

# VISUALIZING MULTI-ATTRIBUTE DATA

## DATA TABLES

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# RECAP

you have learned about

- visual variables and marks
- that their perceptual properties matter

# RECAP

## ➔ Magnitude Channels: Ordered Attributes

Position on common scale 

Position on unaligned scale 

Length (1D size) 

Tilt/angle 

Area (2D size) 

Depth (3D position) 

Color luminance 

Color saturation 

Curvature 

Volume (3D size) 

Effectiveness  
Most  
Least

## ➔ Identity Channels: Categorical Attributes

Spatial region 

Color hue 

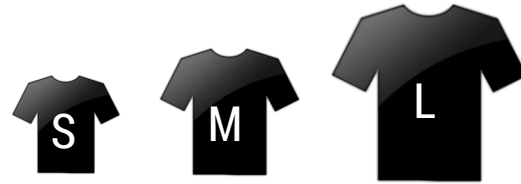
Motion 

Shape 

# RECAP

## DATA TYPES

ORDINAL (ranking)



NOMINAL (categorical)

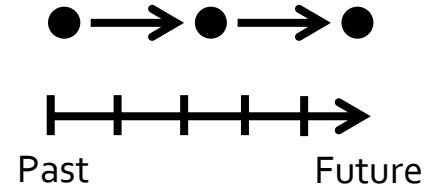


QUANTITATIVE (numerical)

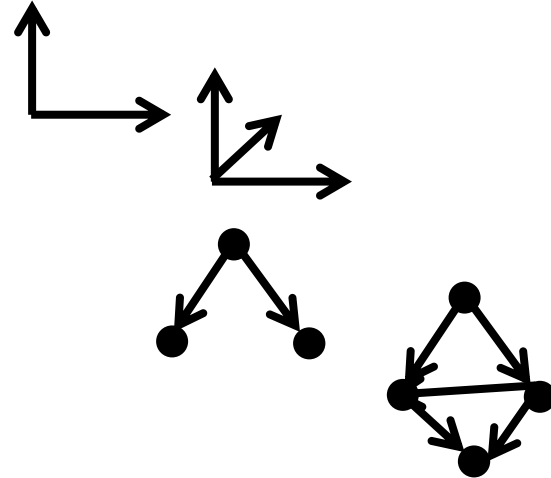


# RECAP

- 1D (linear)
- Temporal
- 2D (maps)
- 3D
- nD (relational)
- Trees (hierarchies)
- Networks (graphs)

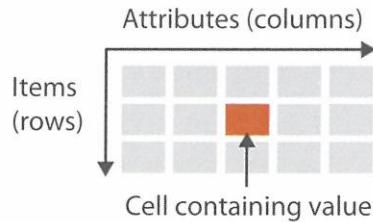


vis examples later

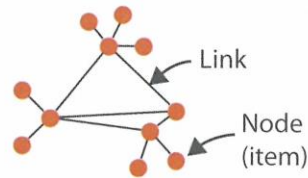


# ANOTHER VIEW

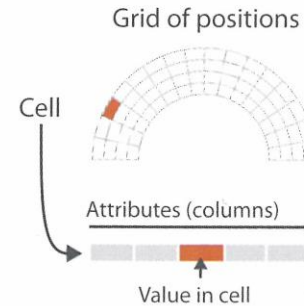
→ Tables



→ Networks



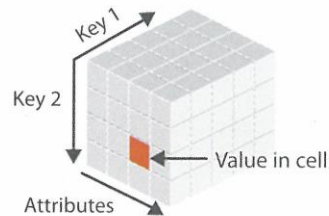
→ Fields (Continuous)



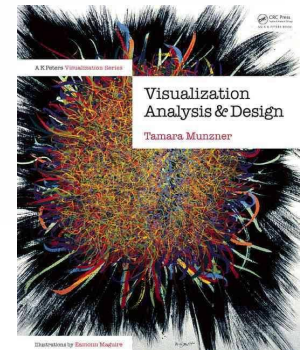
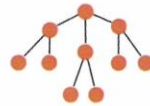
→ Geometry (Spatial)



