	No compromises (winner takes all)
Geometric Mean [average factor]	$\sqrt[3]{abc}$	Investments, growth, area, volume
Harmonic Mean [average rate]	$\frac{3}{\frac{1}{a} + \frac{1}{b} + \frac{1}{c}}$	Speed, production, cost

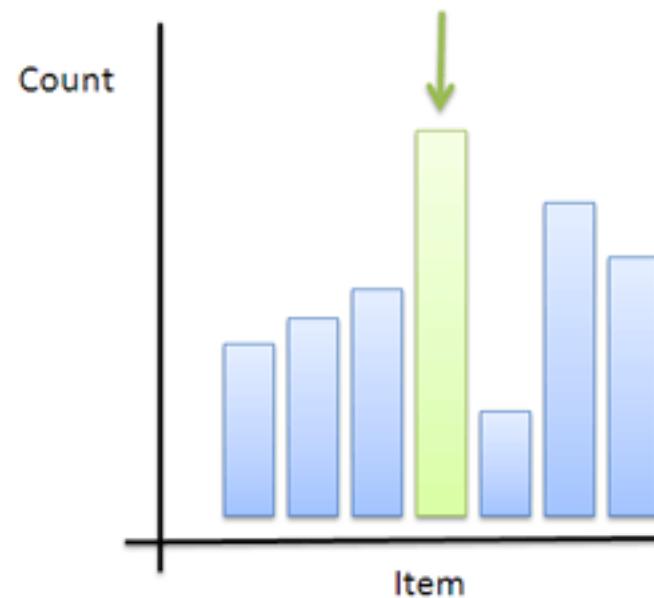
CENTRAL TENDENCY

Median



CENTRAL TENDENCY

Mode (Most Popular)

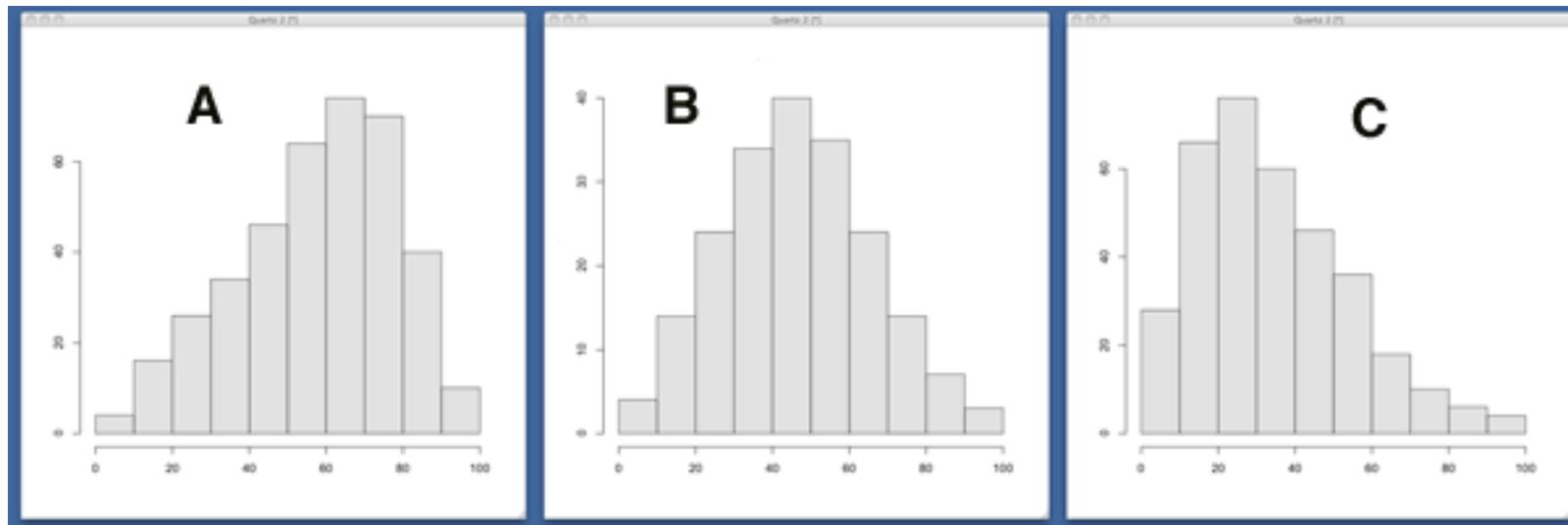


CENTRAL TENDENCY

negative skew

symmetric

positive skew



From Shreya Sethi

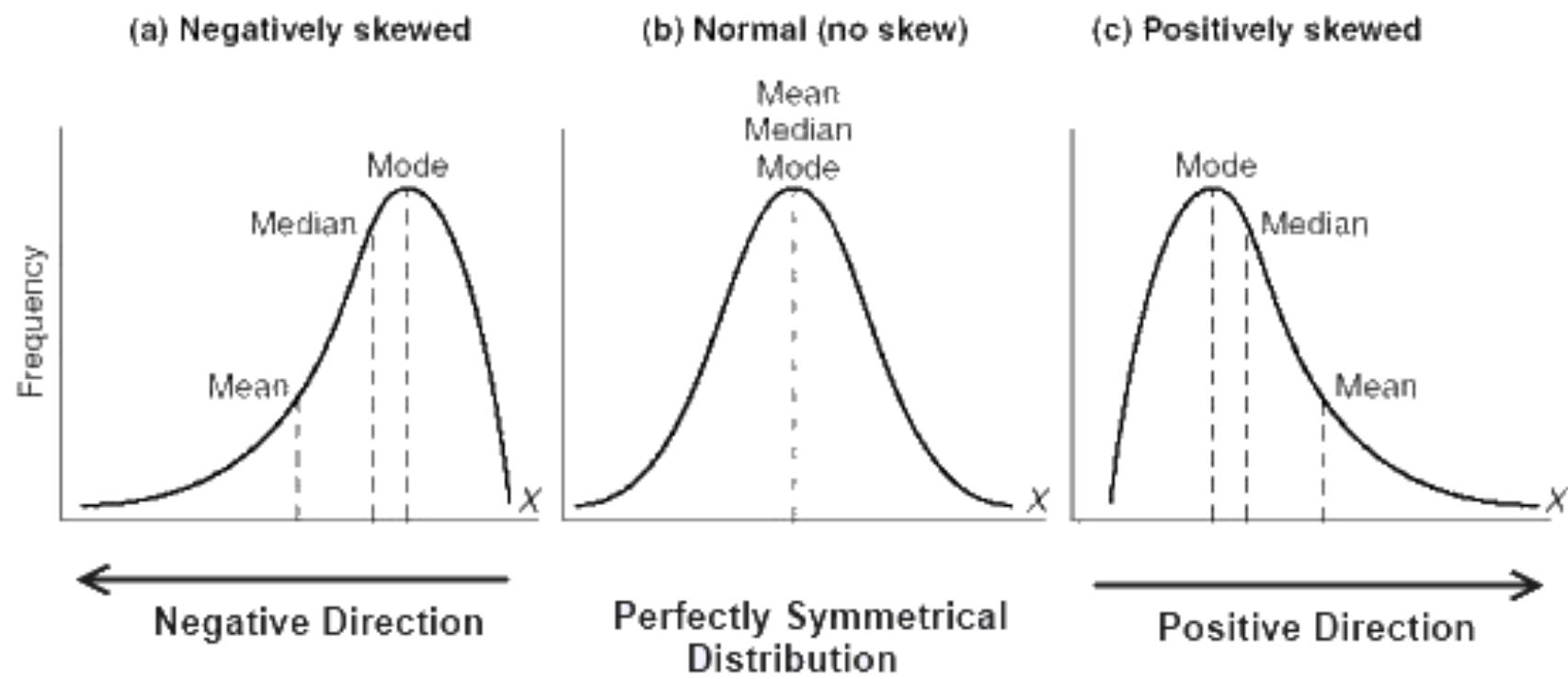
CENTRAL TENDENCY



CENTRAL TENDENCY



CENTRAL TENDENCY

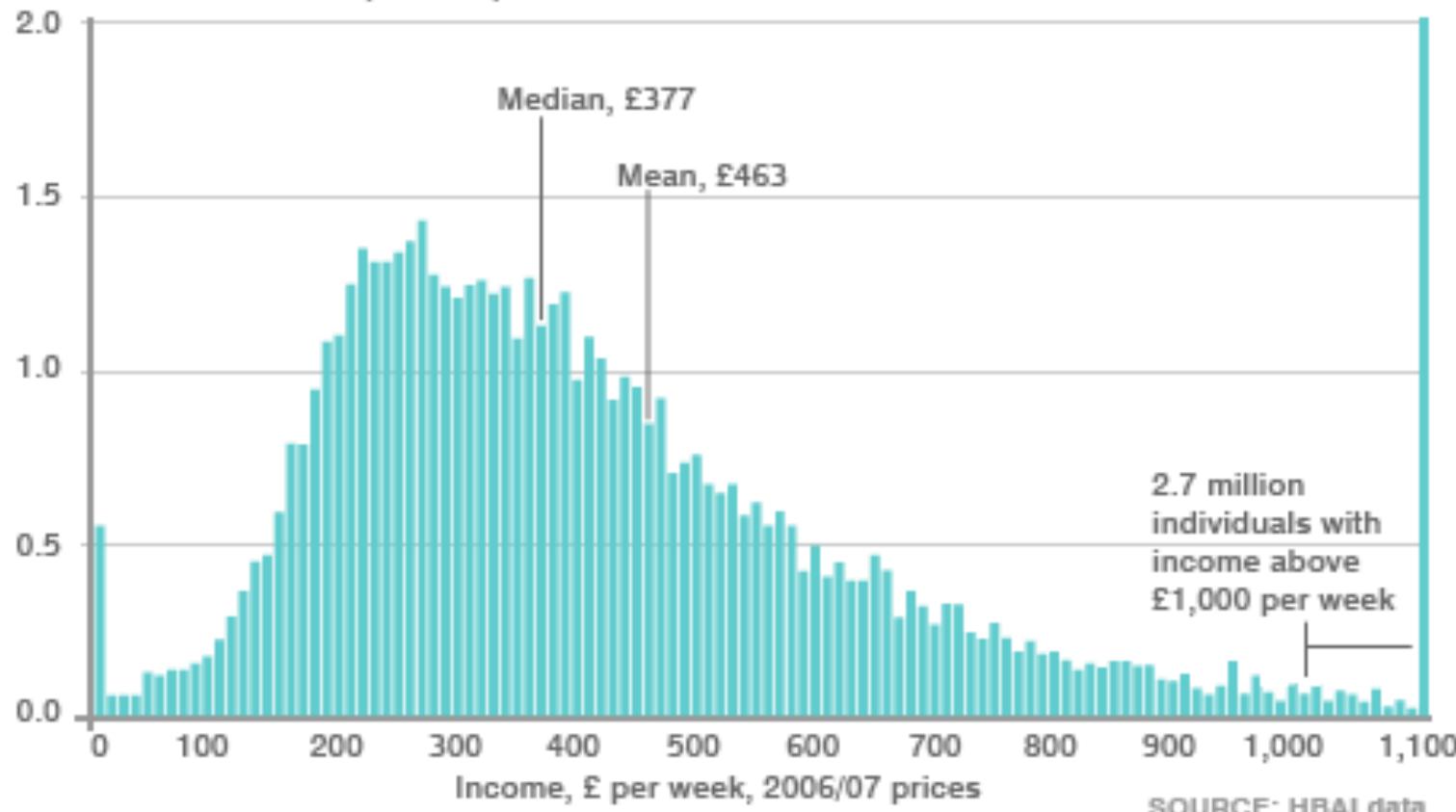


From Shreya Sethi

CENTRAL TENDENCY

THE UK INCOME DISTRIBUTION IN 2006 / 7

Number of individuals (millions)



From Michael Blastland

DISPERSION

Standard Deviation

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2}$$

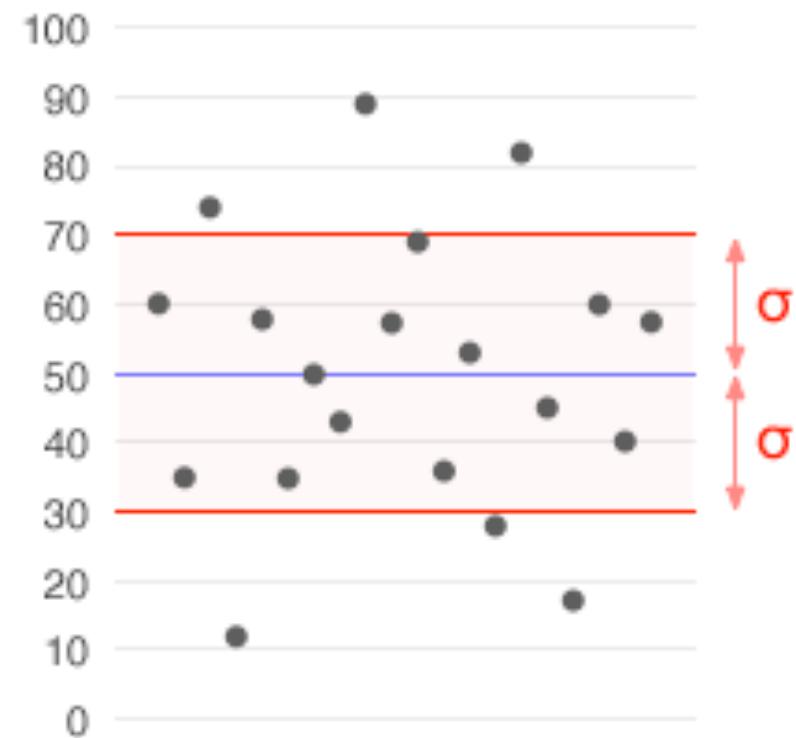
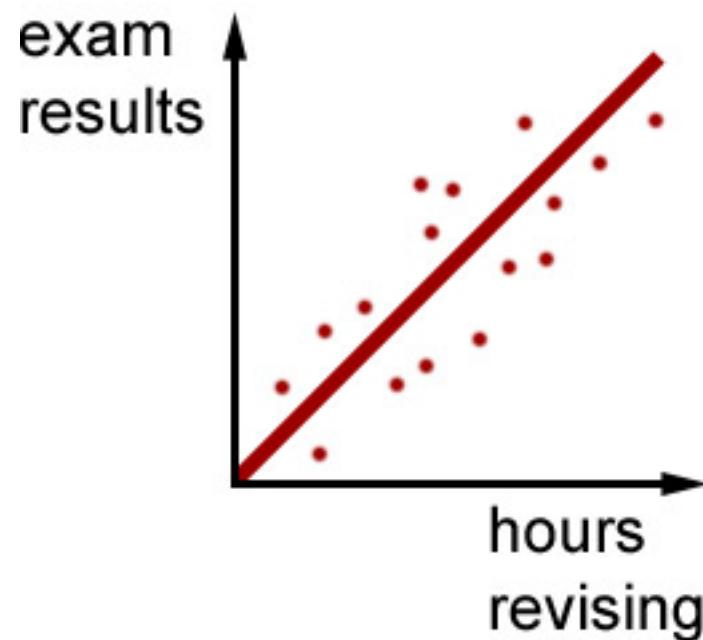


Image from Wikipedia

DEPENDENCE

- Correlation



POSITIVE CORRELATION

- people who do more revision get higher exam results.

Source unknown

DEPENDENCE

- Correlation

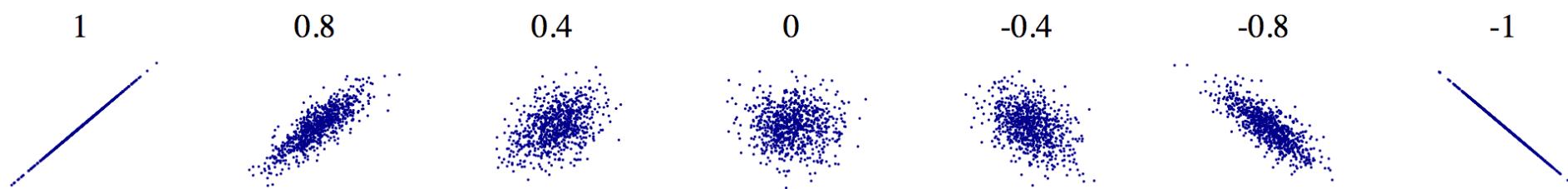
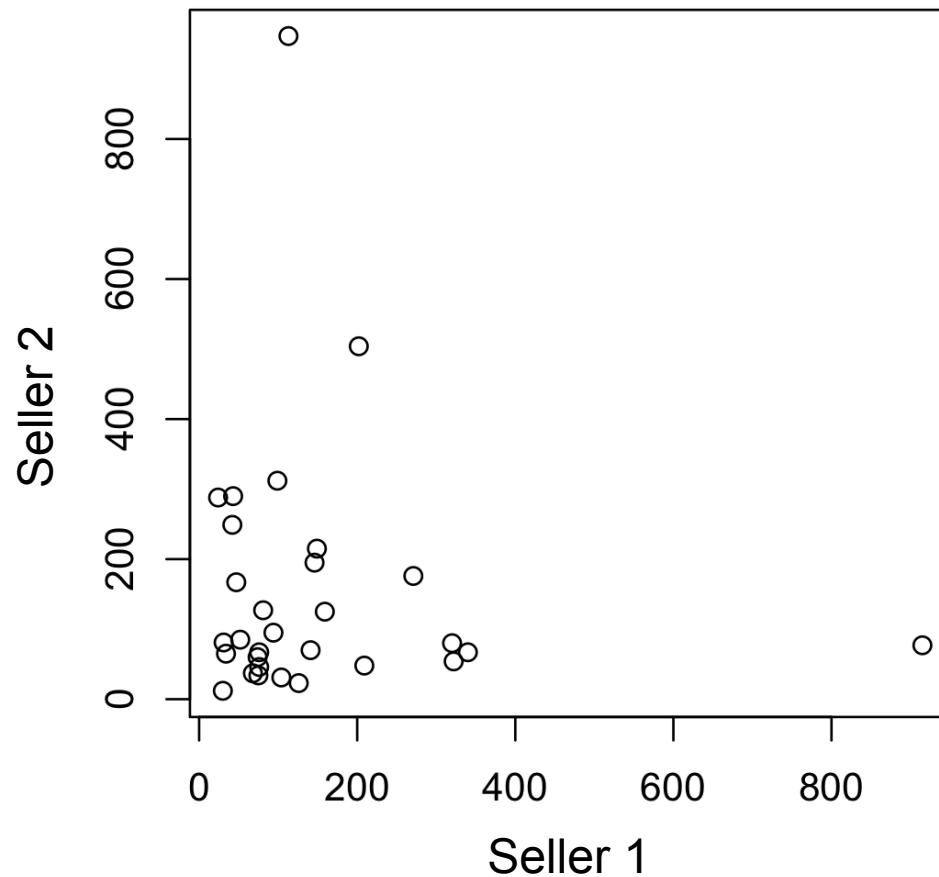