→ *Multidimensional Table*



→ *Trees*



# TODAY

How to turn something like this ... into a multi-dimensional data representation

## Vélib' : Disponibilité temps réel

[Informations](#) [Tableau](#) [Carte](#) [Analyse](#) [Export](#) [API](#)

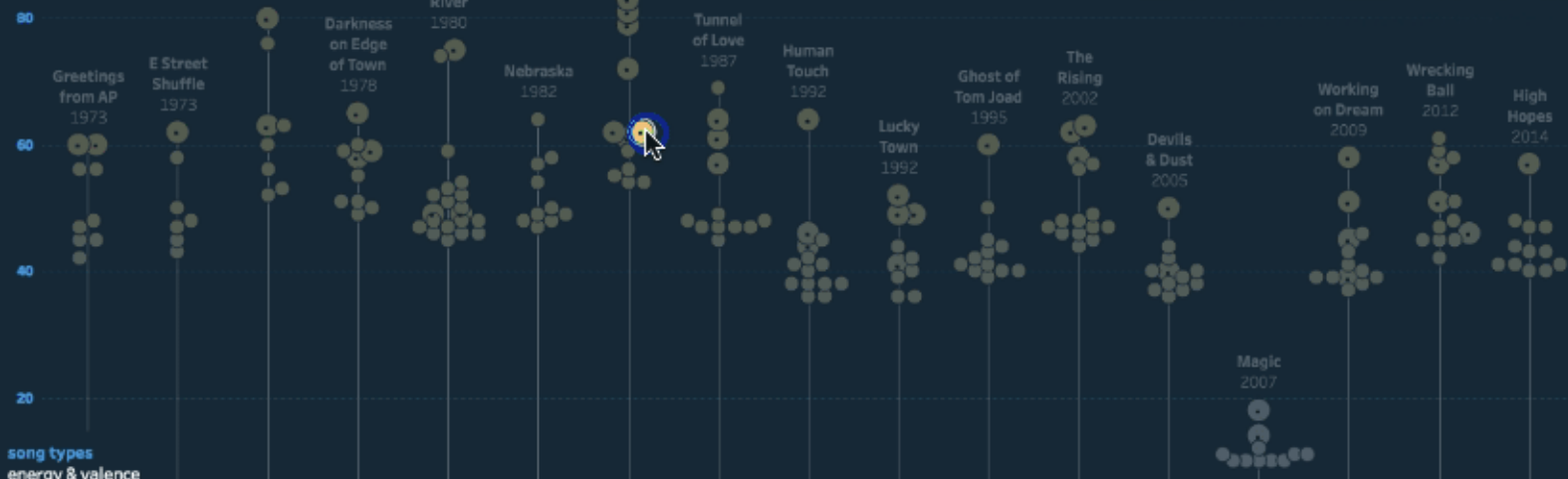
	Code de la station	Nom de la station	Etat des stations	Etat du Totem	Nombres de bornes en station	Nombre de bornes disponibles	Nombre de vélo mécanique	Nombre vélo électrique	Achat possible en
1	11037	Faubourg Du Temple - Republique	Close	yes	39	36	2	1	yes
2	11104	Charonne - Robert et Sonia Delauney	Operative	yes	20	17	2	1	no
3	14111	Cassini - Denfert-Rochereau	Close	yes	25	25	0	0	yes
4	12109	Mairie du 12ème	Operative	yes	30	30	0	0	no
5	5110	Lacépède - Monge	Operative	yes	23	16	6	1	yes
6	17038	Grande Armée - Brunel	Operative	yes	62	40	20	2	yes
7	10152	Gare du Nord - Place de Valenciennes	Operative	yes	25	18	6	1	yes
8	13007	Le Brun - Gobelins	Operative	yes	48	47	1	0	yes
9	41301	Bois de Vincennes - Gare	Operative	yes	51	39	8	4	yes
10	31024	Romainville - Vaillant-Couturier	Operative	yes	38	35	2	1	no
11	15028	Grenelle - Dr Finlay	Operative	yes	71	63	7	2	yes
12	16118	Michel-Ange - Parent de Rosan	Operative	yes	26	25	0	1	no
13	20035	Pyrénées - Mémilmontant	Operative	yes	26	24	0	2	no
14	10027	Dunkerque - Alsace	Operative	yes	18	10	8	0	no
15	8048	Marceau - Chaillot	Operative	yes	21	8	9	4	no
16	14013	Liard - Amiral Mouchez	Operative	yes	1	1	1	0	yes
17	5024	Place Monge	Close	yes	21	21	0	0	no
18	7018	Séгур - d'Estrées	Operative	yes	19	8	10	1	no
19	10029	Dunkerque - Rocroy	Operative	yes	23	16	6	1	no
20	8009	Gare Saint-Lazare - Isly	Operative	yes	27	14	10	3	yes
21	8036	Lisbonne - Monceau	Operative	yes	33	7	25	1	yes
22	17040	Pereire - Ternes	Operative	yes	48	44	2	2	yes
23	31708	Noisy le Sec - Jean-Baptiste Clément	Operative	yes	22	21	0	1	no
24	10105	Mazagran - Bonne Nouvelle	Operative	yes	26	15	9	2	yes