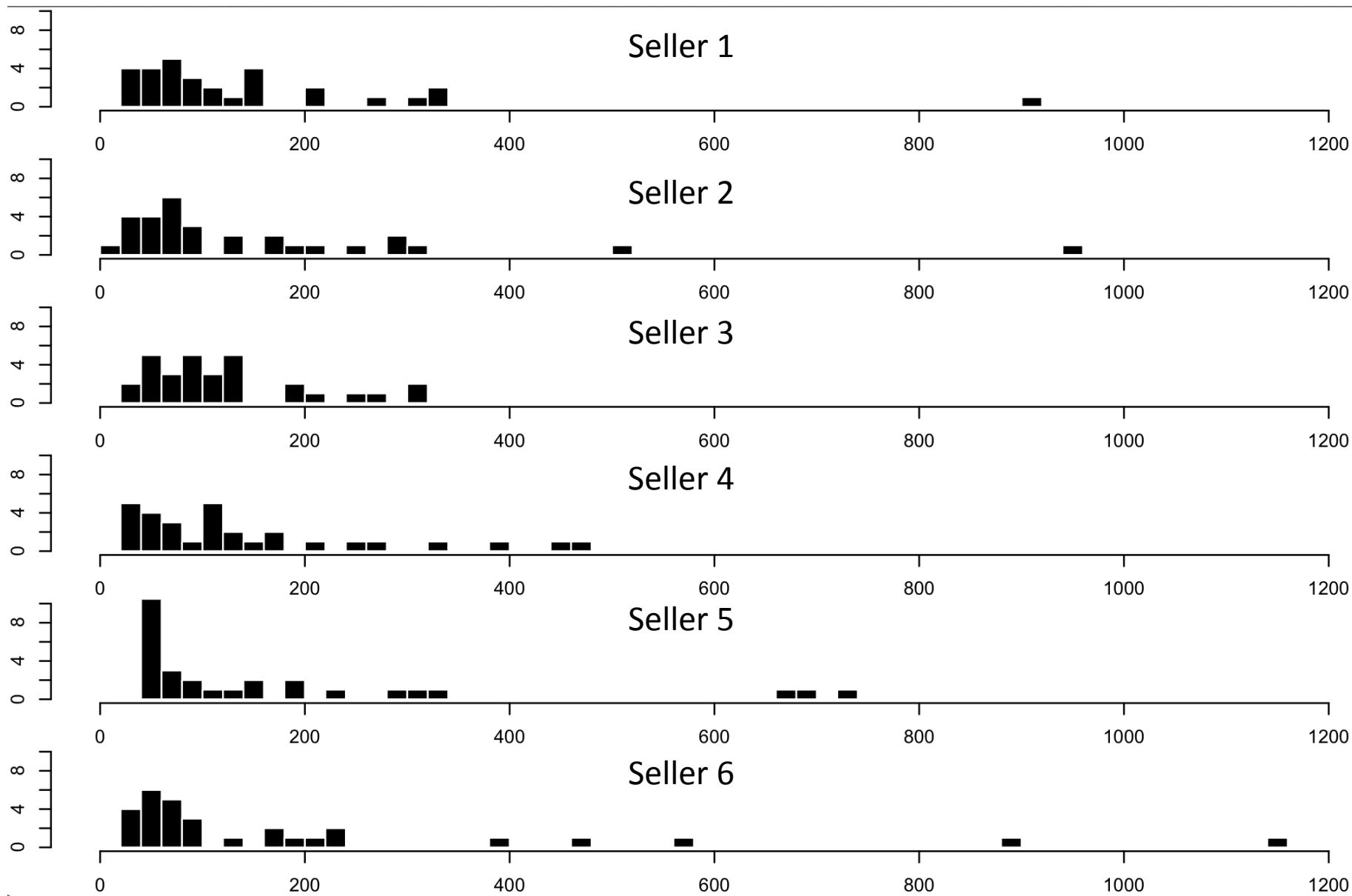
Image from Wikipedia

DEPENDENCE

- Correlation

$$r = -0.08$$



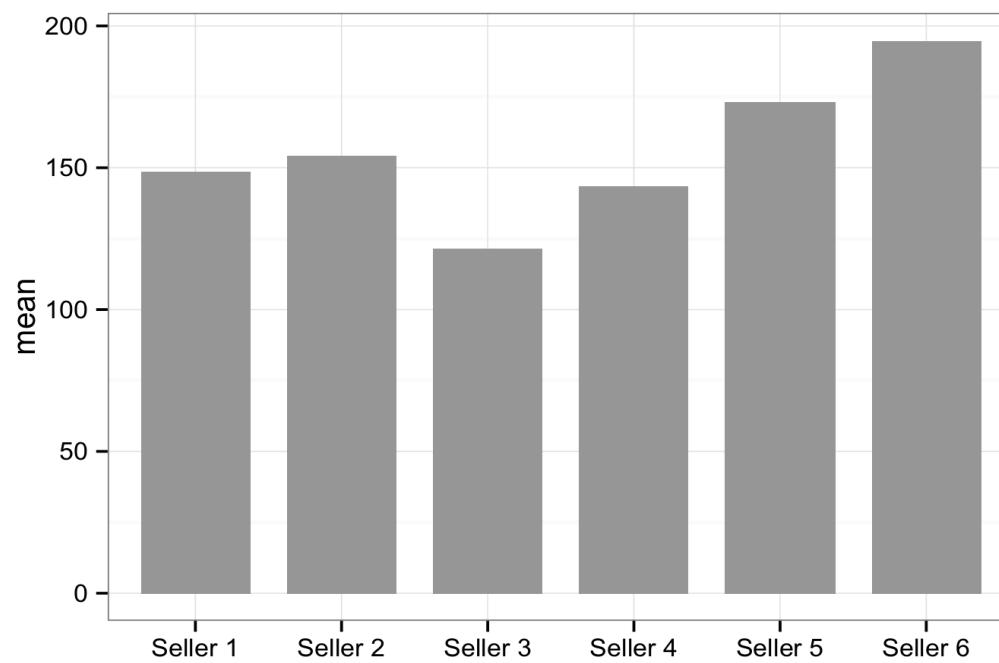


Average Sales

Seller 1	Seller 2	Seller 3	Seller 4	Seller 5	Seller 6
€149	€154	€122	€143	€173	€195

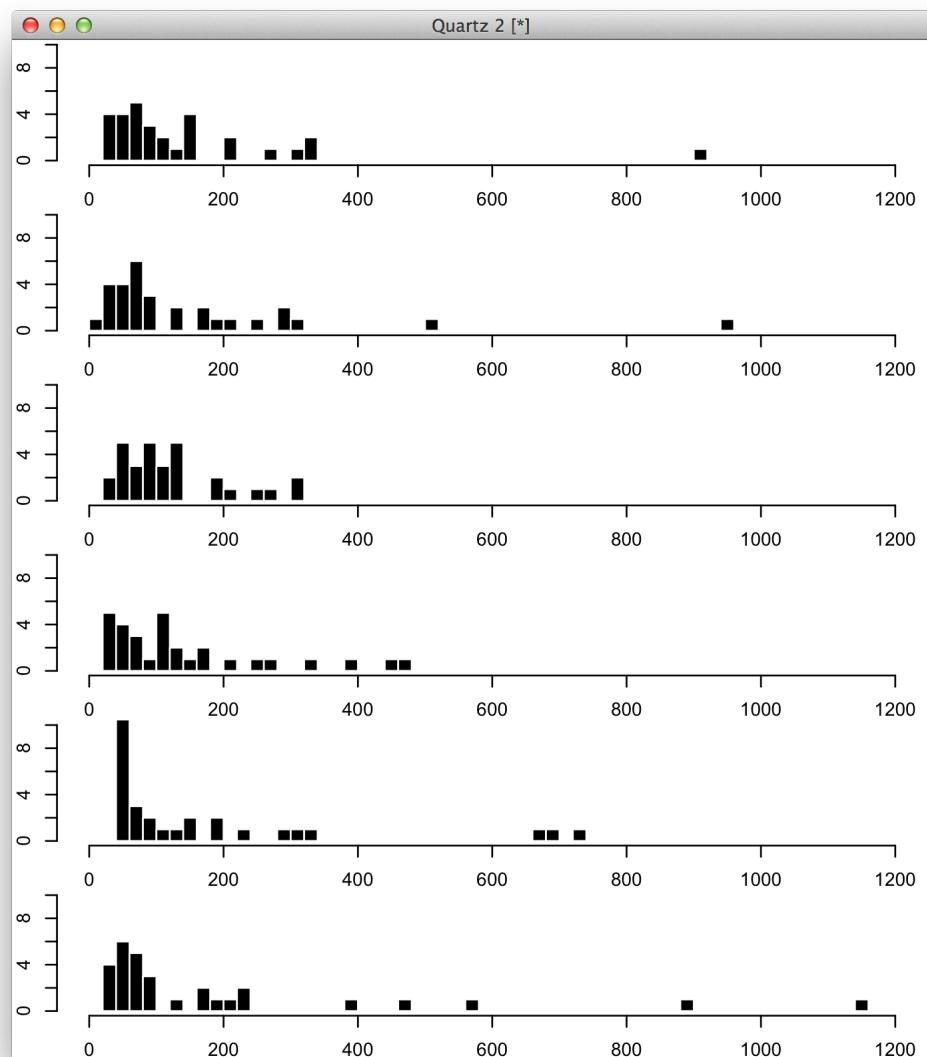
Average Sales

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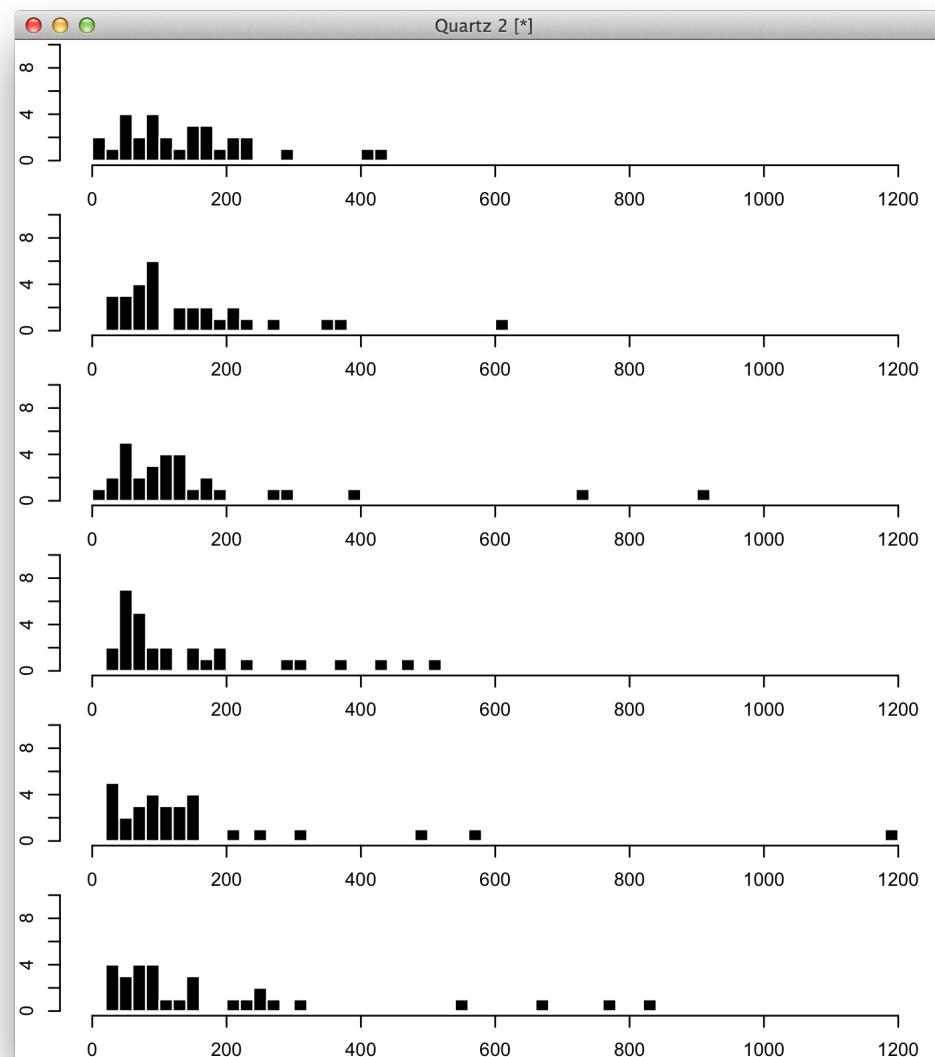