**SOME INSPIRING EXAMPLES**

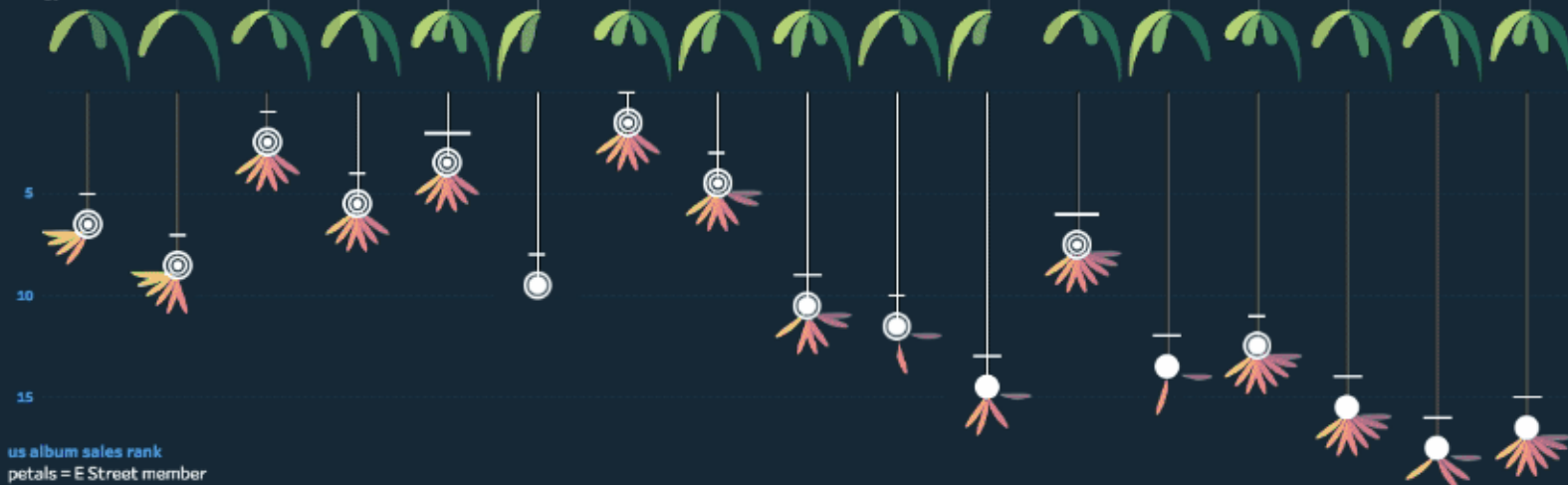


# TOP SONGS

by album  
spotify popularity



song types  
energy & valence



us album sales rank  
petals = E Street member

# TOP ALBUMS

# the history of BRUCE SPRINGSTEEN

Over a 45 year career Bruce Springsteen has released over 200 songs and 17 studio albums. Born in Long Branch NJ and raised in working class Freehold NJ he is known for his poetic lyrics and energetic stage performances. He has sold 135 million albums worldwide. The following is a musical history of Bruce Springsteen using excerpts from his autobiography "Born to Run", interviews, and Wikipedia.

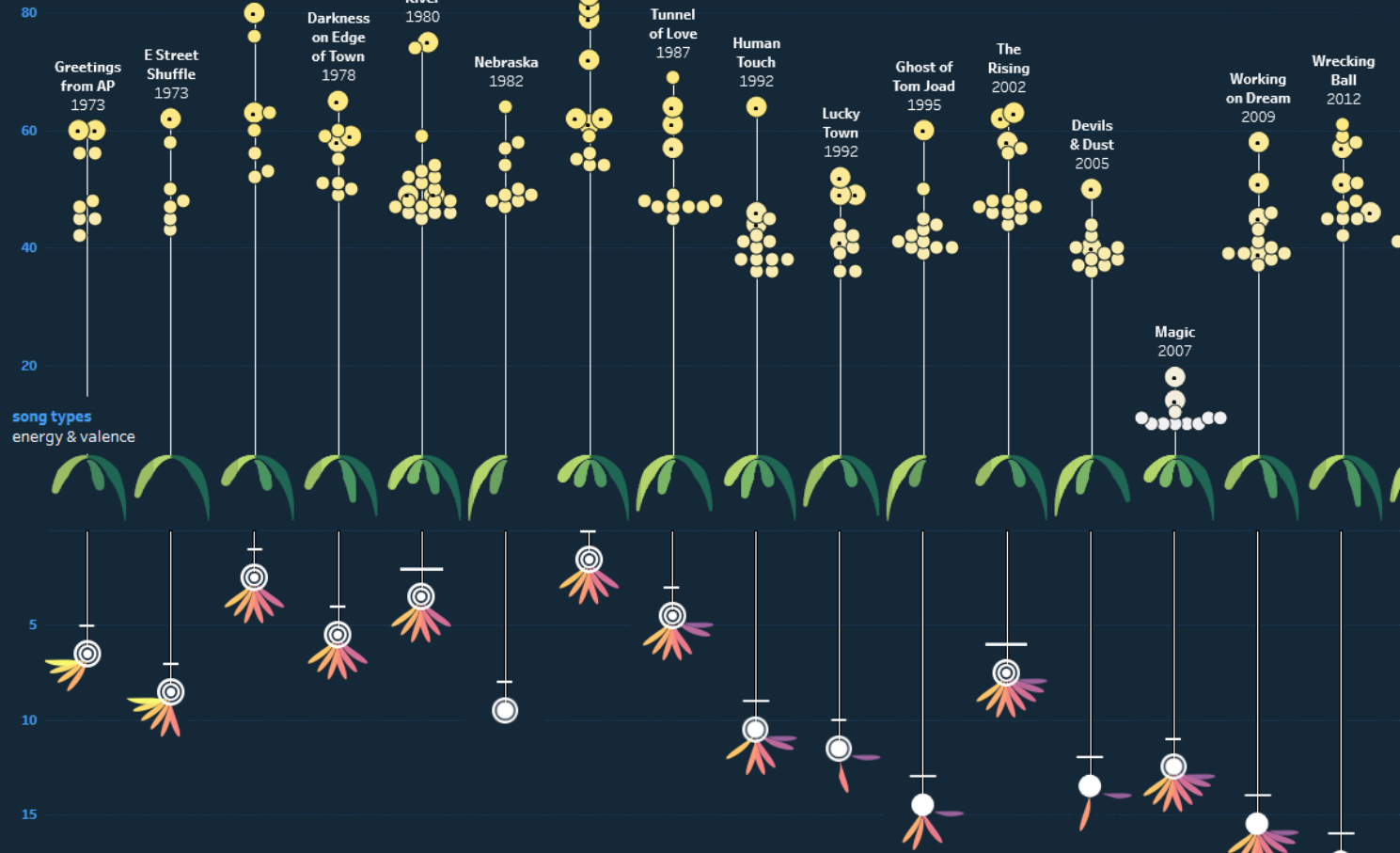
John Hammond of Columbia Records signed Bruce after he played Saint in the City for him in his office. Columbia wanted a solo artist like Bob Dylan and James Taylor but Bruce insisted on recording with a band to get the new sound he was pursuing: "an amalgam of good song-writing mixes with a soul-and-R&B influenced, rock music" as Bruce said in his autobiography "Born to Run".