LOOKING INTO THE FUTURE

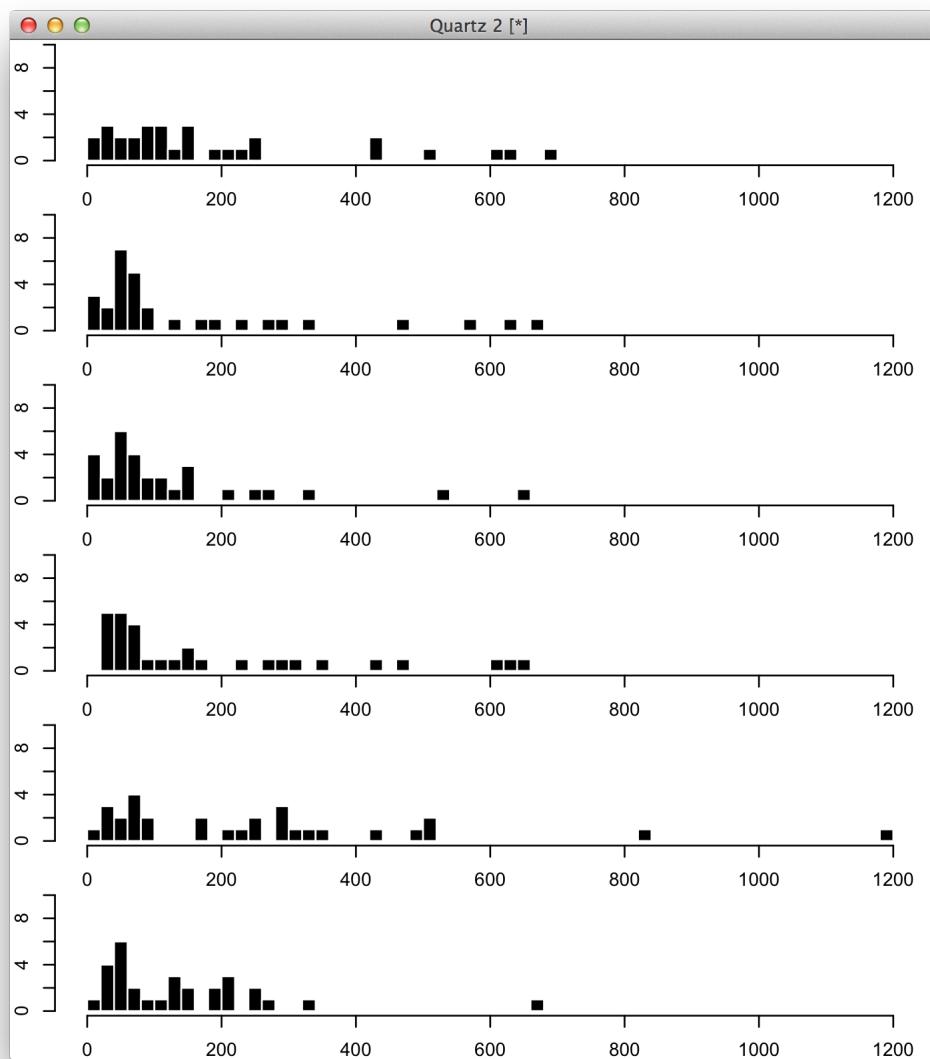
September 2014



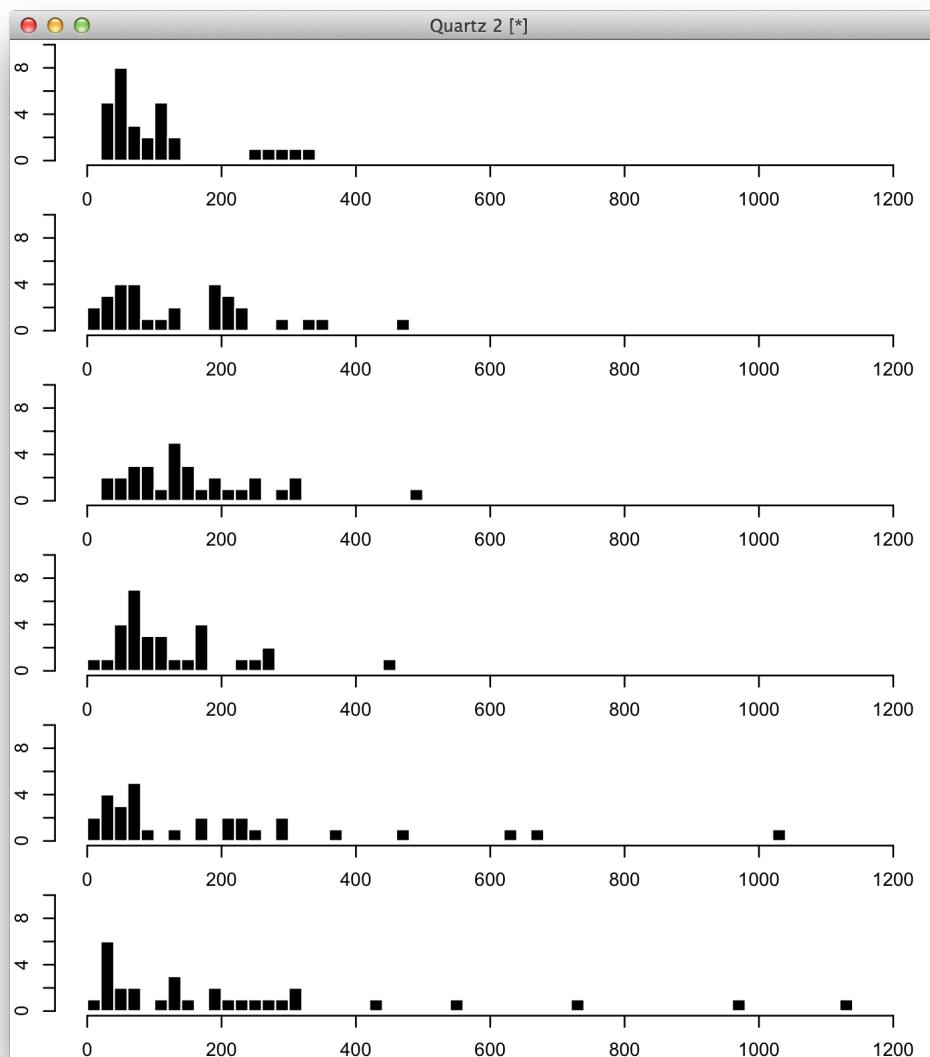
October 2014



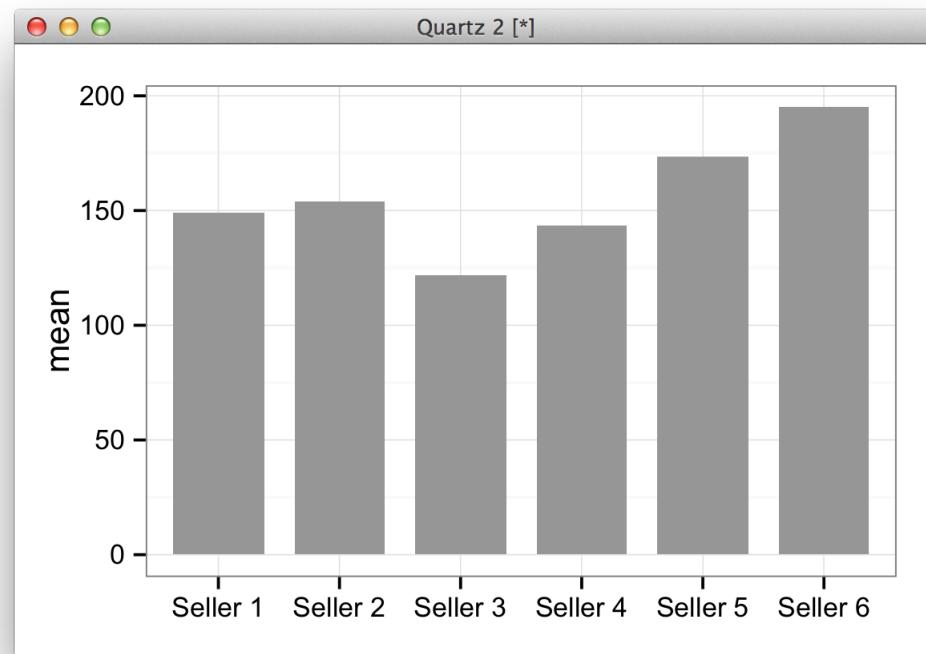
November 2014



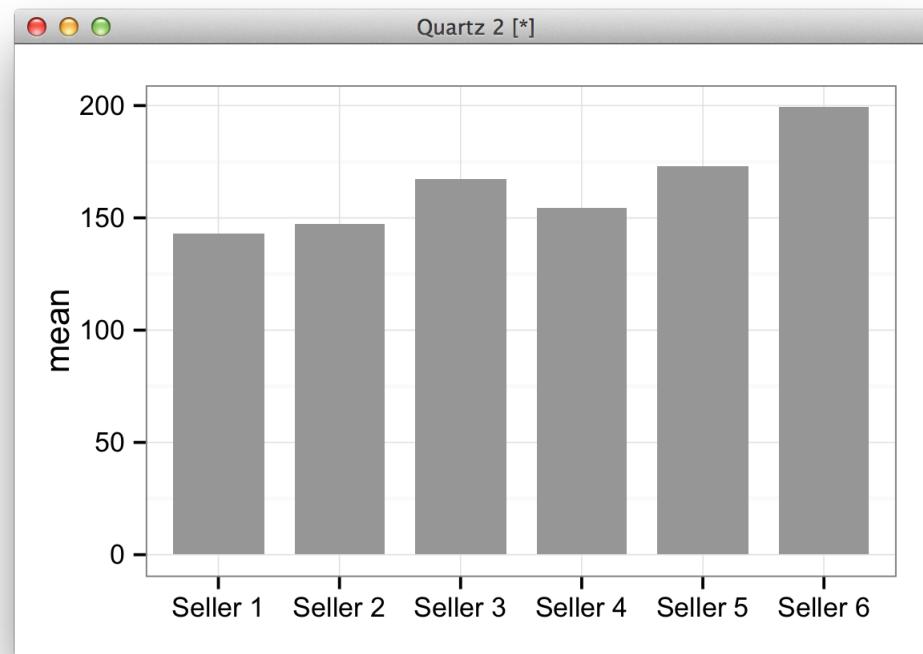
december 2014



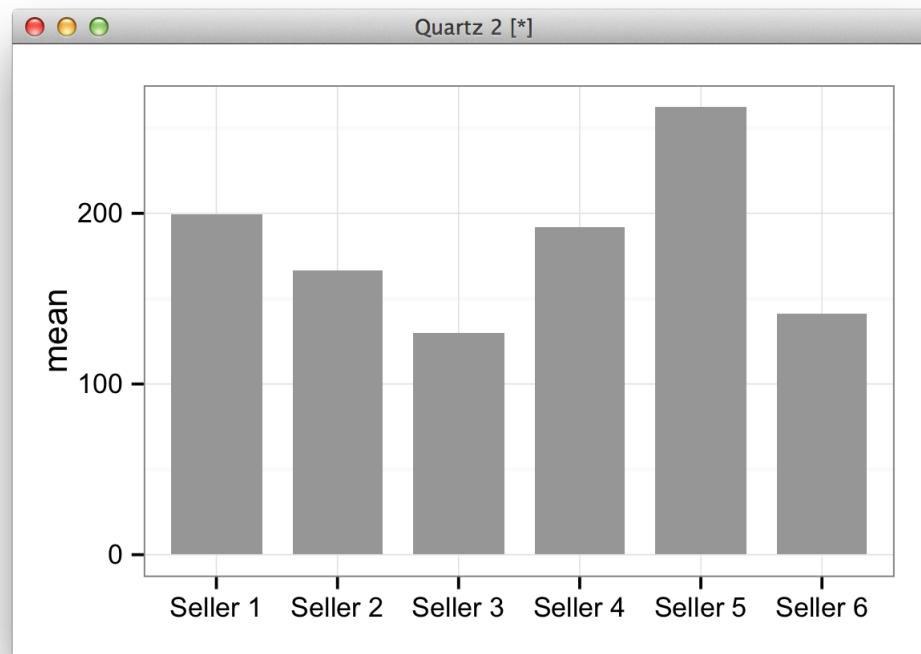
September 2014



October 2014



November 2014



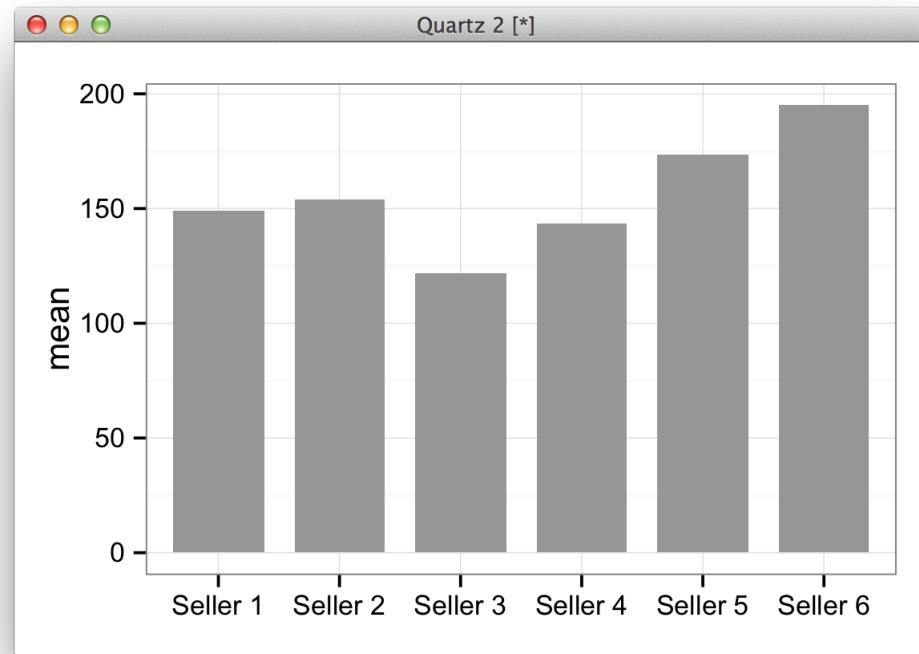
December 2014



September 2014

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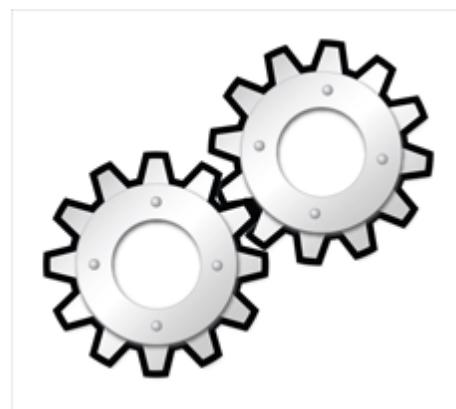
September 2014



How much can we trust this chart?

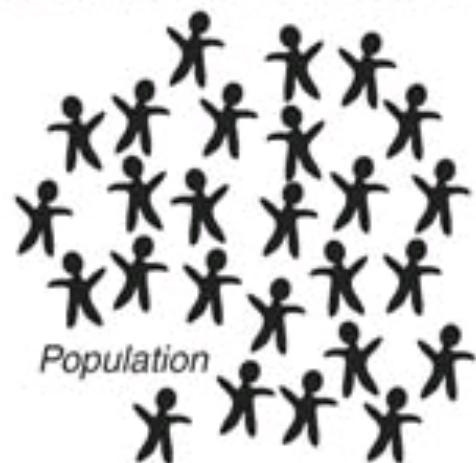
STATISTICAL TOOLS

INFERENTIAL STATISTICS



SAMPLING ERROR

We want to know about these



Parameter

$$\mu$$

(Population mean)

We have these to work with

Random selection



Inference

$$\bar{x}$$

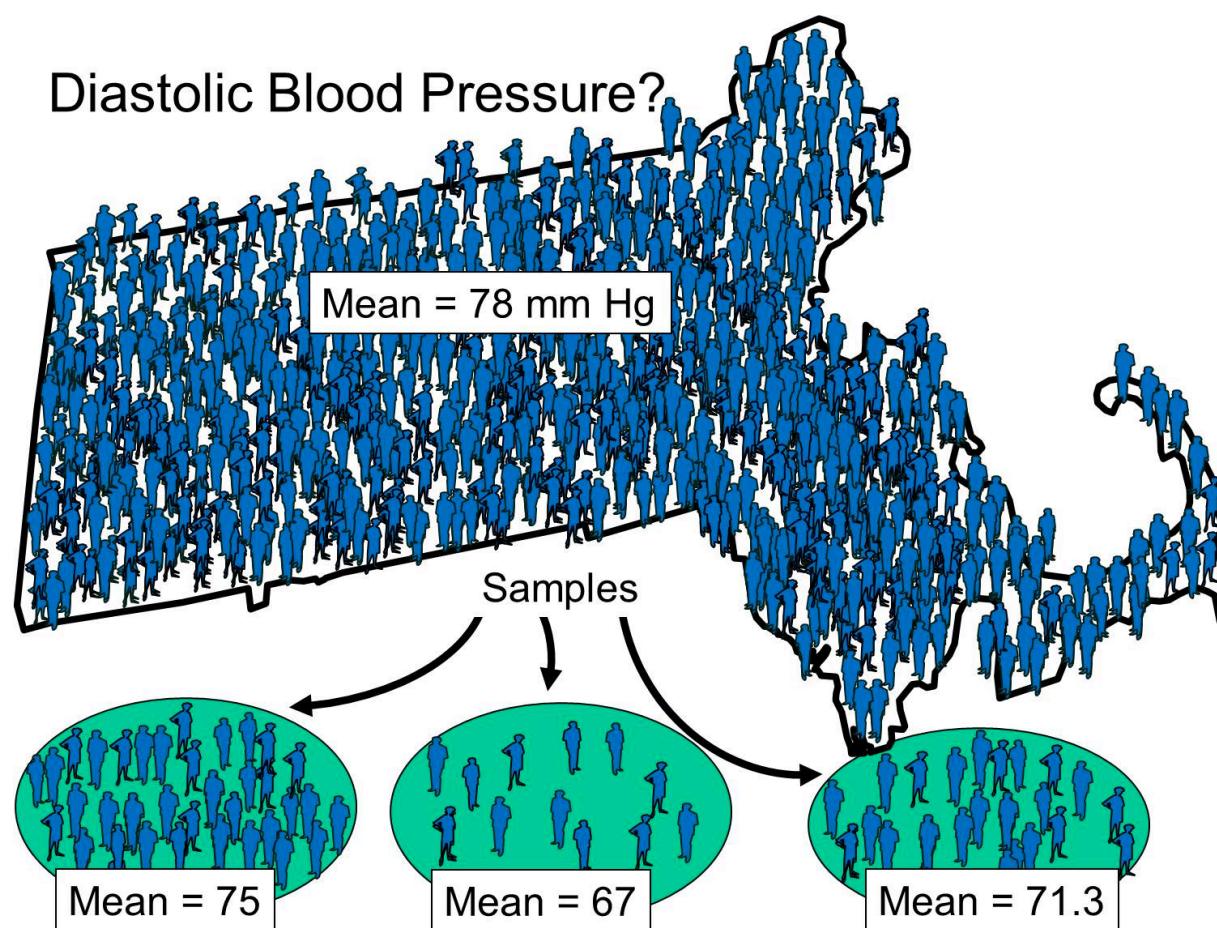
Statistic

(Sample mean)

SAMPLING ERROR

- Terminology:
 - Population vs. sample
 - Sample **statistic** (mean, median, etc.)
 - Population **parameter** (mean, median, etc.)

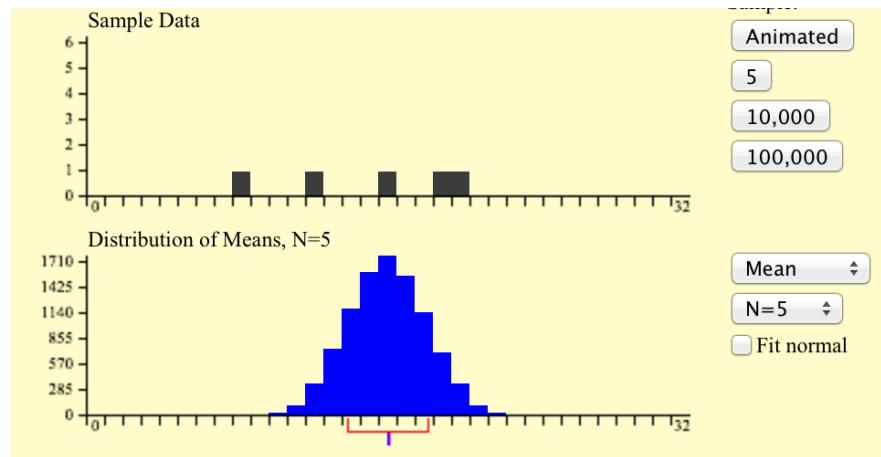
SAMPLING ERROR



From Lisa Sullivan

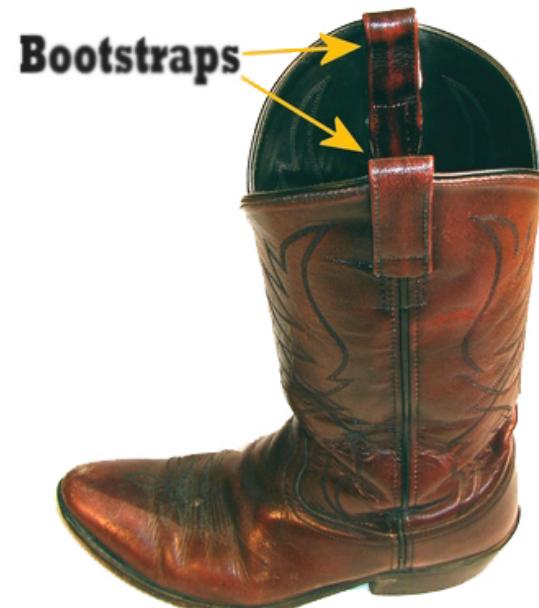
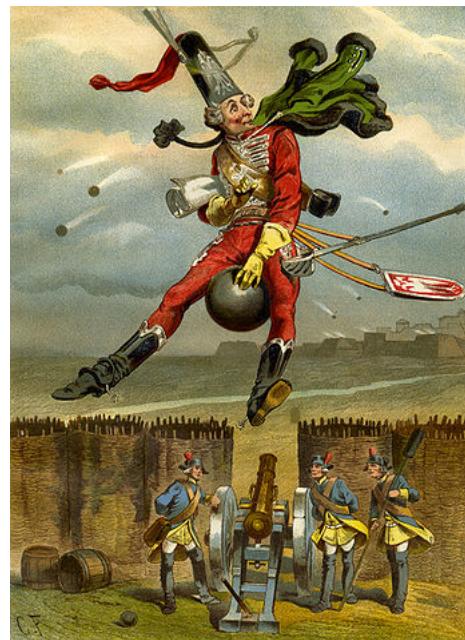
SAMPLING ERROR