**Greetings from Asbury Park, N.J.** is Bruce's debut studio album released on January 5, 1973. After completing the album Clive Davis of Columbia Records was worried there were no hits. So Bruce wrote "Spirit in the Night" and "Blinded by the Light" the next day at the beach. They were the two biggest hits on the album. Early reviews of the album made favorable comparisons to Dylan.

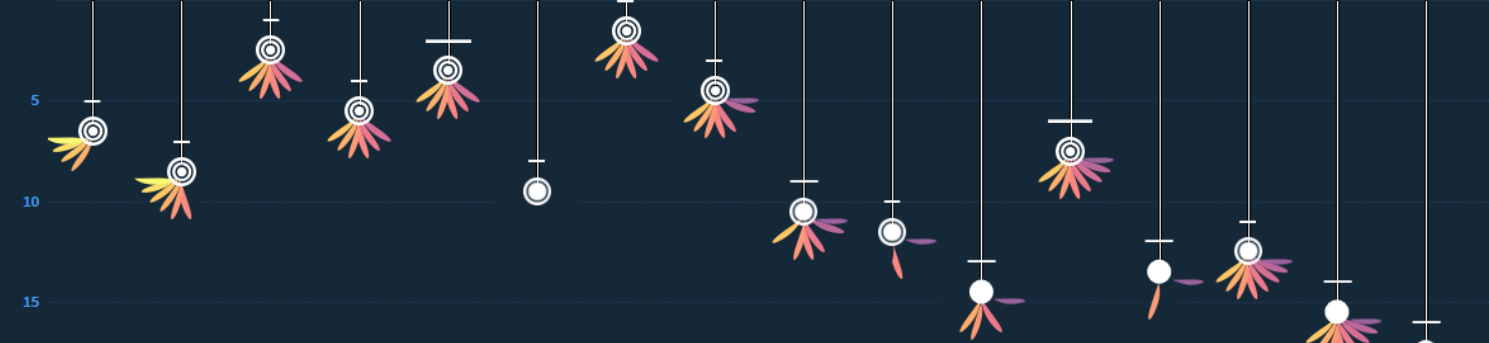
**The Wild, the Innocent & the E Street Shuffle** is Bruce's second album released on November 11, 1973. Bruce recorded this album over 3 months at the 914 Sound Studios in Blauvelt NY. Bruce and Clarence Clemons slept in a tent behind the studio to save money. Like Greetings from Asbury Park the album was not a commercial success but received positive

# TOP SONGS

by album  
spotify popularity



song types  
energy & valence



us album sales rank  
petals = E Street member

# TOP ALBUMS

created by Adam McCann @adamemccann | inspired by Federica Fragapane @fedfragapane & Giorgia Lupi @giorgialupi

# the history of BRUCE SPRINGSTEEN

**Song Popularity by Album**

- Single
- Song

**Song Types Energy & Valence**  
Size = # Songs

High Energy  
High Valence

**Album Sales Rank**

- Bar Length = Album Duration
- Non-Platinum
- ◉ Platinum
- ◉ Multi-Platinum

Max Weinberg on Album

**E Street Members on the Album**  
in order of appearance

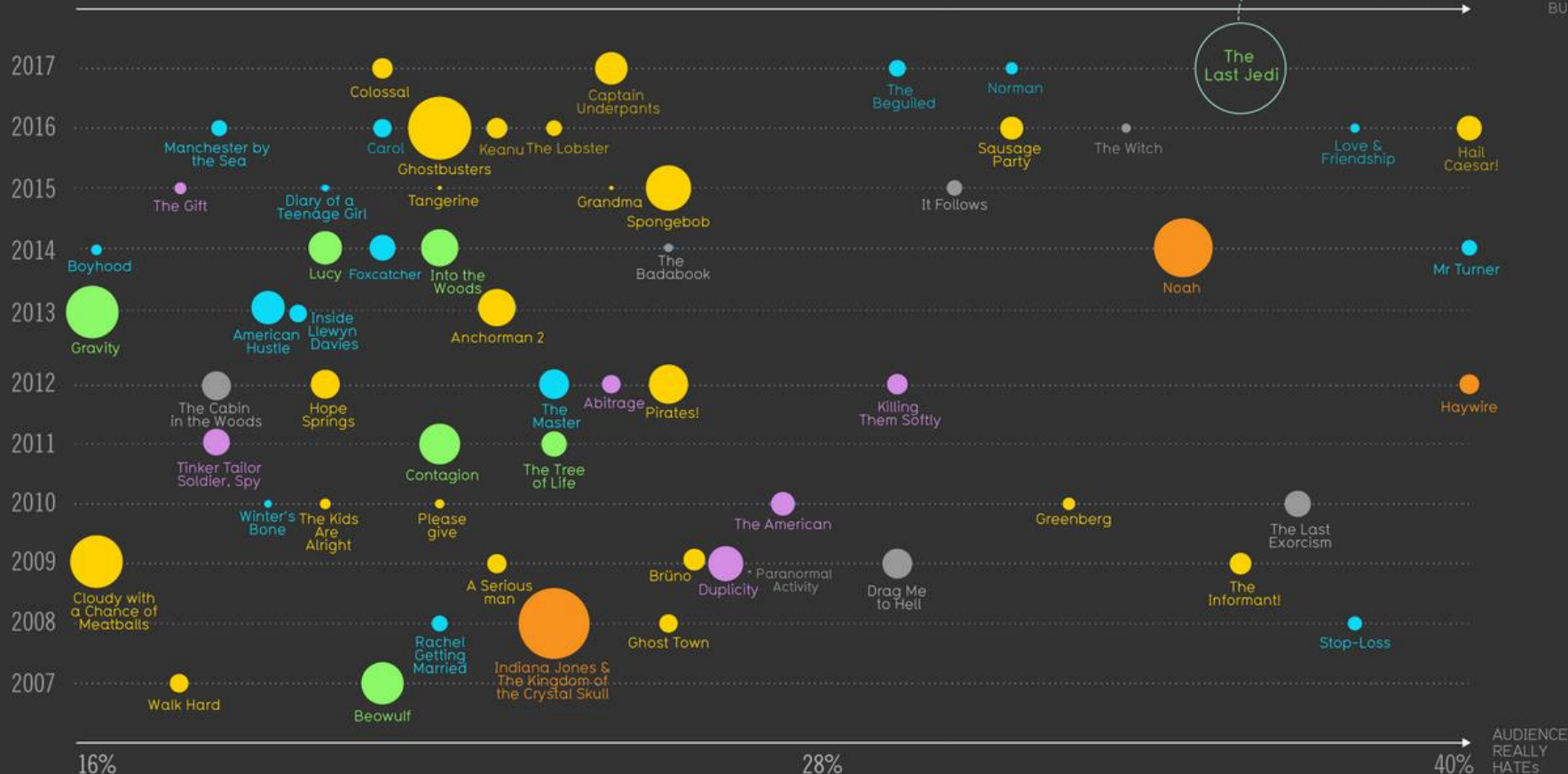
Sources Spotify API via @plamer (popularity, song attributes), Wikipedia (narrative, album sales) and "Born to Run" book (narrative)