- Sampling distribution of a statistic
 - Demo



SAMPLING ERROR

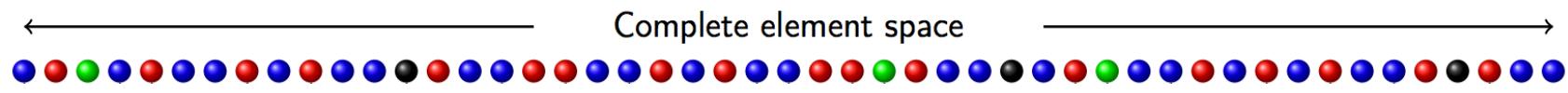
- Bootstrapping



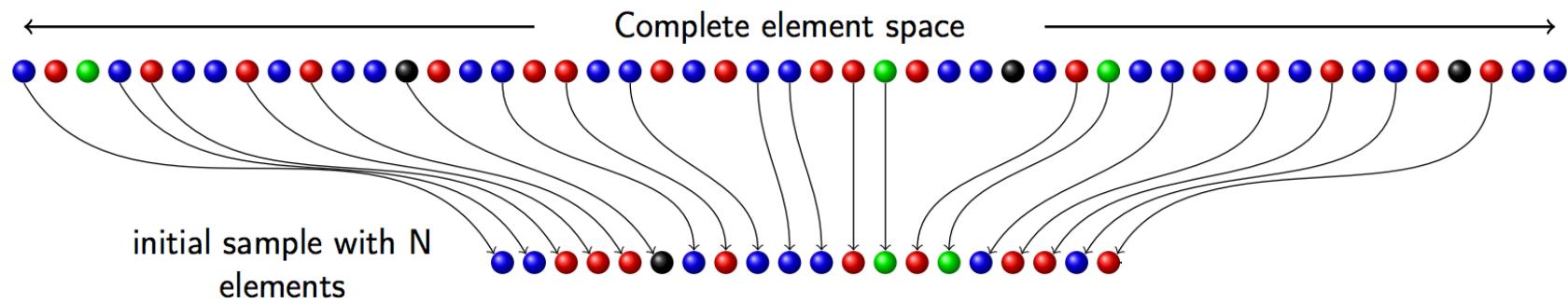
SAMPLING ERROR

- Bootstrapping

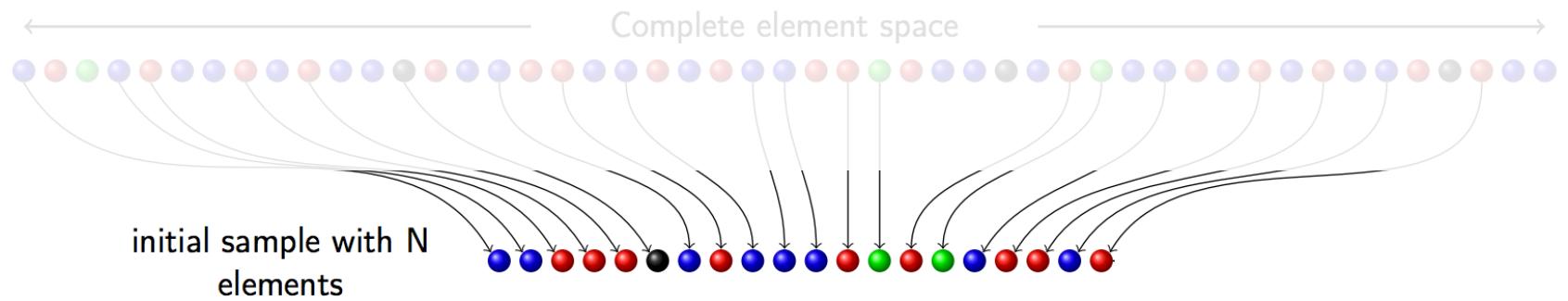




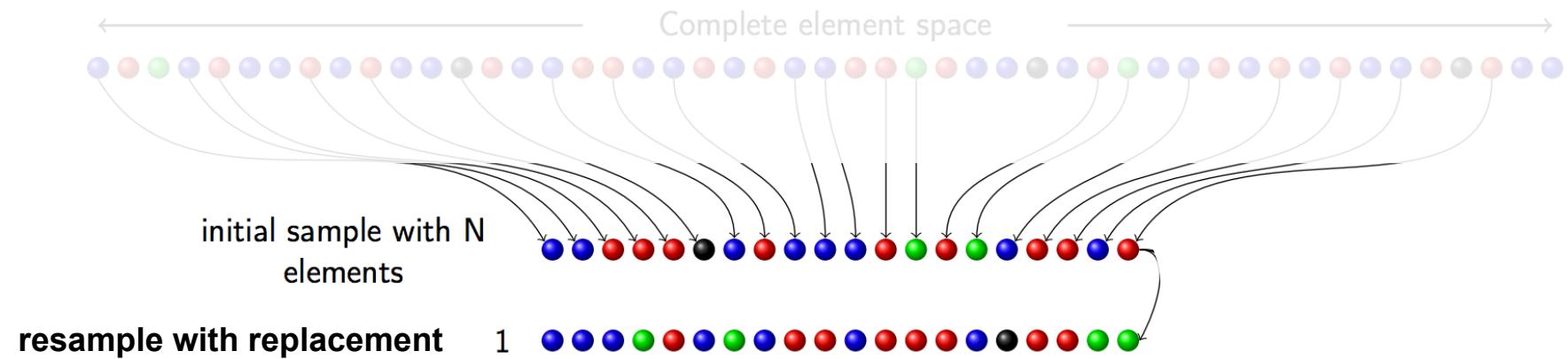
From Germain Salvato-Vallverdu



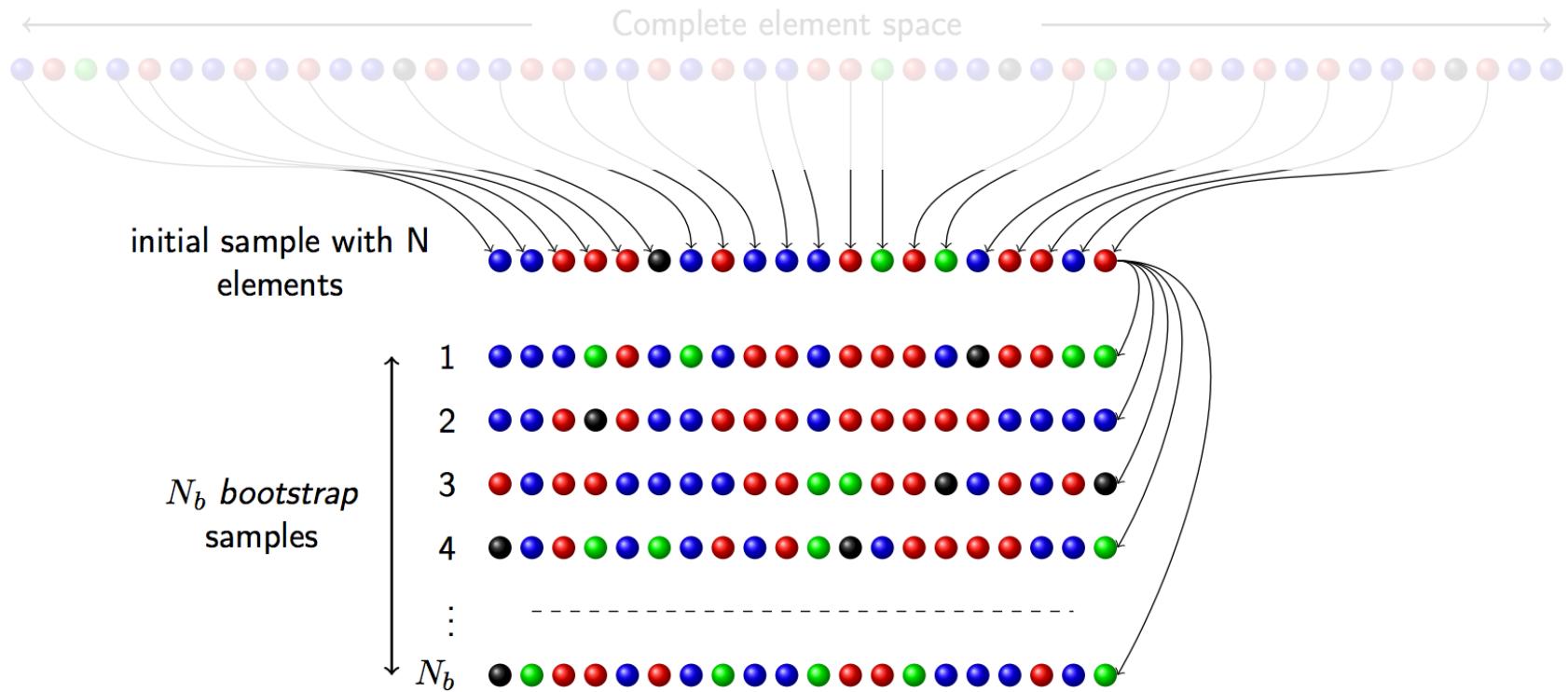
From Germain Salvato-Vallverdu



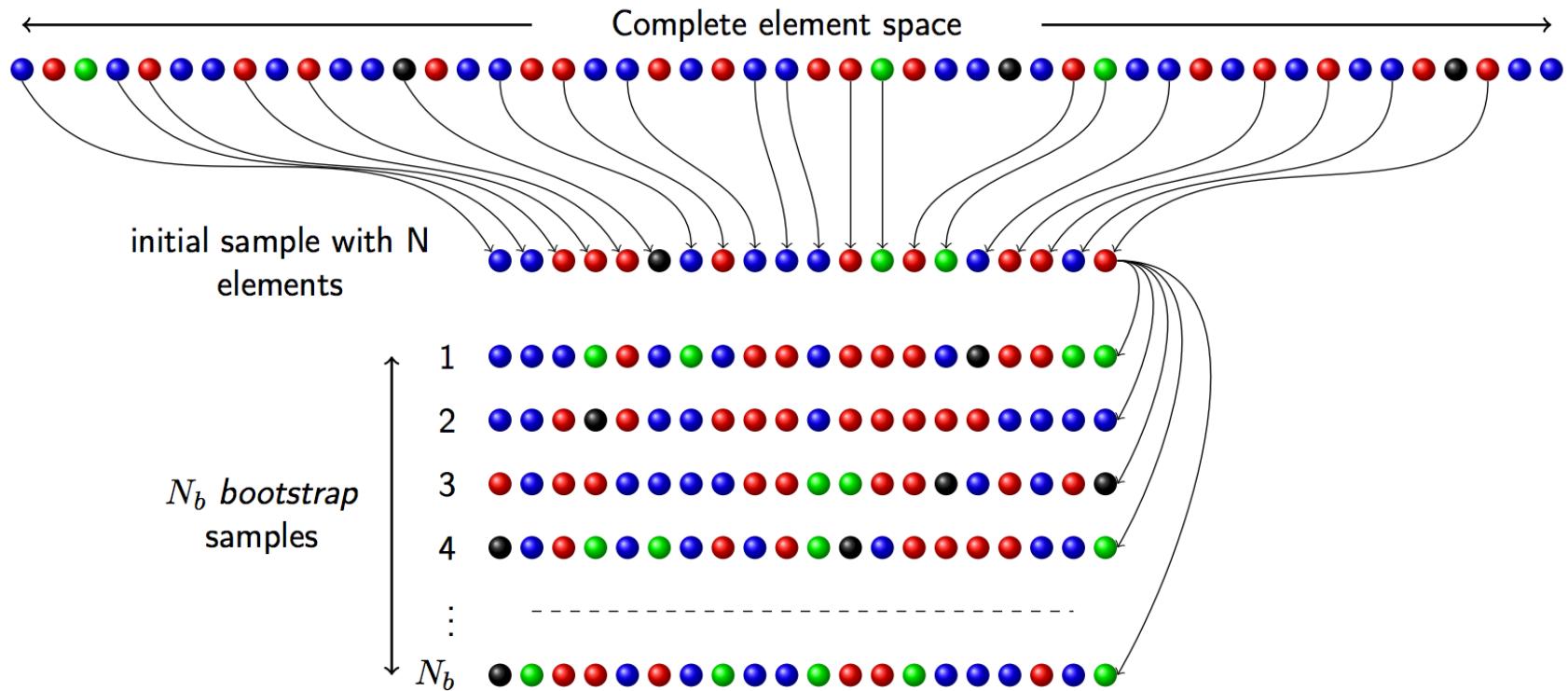
From Germain Salvato-Vallverdu



From Germain Salvato-Vallverdu



From Germain Salvato-Vallverdu



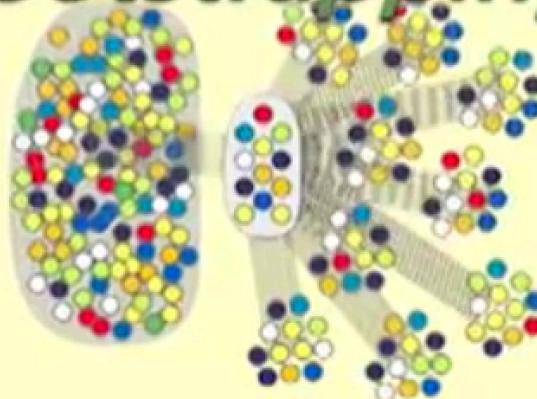
Theorem (B. Efron, Ann. Statist. 1979)

When N tend to infinity, the distribution of average values computed from bootstrap samples is equal to the distribution of average values obtained from ALL samples with N elements which can be constructed from the complete space. Thus the width of the distribution gives an evaluation of the sample quality.

SAMPLING ERROR

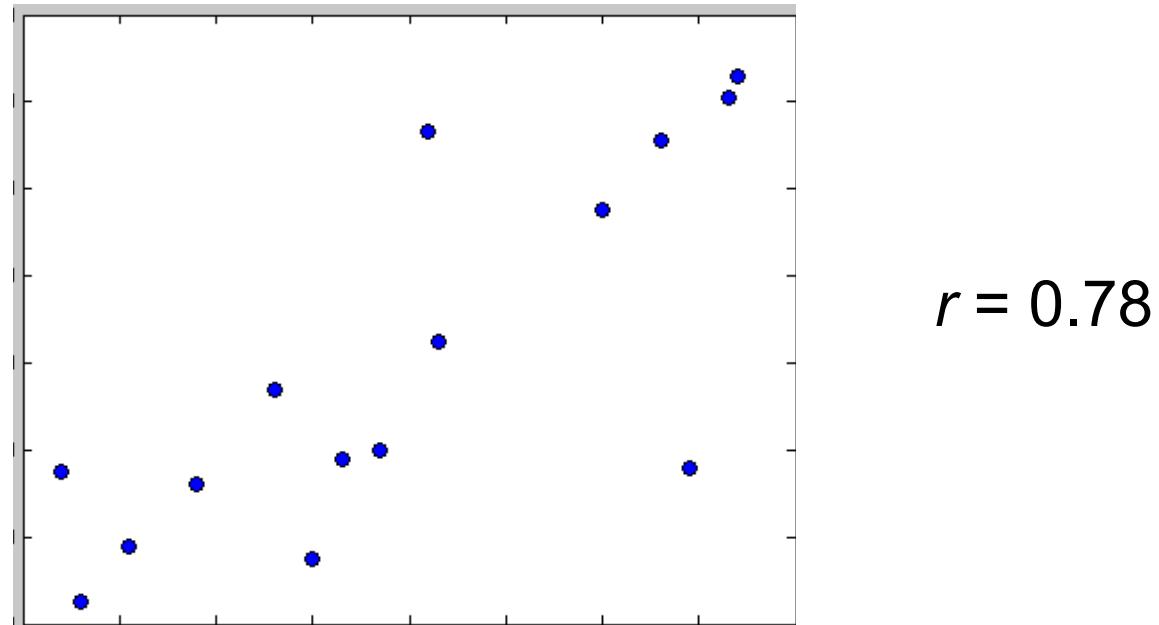
- Bootstrapping video

*Confidence
Intervals
Using
Bootstrapping*



SAMPLING ERROR

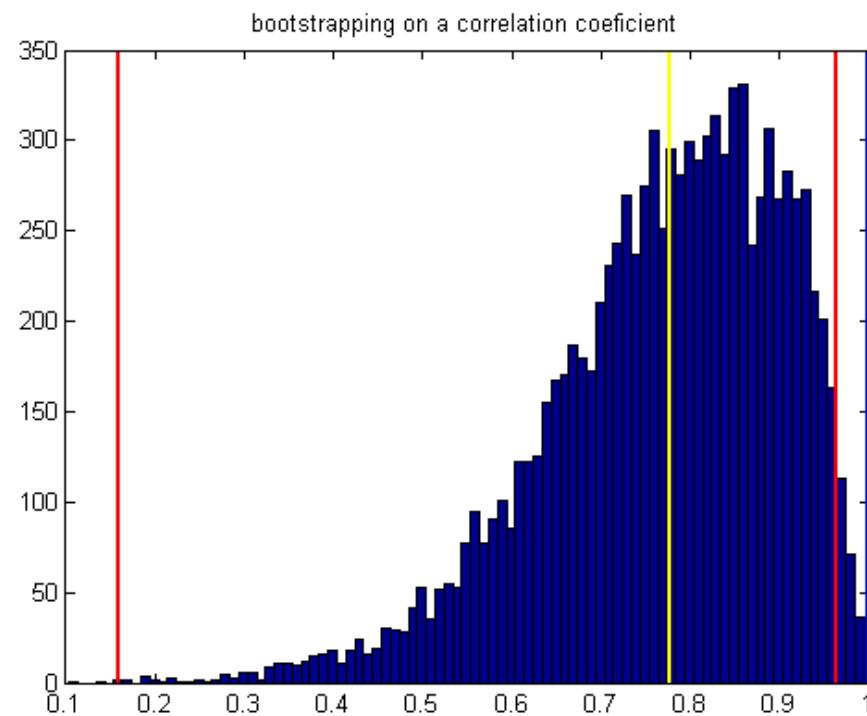
- Bootstrapping correlations



From lone Fine

SAMPLING ERROR

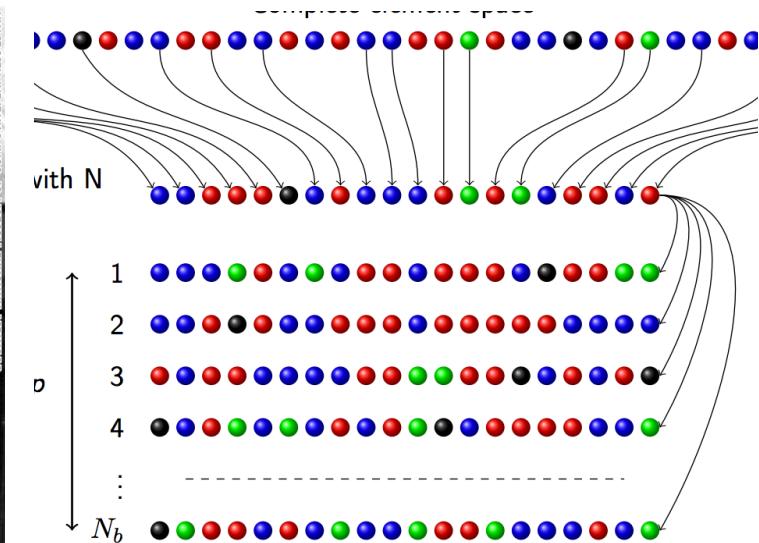
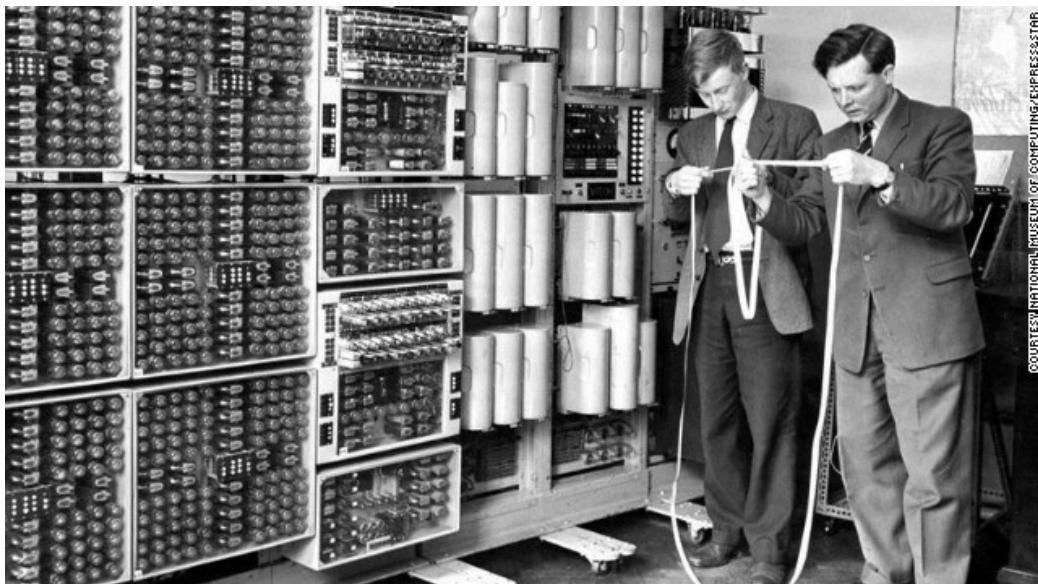
- Bootstrapping correlations



From lone Fine

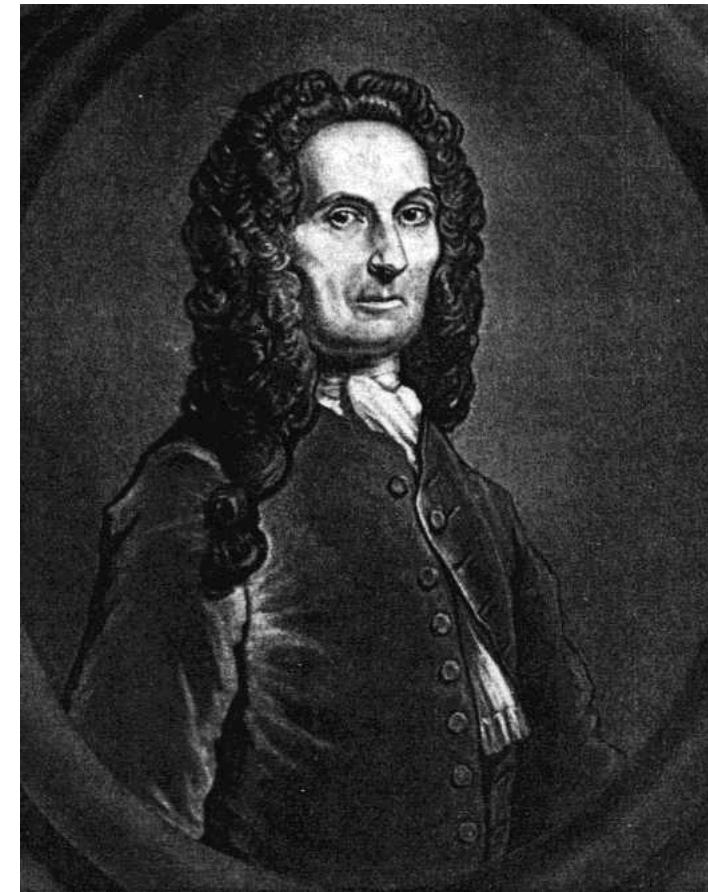
SAMPLING ERROR

- How did people do before computers?



MORE HISTORY

- Abraham De Moivre
1667 - 1754



MORE HISTORY

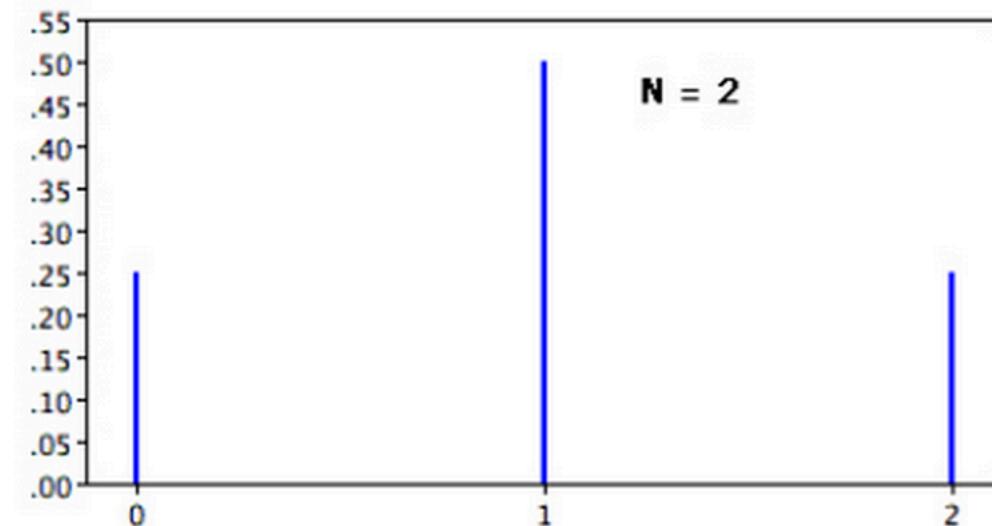
- Abraham De Moivre
1667 - 1754



MORE HISTORY

- Abraham De Moivre

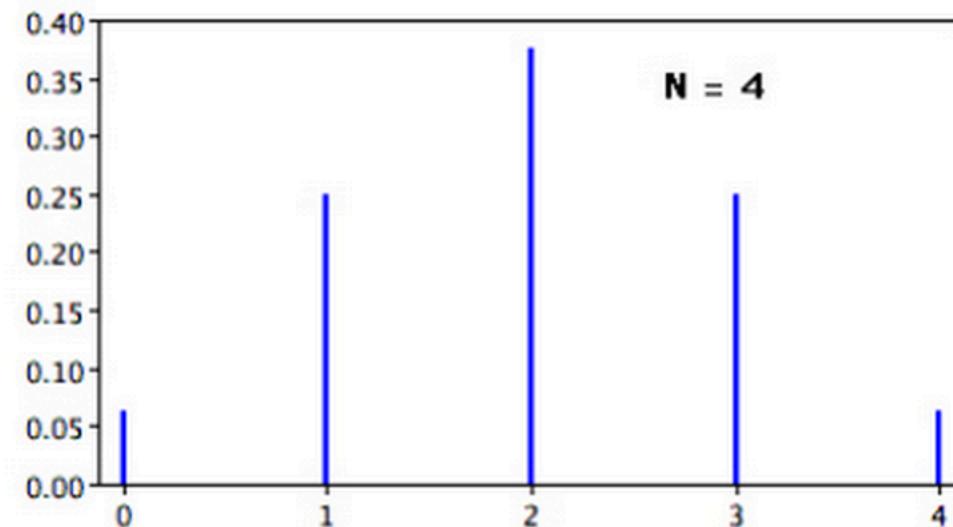
1667 - 1754



MORE HISTORY

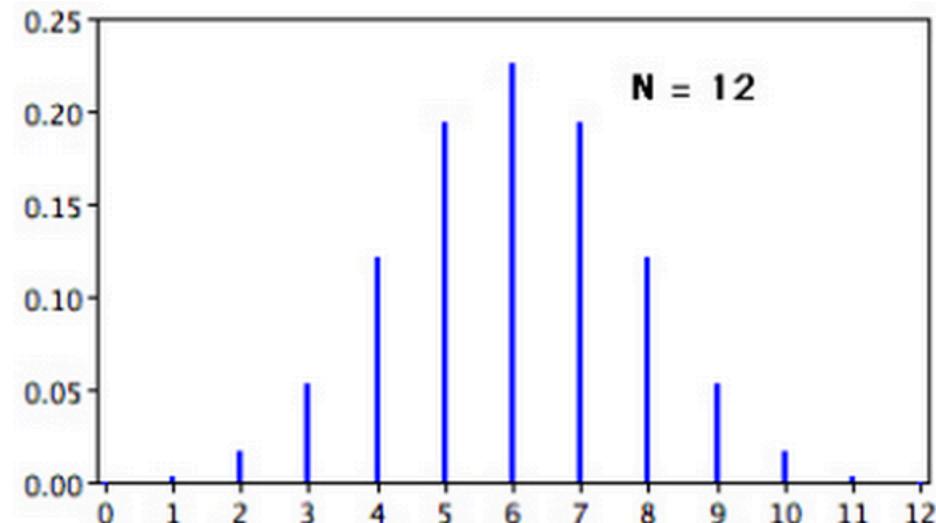
- Abraham De Moivre

1667 - 1754

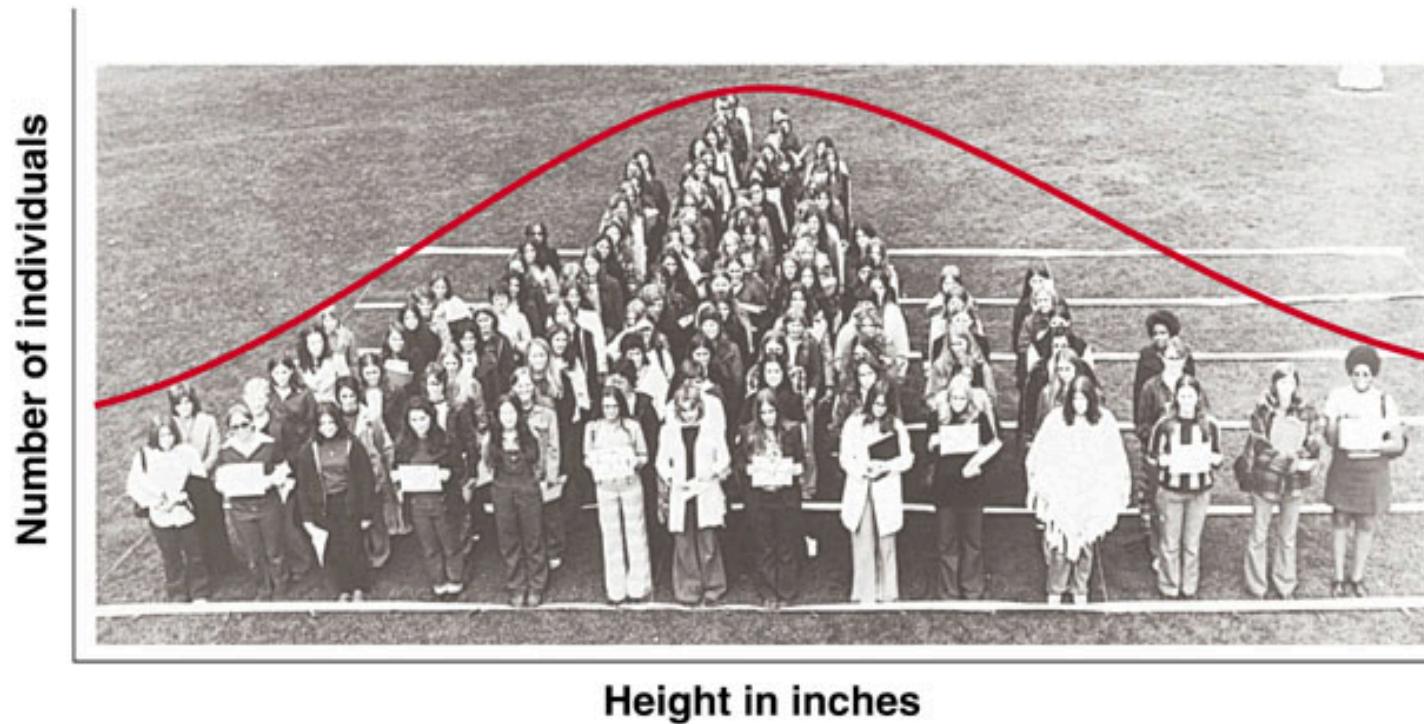


MORE HISTORY

- Abraham De Moivre
1667 - 1754

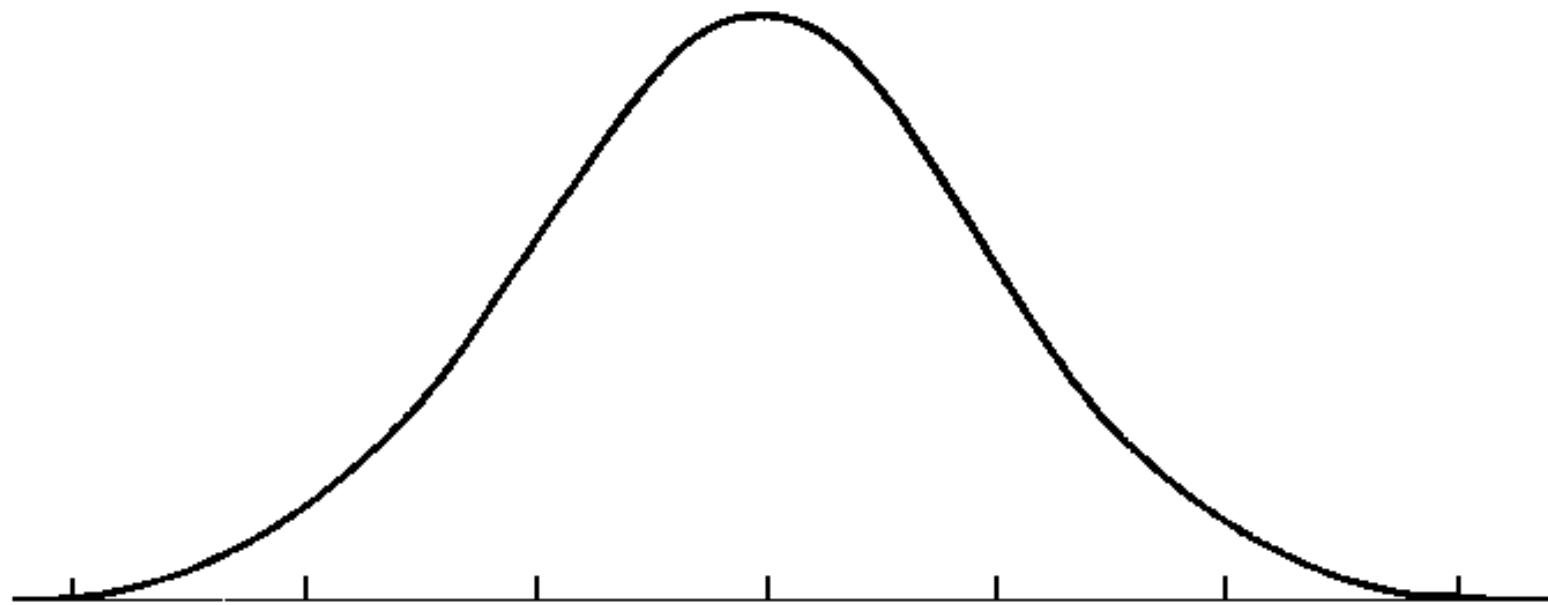


MORE HISTORY



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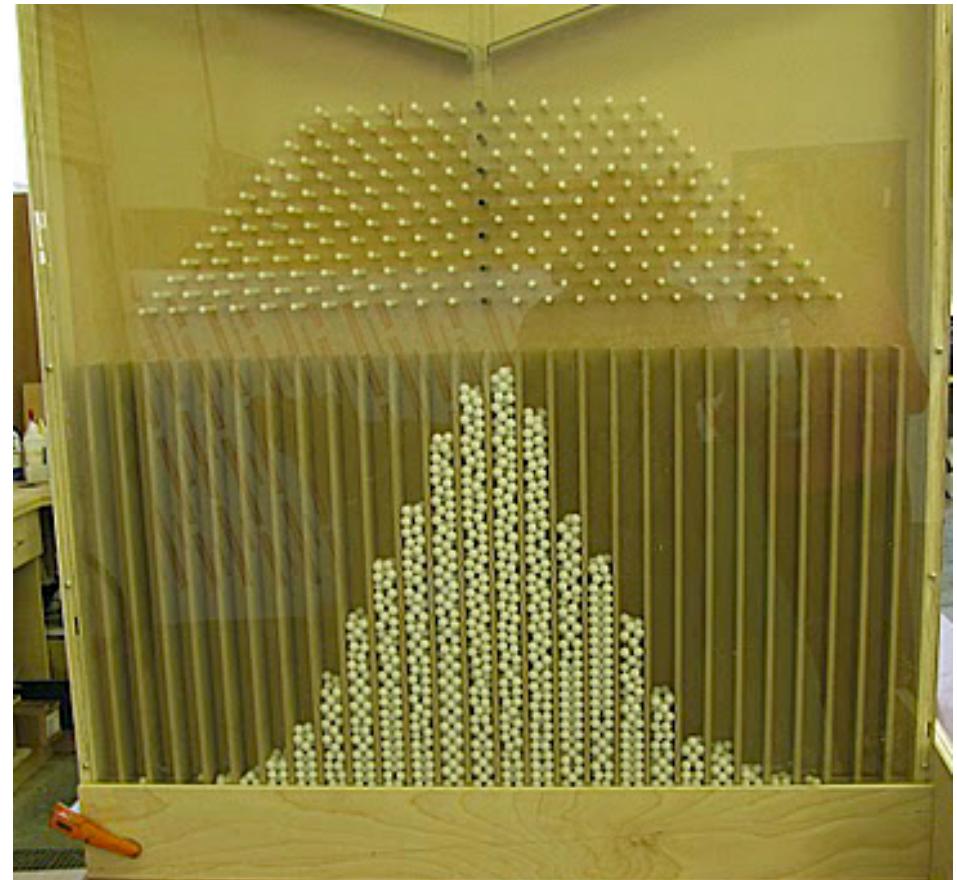
NORMAL DISTRIBUTION



NORMAL DISTRIBUTION

- Sir Francis Galton
1822 – 1911

Bean Machine
or Galton Board:



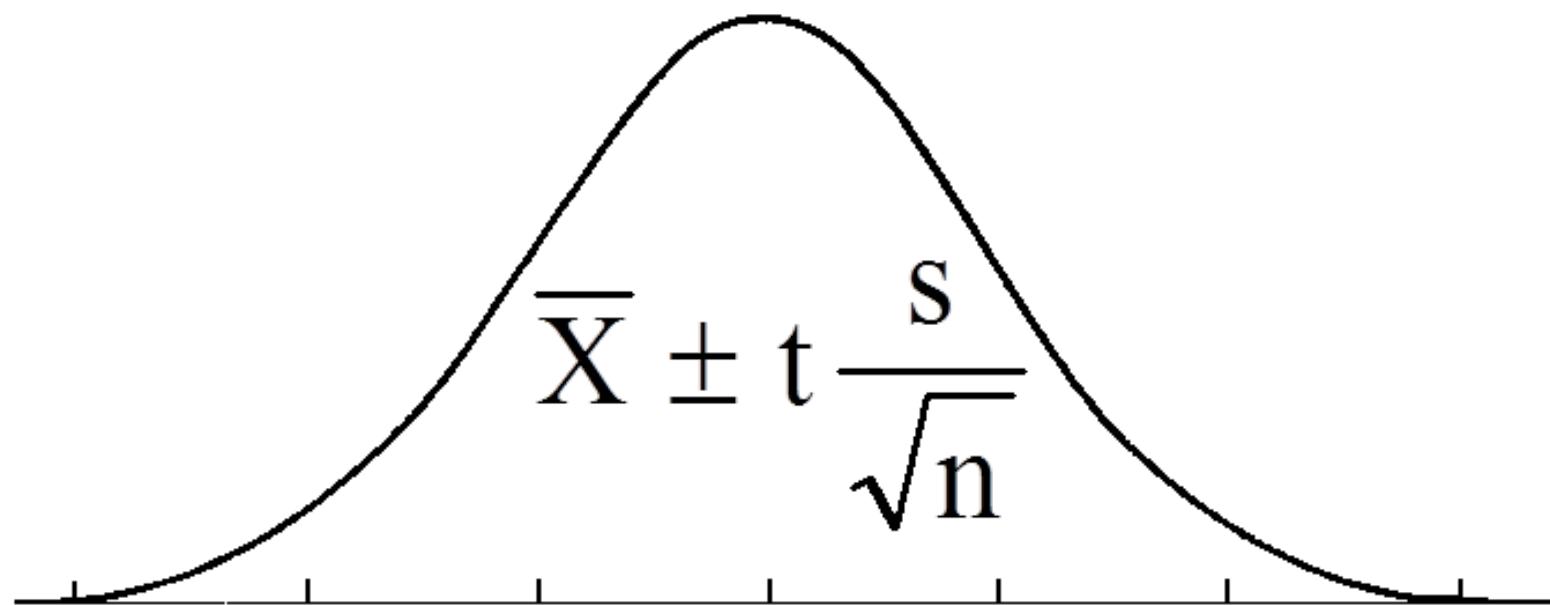
NORMAL DISTRIBUTION

Central Limit Theorem

Given certain conditions, the arithmetic mean of a sufficiently large number of iterates of independent random variables, each with a well-defined expected value and well-defined variance, will be approximately normally distributed

NORMAL DISTRIBUTION

“Exact” Confidence Intervals

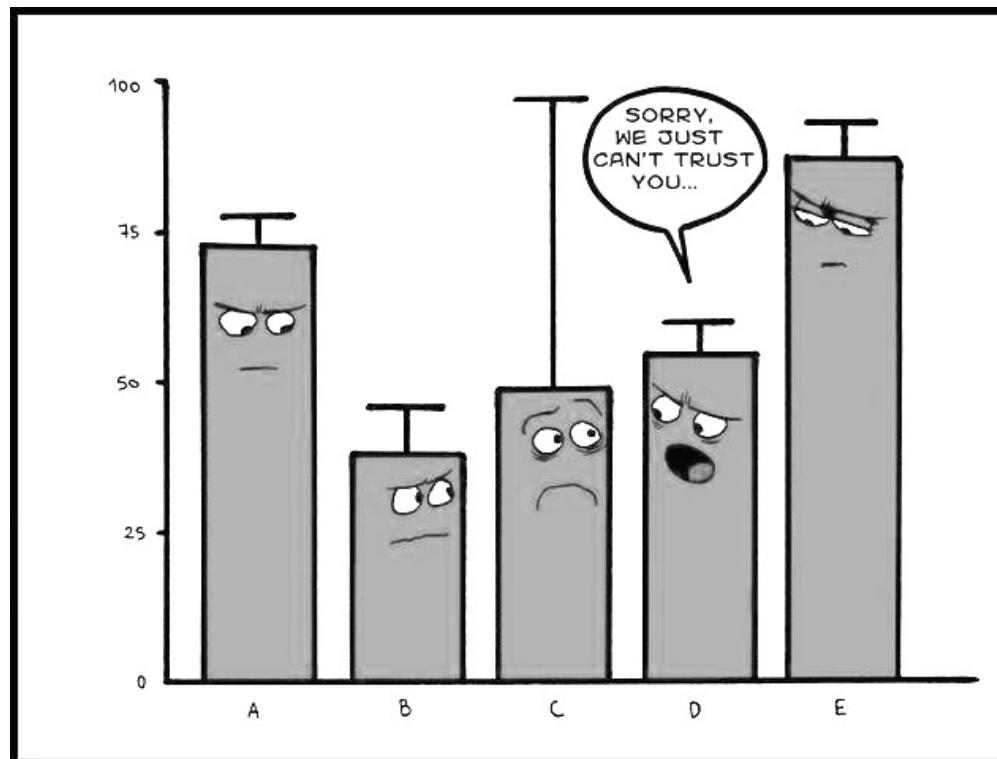


$t \sim 1.96$ for large samples

SAMPLING ERROR

- Terminology:
 - **Point estimate** = sample statistic = best guess
 - **Interval estimate** = other good guesses

CONFIDENCE INTERVALS



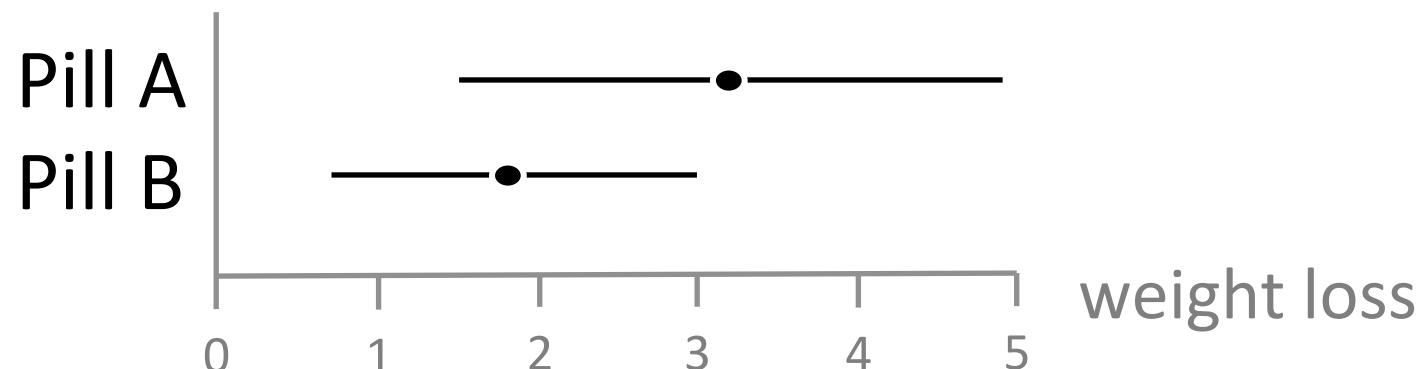
CONFIDENCE INTERVALS

- Several interpretations
- « *a range of plausible values for μ . Values outside the CI are relatively implausible.* »
(Cumming and Finch, 2005)
- Examples of presentation formats:
 - 2.2m, 95% CI [1.6m, 2.8m]
 - 2.2m +/- 0.6m
 - from 1.6m to 2.8m