How to Read

# Movies Critics Loved, But Audiences Really Didn't

% gap between audience & critics 'rotten tomatoes' score

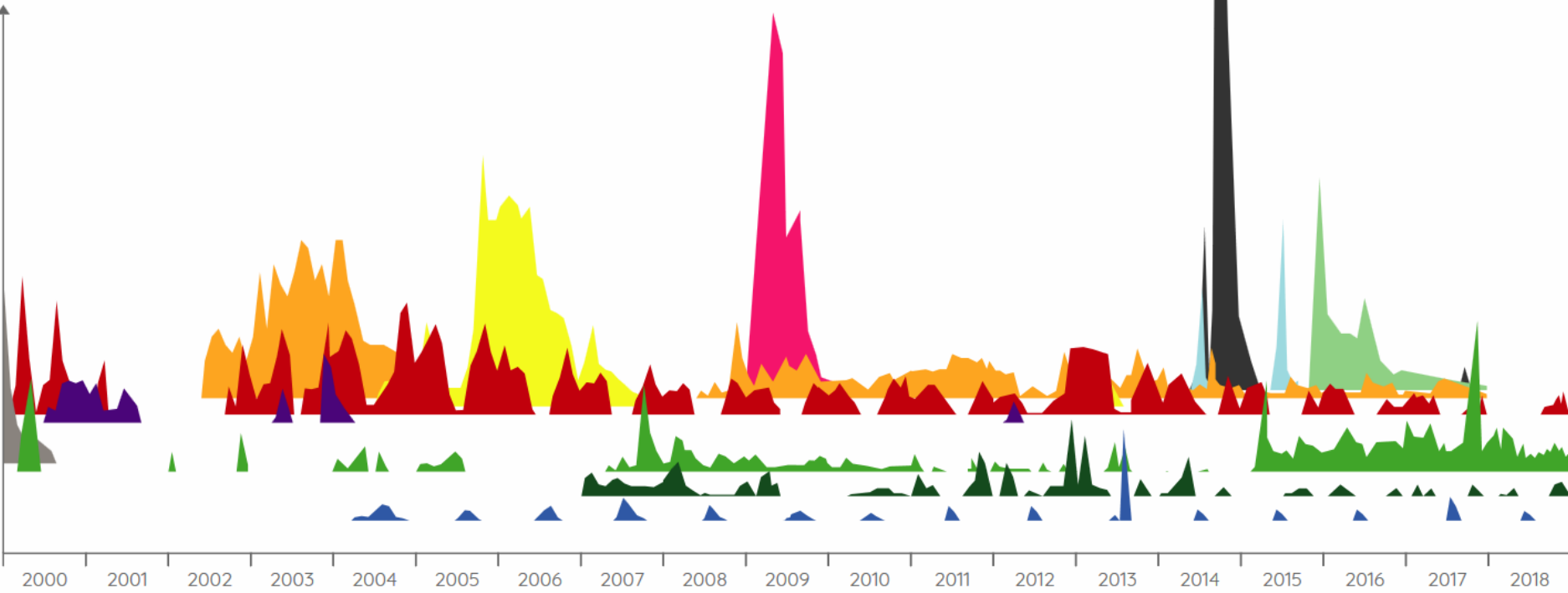
biggest budget movie with the most dramatic split between critics & audience opinion



# Mountains Out of Molehills

A timeline of media-inflamed fears

INTENSITY  
(no. of news media mentions)



- ASTERIODS
- BIRD FLU
- EBOLA
- KILLER WASPS
- MAD COW DISEASE
- MERS
- MILLENNIUM BUG
- SARS
- SWINE FLU
- VACCINES & AUTISM
- VIOLENT VIDEO GAMES
- ZIKA