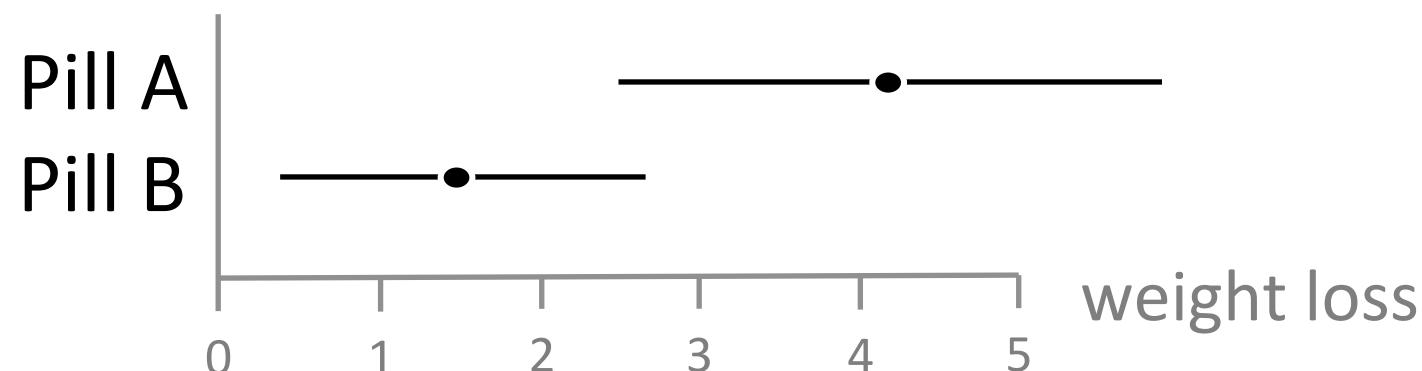
CONFIDENCE INTERVALS

- « a range of plausible values for μ . Values outside the CI are relatively implausible. »
(Cumming and Finch, 2005)



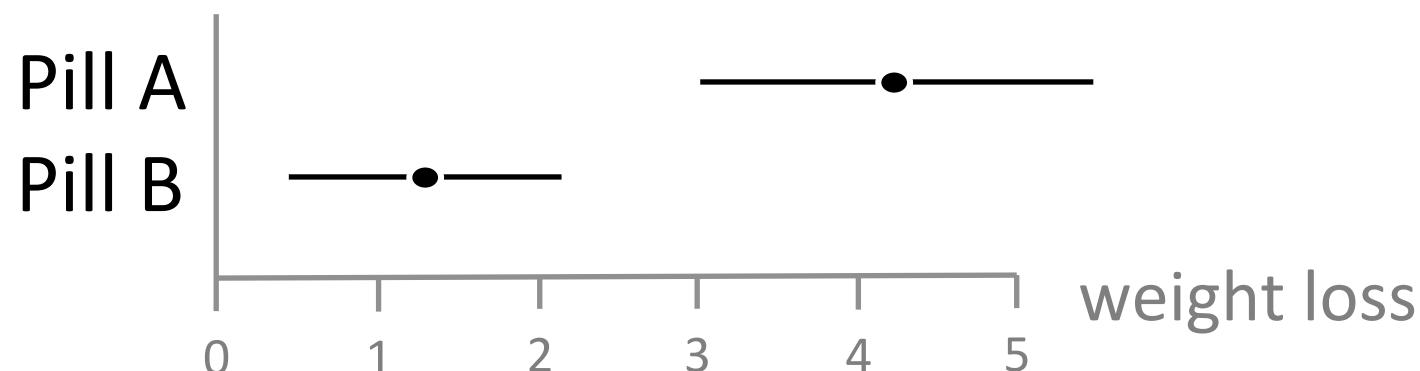
CONFIDENCE INTERVALS

- « a range of plausible values for μ . Values outside the CI are relatively implausible. »
(Cumming and Finch, 2005)



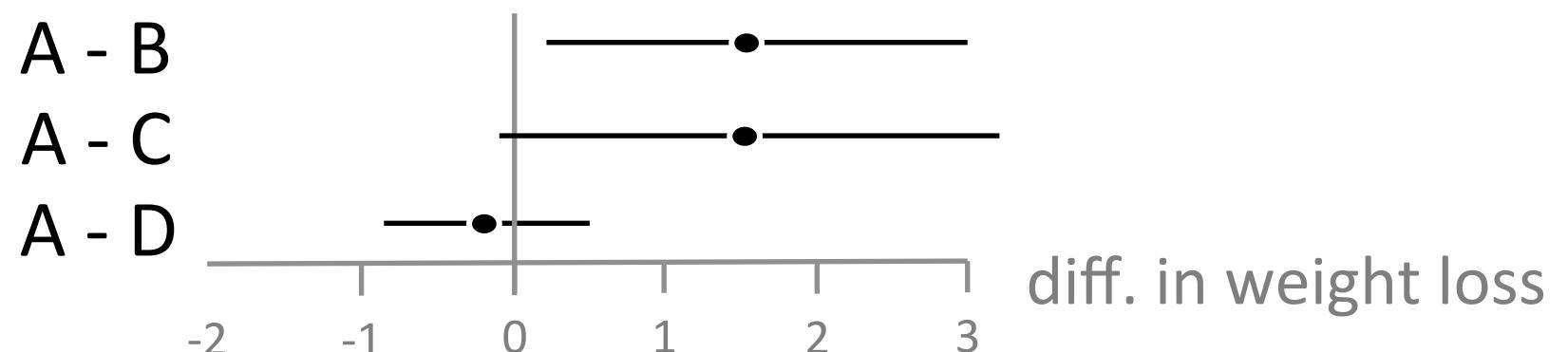
CONFIDENCE INTERVALS

- « a range of plausible values for μ . Values outside the CI are relatively implausible. »
(Cumming and Finch, 2005)



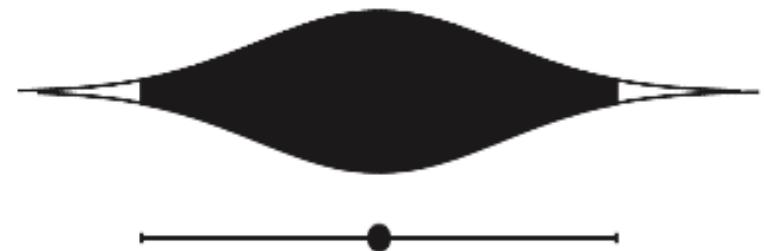
CONFIDENCE INTERVALS

- « a range of plausible values for μ . Values outside the CI are relatively implausible. »
(Cumming and Finch, 2005)



CONFIDENCE INTERVALS

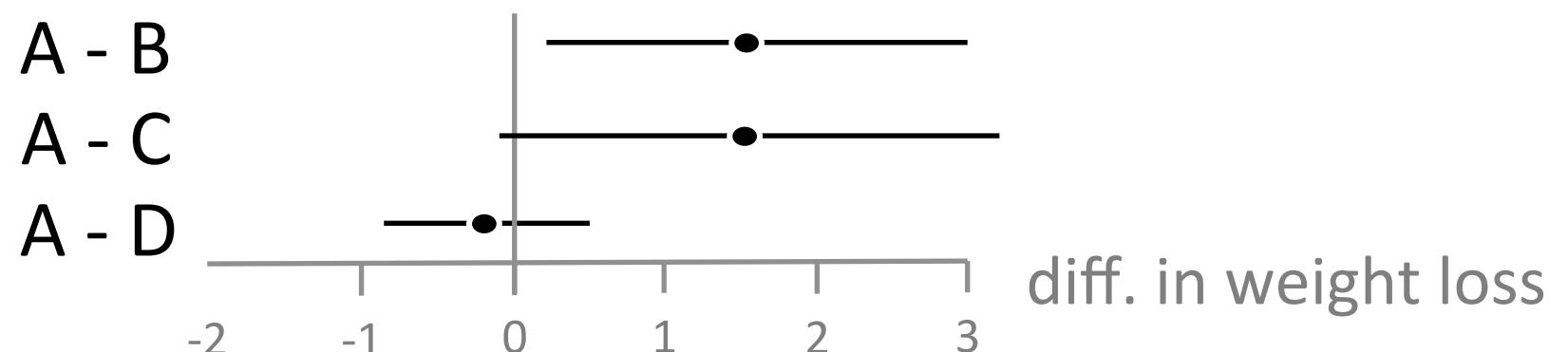
- “*values close to our M are the best bet for μ , and values closer to the limits of our CI are successively less good bets.*”



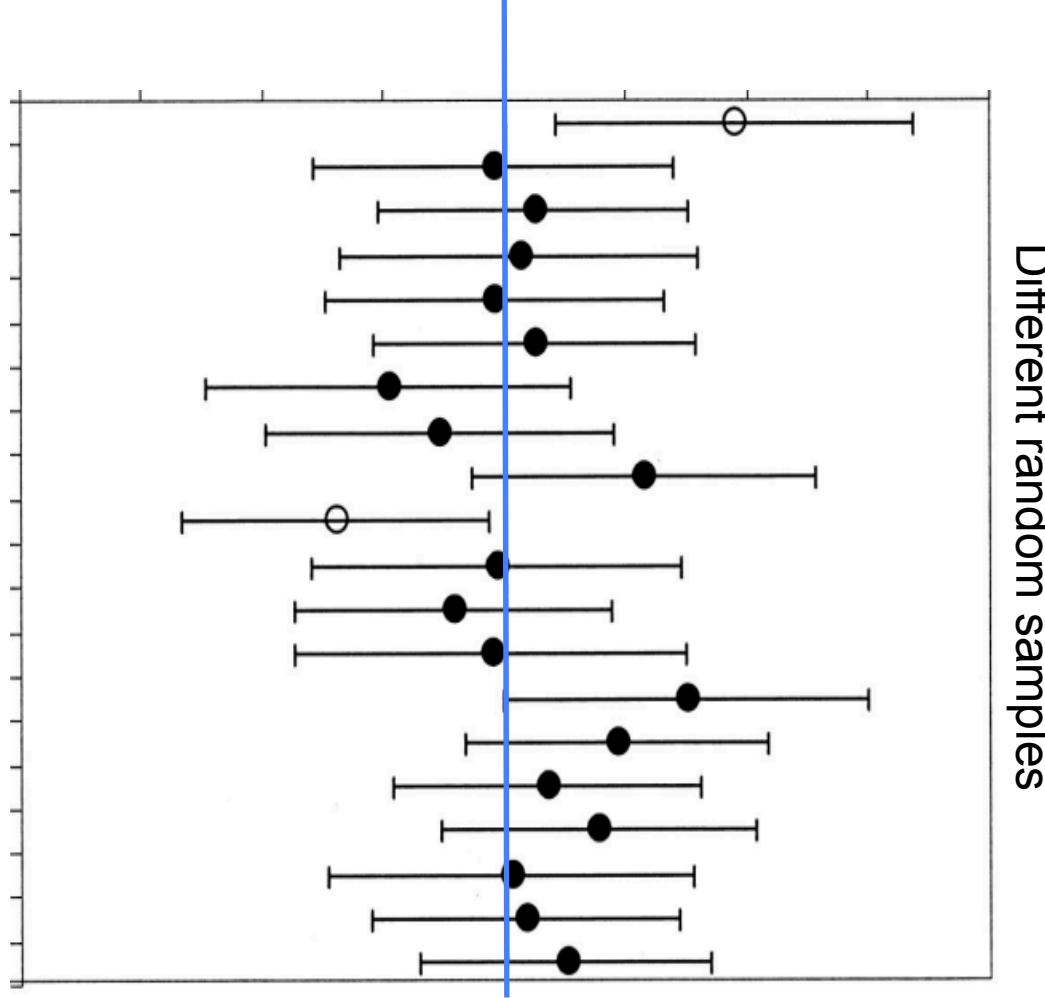
(Cumming, 2013)

CONFIDENCE INTERVALS

- « a range of plausible values for μ . Values outside the CI are relatively implausible. »
(Cumming and Finch, 2005)



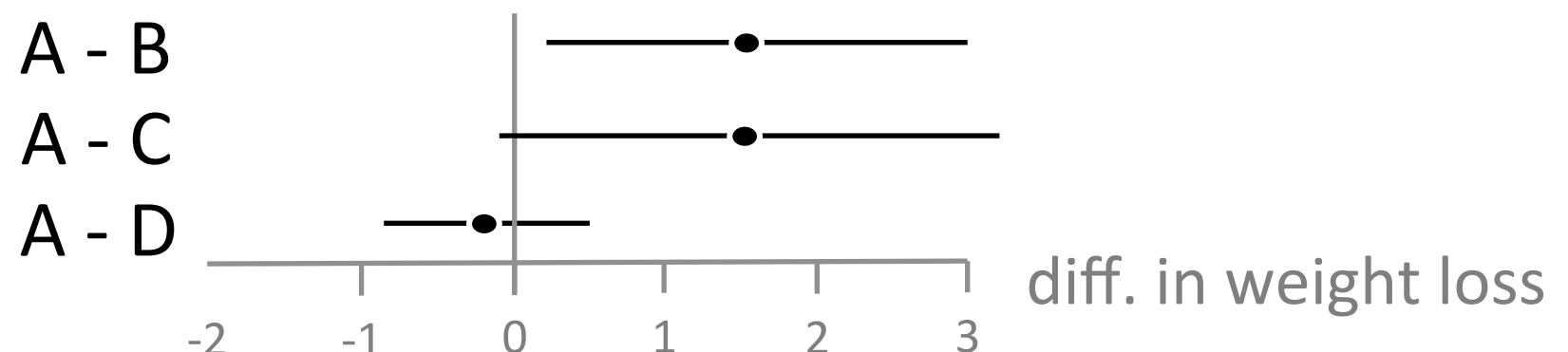
True mean



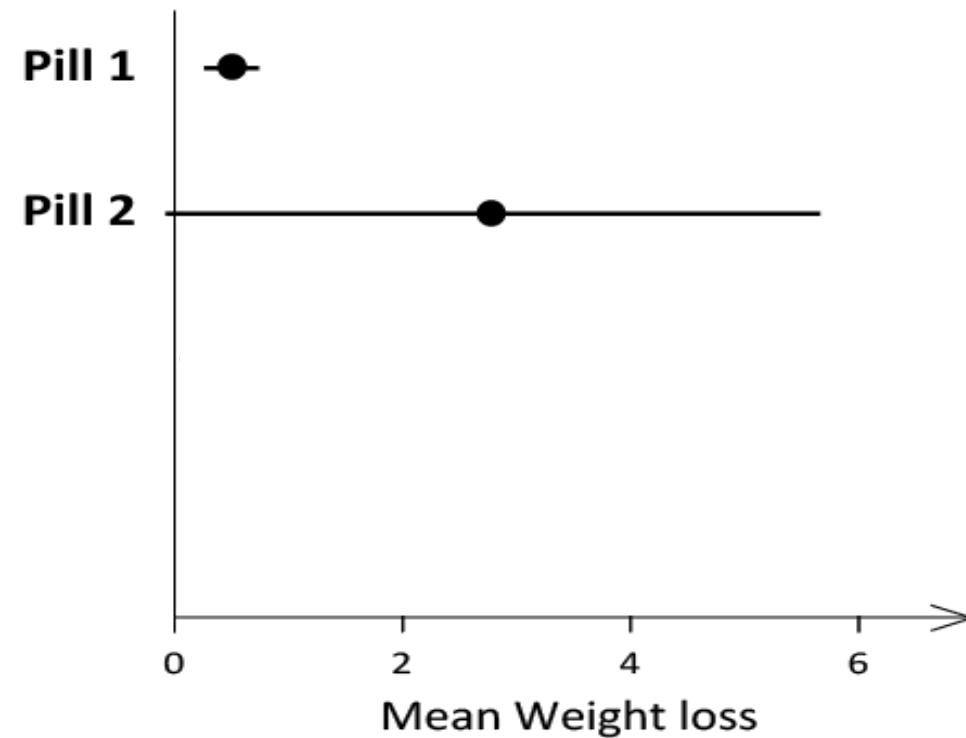
Different random samples

CONFIDENCE INTERVALS

- « a range of plausible values for μ . Values outside the CI are relatively implausible. »
(Cumming and Finch, 2005)

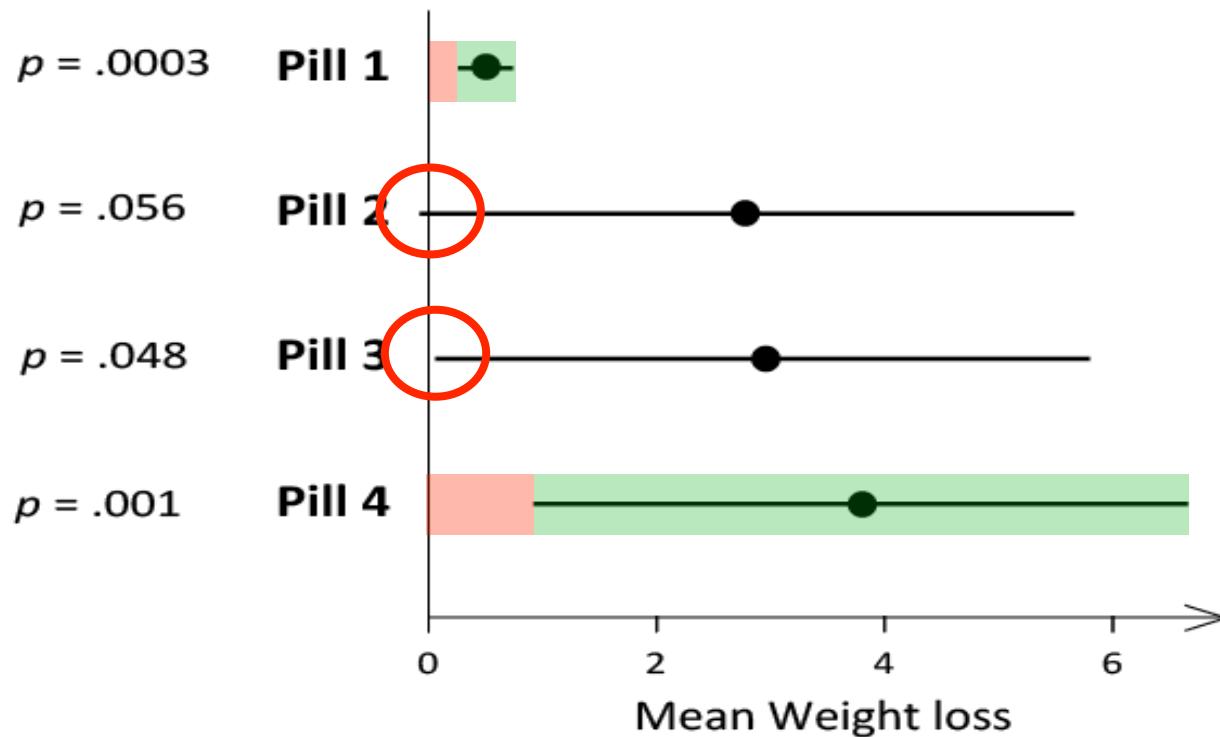


WHICH PILL IS BEST?



Error bars are 95% CIs

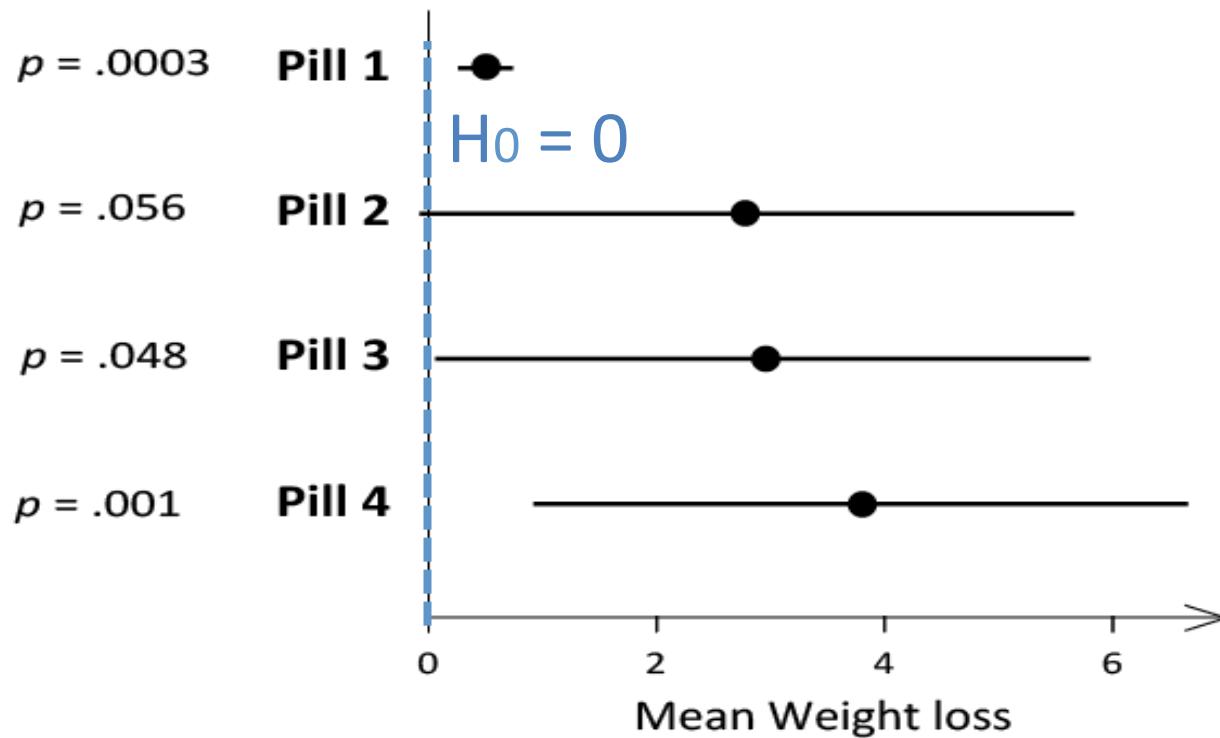
STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

p-values are based on a null hypothesis of no effect

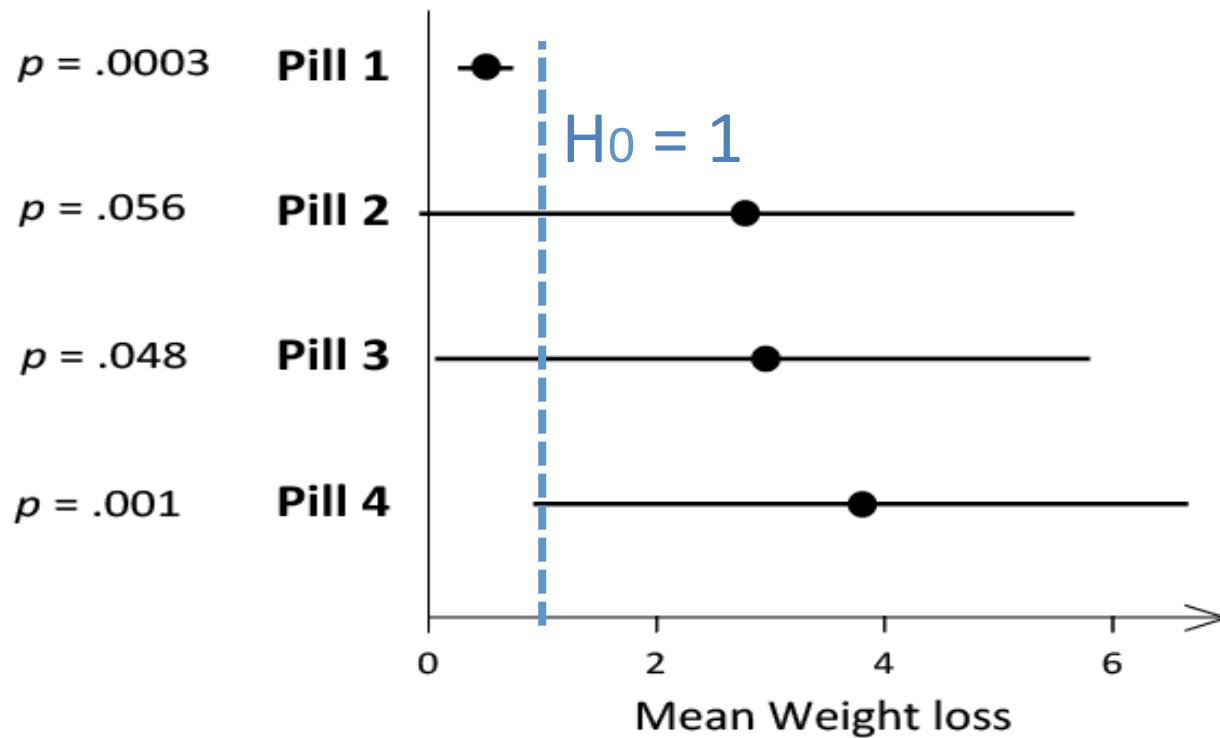
STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

p-values are based on a null hypothesis of no effect

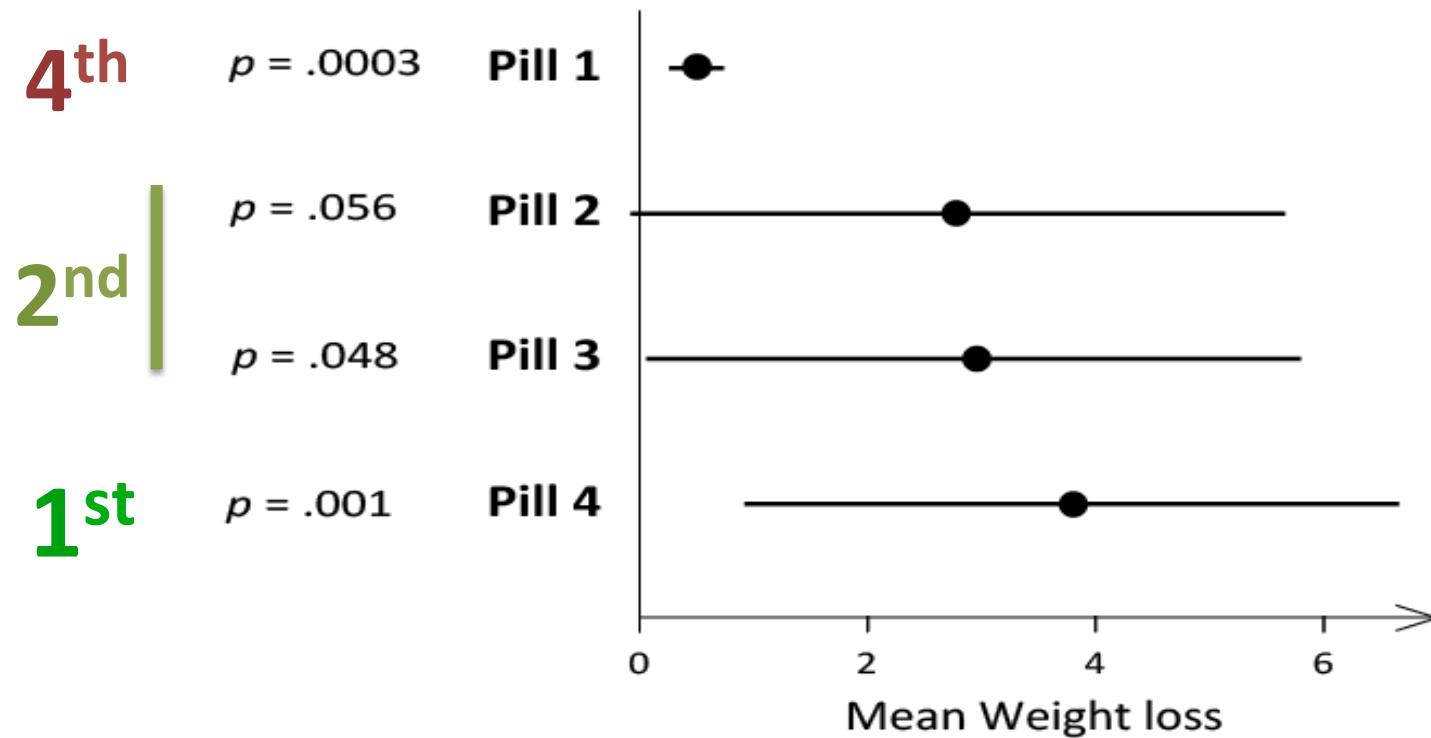
STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

p-values are based on a null hypothesis of no effect

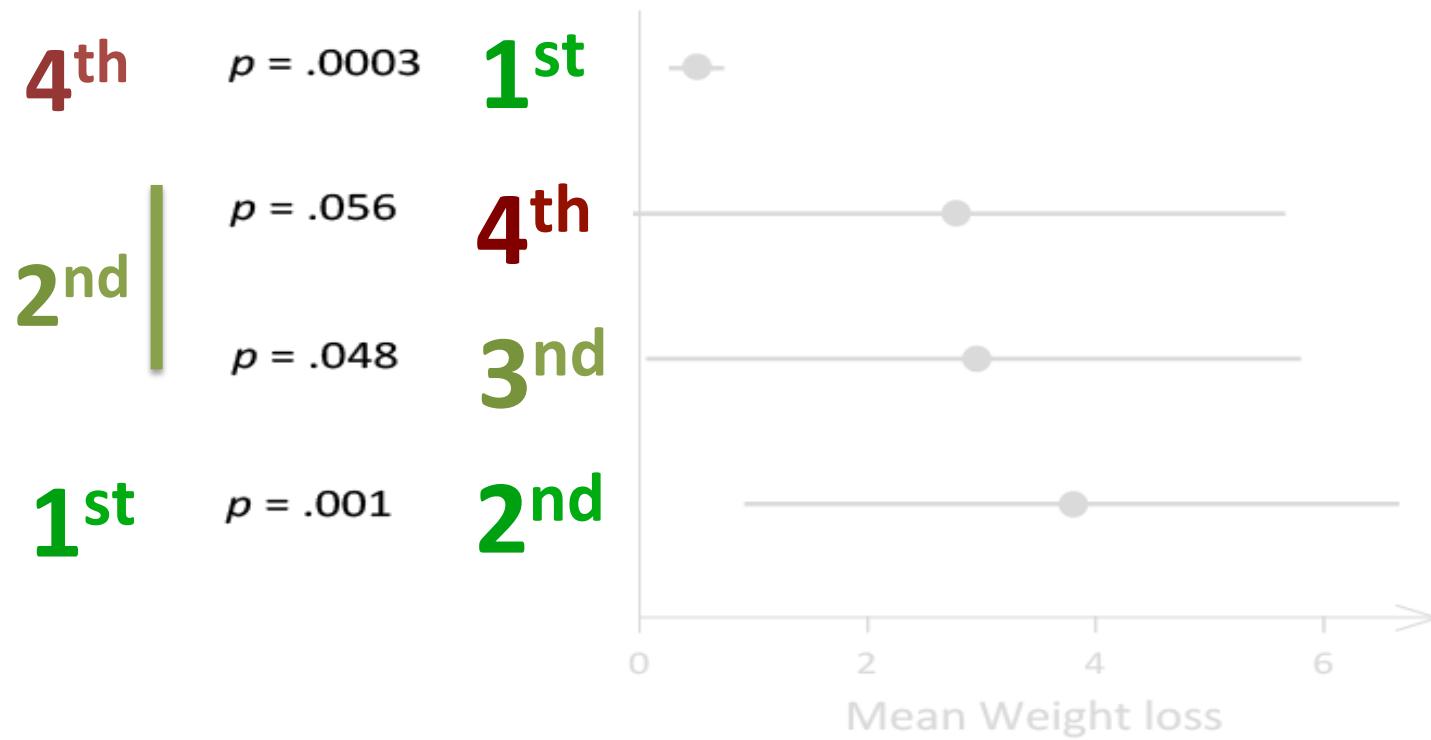
STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

p -values are based on a null hypothesis of no effect

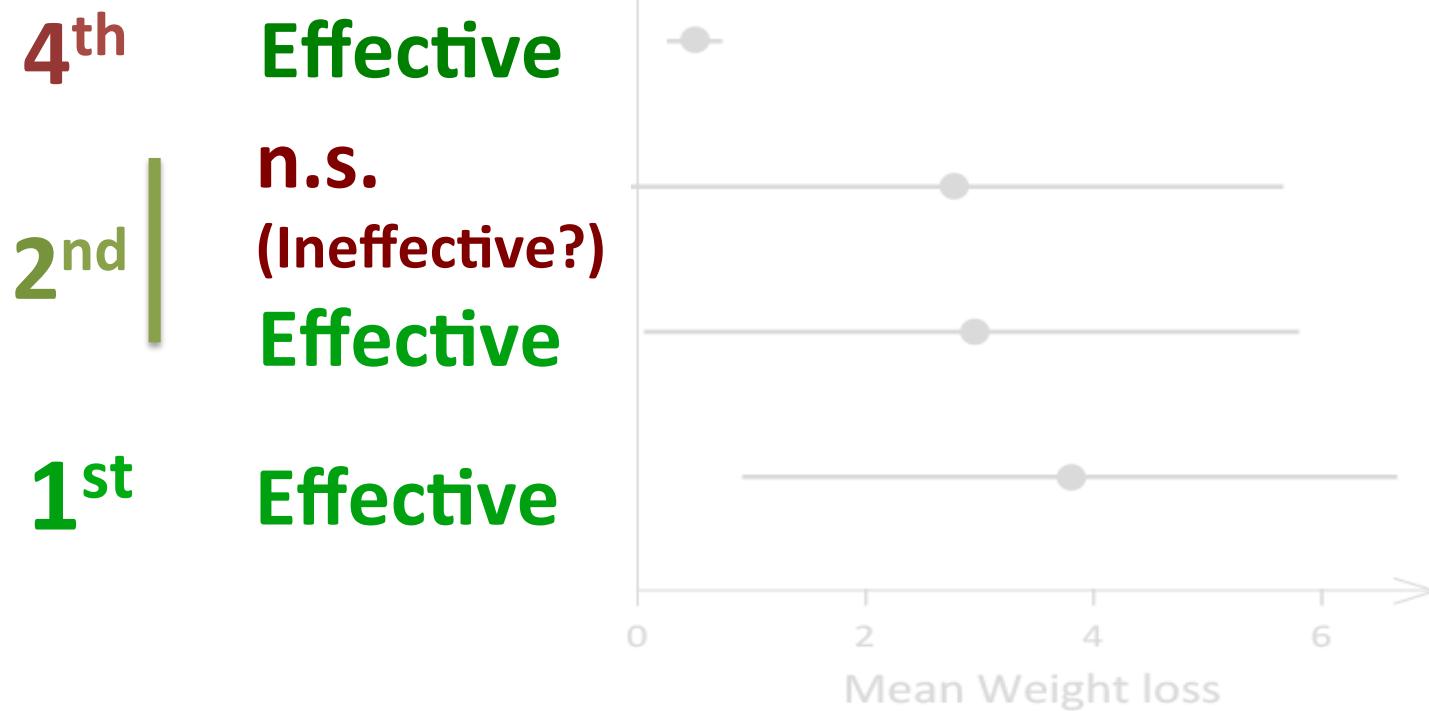
STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

p-values are based on a null hypothesis of no effect

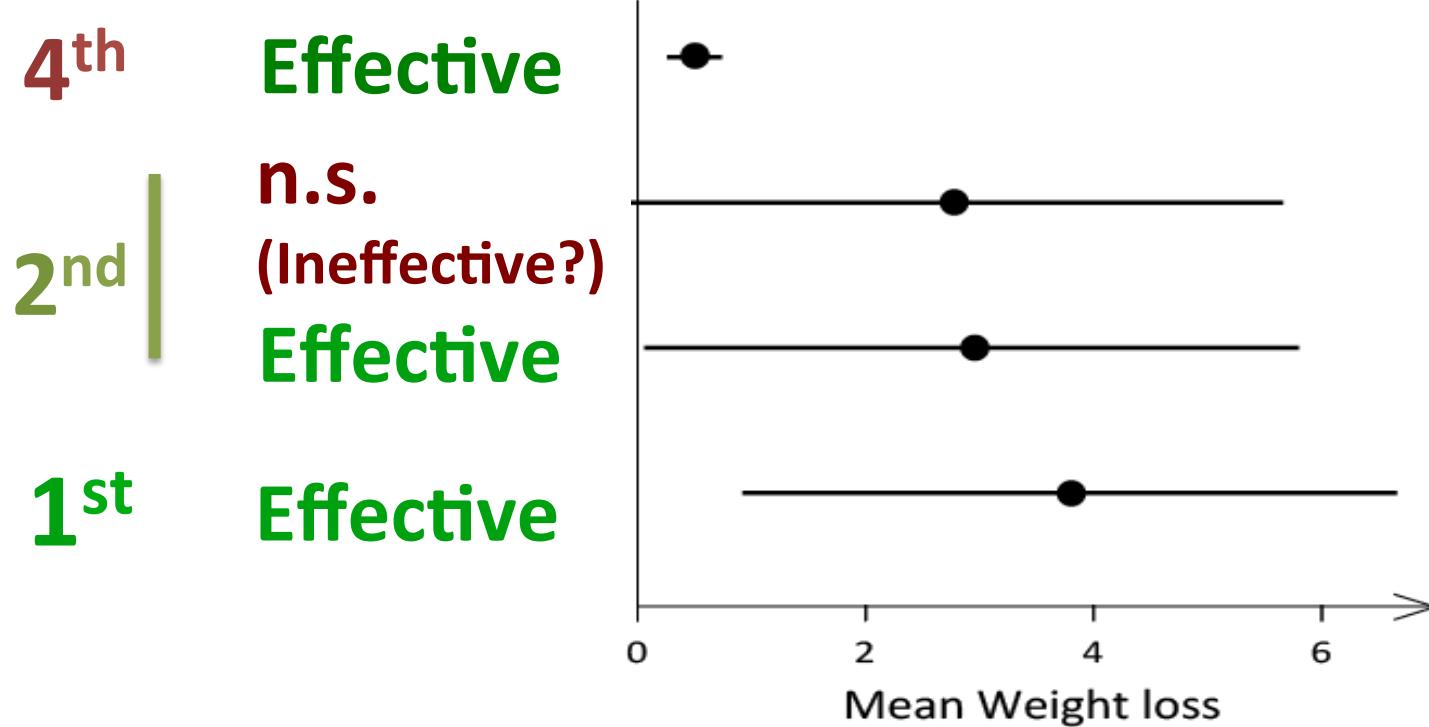
STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

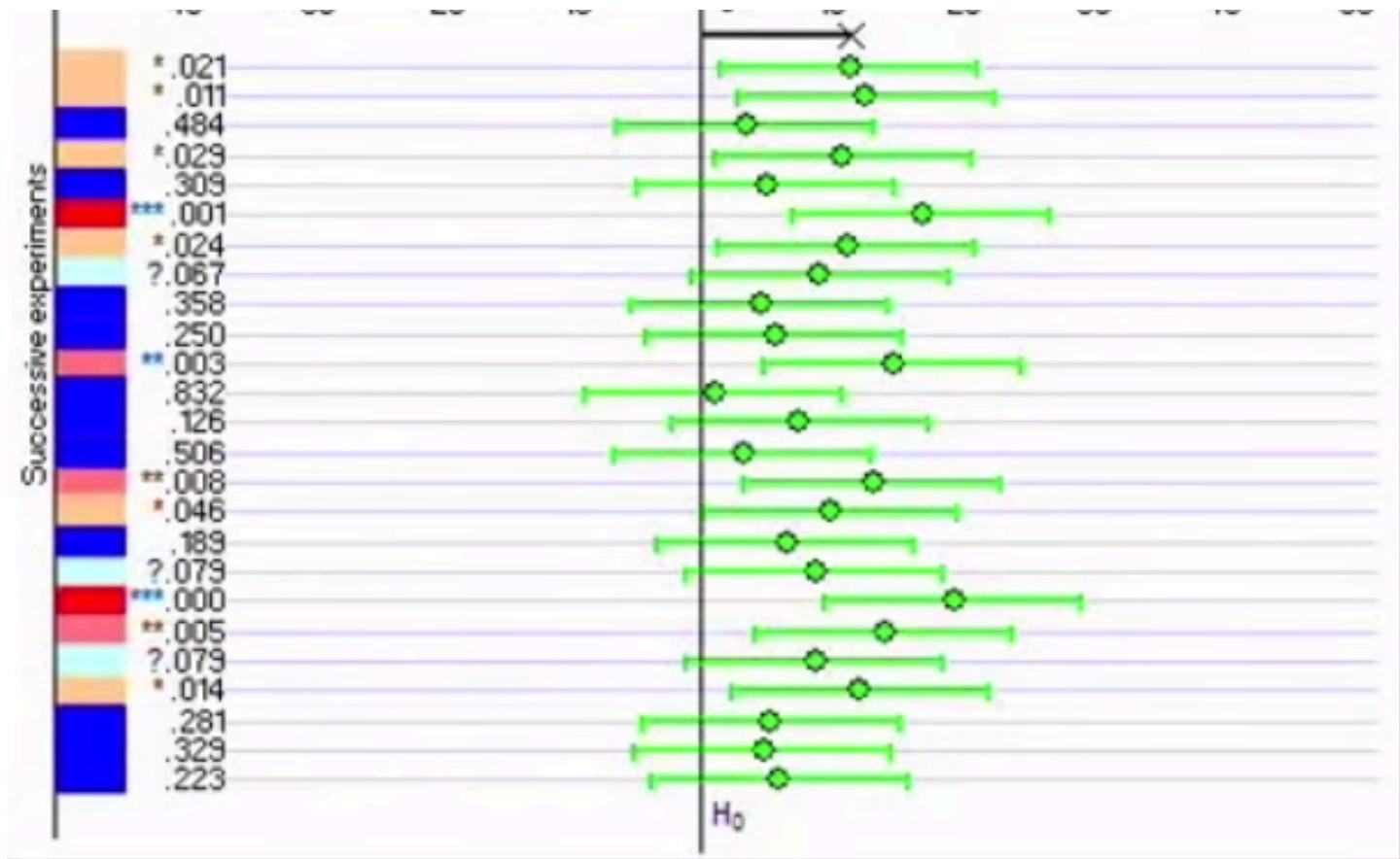
p-values are based on a null hypothesis of no effect

STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

p-values are based on a null hypothesis of no effect



Make sure you check *the dance of p-values* on youtube

STATISTICAL SIGNIFICANCE

effect of METHOD ($F_{4,44} = 10.1, p < 0.0001$ and $F_{3,33} = 49.1, p < 0.0001$) for both datasets (4) and a significant effect of SCALE for the data (not for SCALE ≥ 4 ($F_{2,22} = 2.7, p = 0.0885$)). $F_{1,11} = 0.1116$ and $F_{1,11} = 3.9, p = 0.0718$). interactions of METHOD \times W ($F_{12,132} = 6.1, p < 0.0001$ and $F_{6,66} = 10.6, p < 0.0001$) for SCALE = 1 in particular, we have a higher error than his difference vanishes as W increases. The Mag with other methods. For the remaining is in the error rates.

... - - -

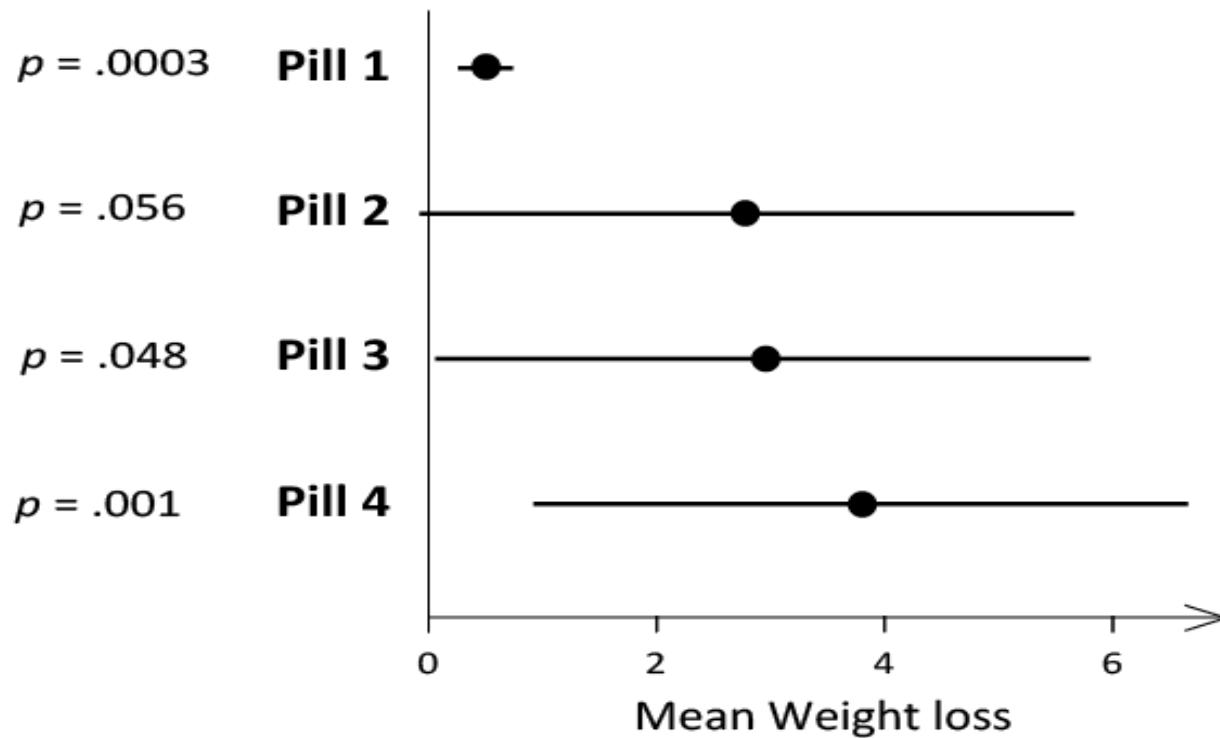
STATISTICAL SIGNIFICANCE

“ [NHST] is based upon a fundamental misunderstanding of the nature of rational inference, and is seldom if ever appropriate to the aims of scientific research. ”

Rozeboom (1960)

For more www.aviz.fr/parallel

STATISTICAL SIGNIFICANCE



Error bars are 95% CIs

p-values are based on a null hypothesis of no effect

STATISTICAL SIGNIFICANCE

*“ It seems clear that **no** confidence interval should be interpreted as a significance test.”*

(Schmidt and Hunter, 1997)

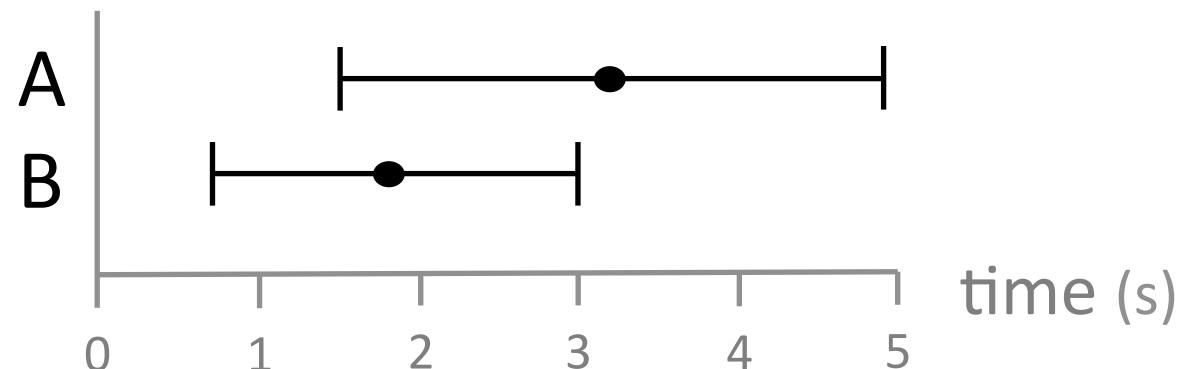
STATISTICAL SIGNIFICANCE

*“It is best for individual researchers to present point estimates and confidence intervals and **refrain from attempting to draw final conclusions** about research hypotheses .”*

(Schmidt and Hunter, 1997)

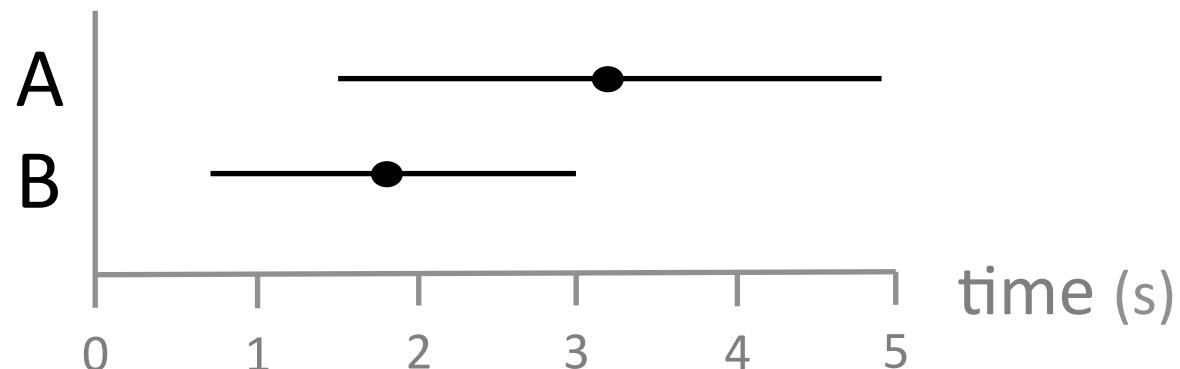
HOW TO GRAPH CIS?

- As error bars



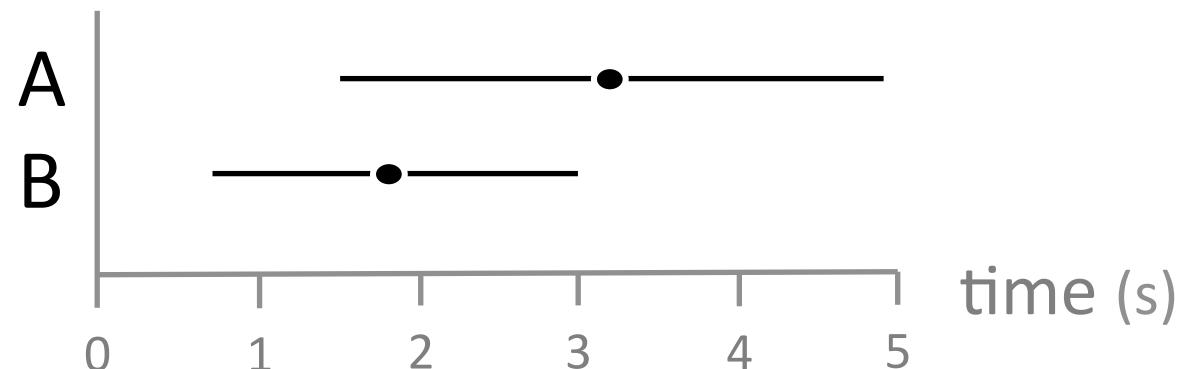
HOW TO GRAPH CIS?

- As error bars
- Better way:



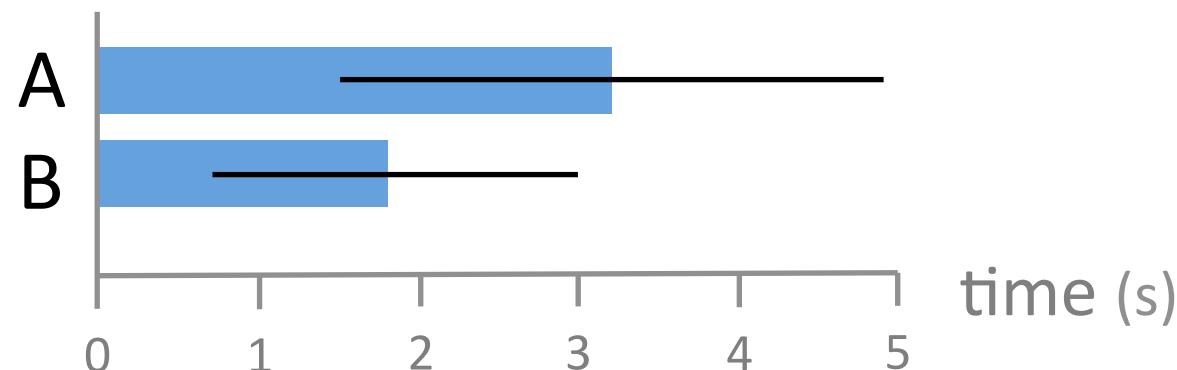
HOW TO GRAPH CIS?

- As error bars
 - Slightly nicer:



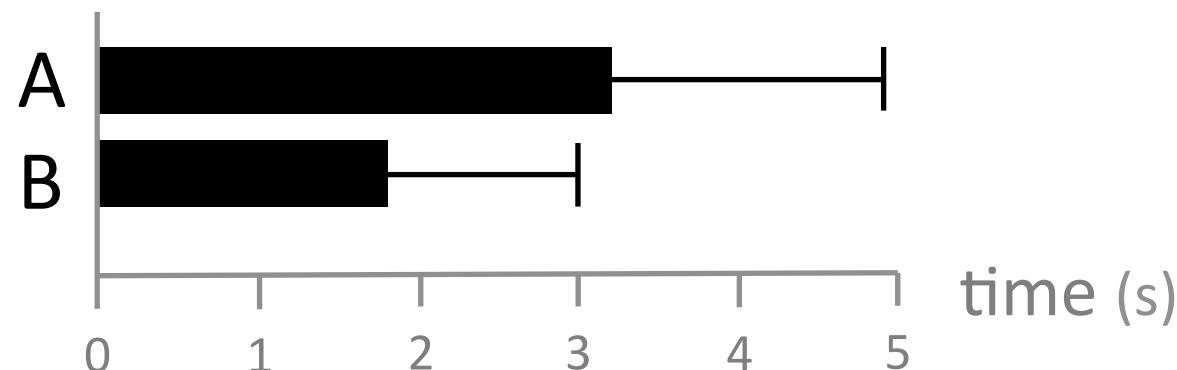
HOW TO GRAPH CIS?

- As error bars
 - With bar charts:



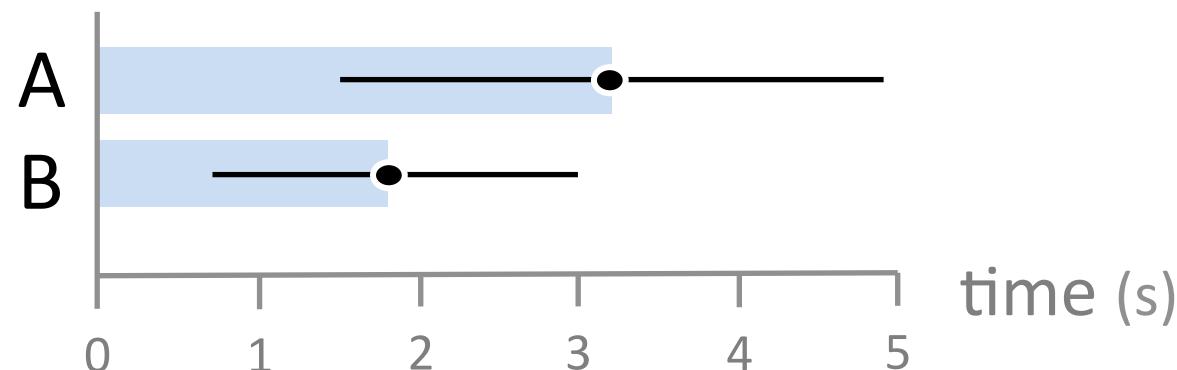
HOW TO GRAPH CIS?

- As error bars
 - Dynamite plots:



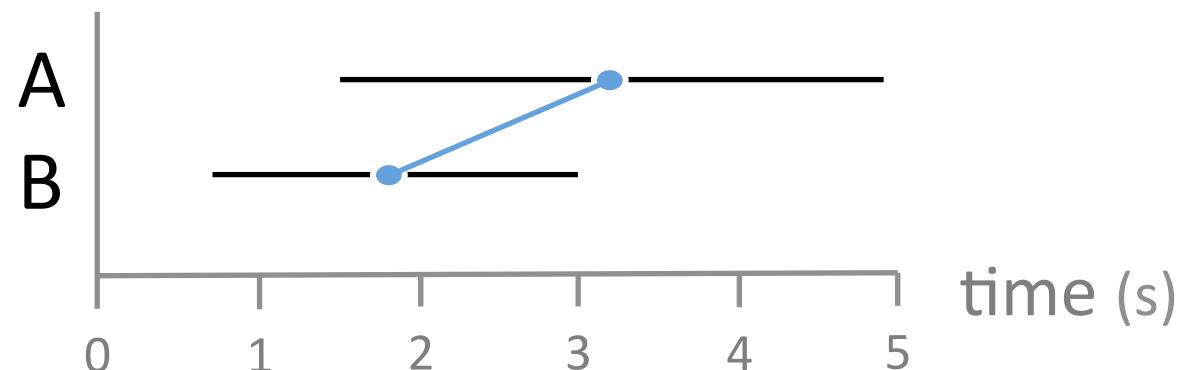
HOW TO GRAPH CIS?

- As error bars
 - Perhaps a better approach:



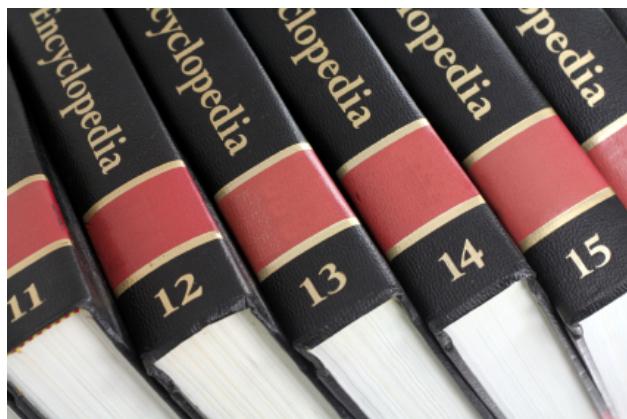
HOW TO GRAPH CIS?

- As error bars
 - With line charts:



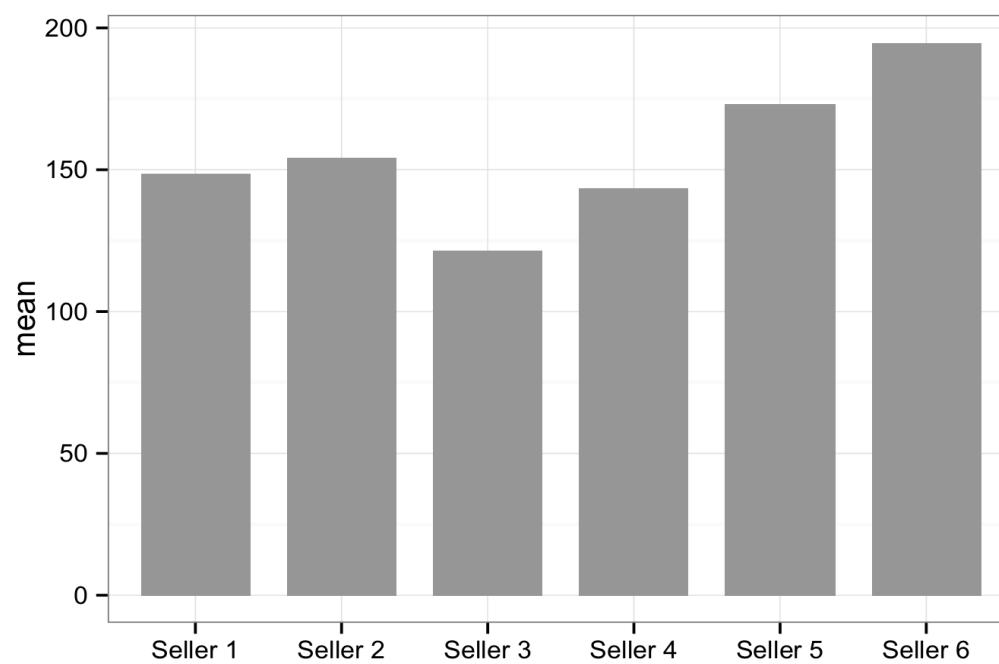
BACK TO OUR EXAMPLE

- Selling encyclopedias



Average Sales

Seller 1	Seller 2	Seller 3	Seller 4	Seller 5	Seller 6
€149	€154	€122	€143	€173	€195



day	Seller 1	Seller 2	Seller 3	Seller 4	Seller 5	Seller 6
1	€320	€80	€139	€330	€133	€387
2	€74	€60	€98	€44	€182	€29
3	€340	€67	€42	€100	€51	€91
4	€322	€54	€89	€44	€67	€886
5	€146	€195	€47	€173	€49	€227
6	€24	€288	€124	€111	€730	€79
7	€42	€249	€26	€77	€672	€45
8	€76	€67	€140	€382	€195	€171
9	€99	€312	€125	€123	€43	€98
10	€915	€77	€106	€250	€149	€70
11	€202	€504	€101	€205	€682	€134
12	€47	€167	€126	€48	€93	€63
13	€34	€65	€55	€56	€333	€1,157
14	€76	€46	€89	€104	€56	€470
15	€75	€34	€184	€35	€299	€205
16	€68	€37	€275	€170	€57	€192