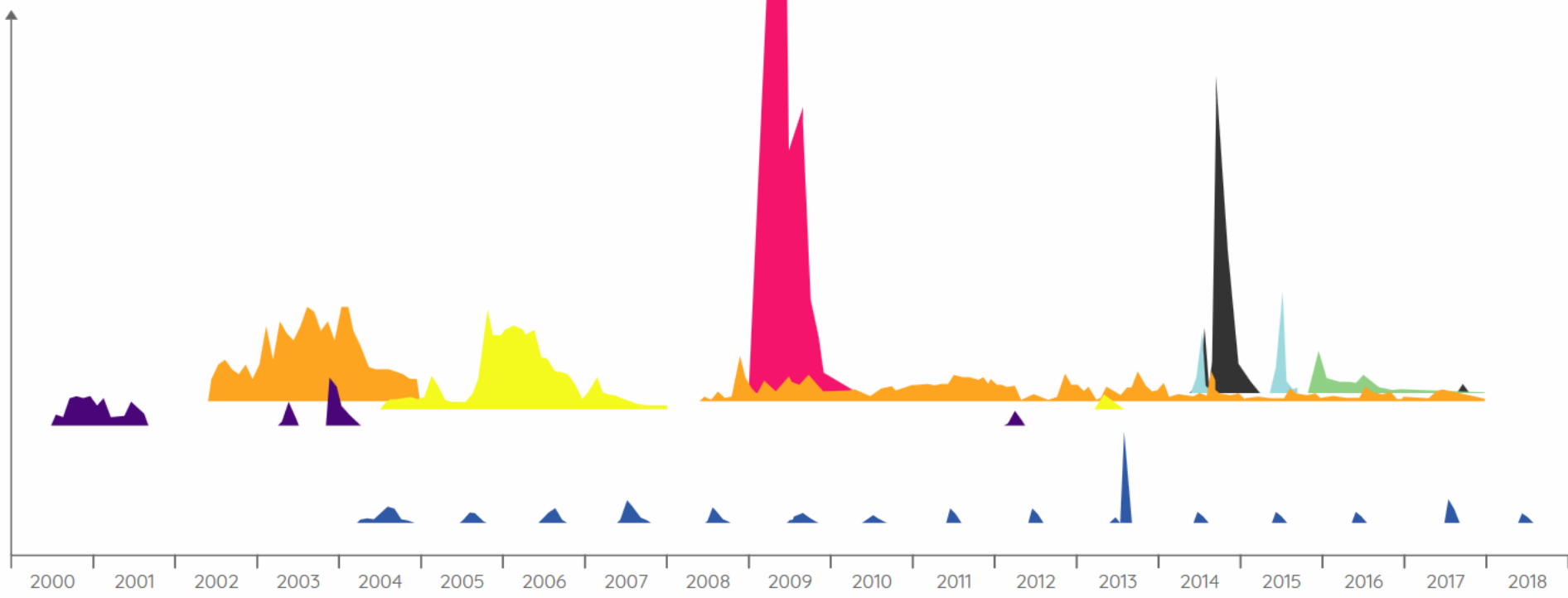
David McCandless, Fabio Bergamaschi // source: Google Trends

align to baseline scale to fit Ebola scale by deaths

# Mountains Out of Molehills

A timeline of media-inflamed fears

No. of Deaths



ASTEROIDS BIRD FLU EBOLA KILLER WASPS MAD COW DISEASE MERS MILLENIUM BUG SARS SWINE FLU VACCINES & AUTISM VIOLENT VIDEO GAMES ZIKA

David McCandless, Fabio Bergamaschi // source: Google Trends

align to baseline scale to fit Ebola scale by deaths

# THE MANY MOONS OF JUPITER

**I**n 1610, Galileo Galilei gazed up through his telescope in the direction of Jupiter. In that moment he likely became the first person to see a moon other than our own, as light that had left the vicinity of the gas giant around half an hour earlier crashed into his pupils and revealed four dotted silhouettes. These Galilean moons, one of which is even larger than the planet Mercury, became the opening entries into a collection that is still increasing today. In fact in 2018, 407 years after the Italian polymath made his discovery, scientists confirmed the existence of

12 more moons locked in slow rotation with the largest planet in our solar system. These newly found satellites form part of a diverse family, many of which share little commonality other than their gravitational anchor. Their orbital shapes range from near perfect circles to highly eccentric and inclined. Their scales vary hugely, from the size of planets to just a kilometer across. Some may have been asteroids captured by Jupiter's powerful gravitational pull, while others were likely a by-product of the very formation of the planet itself.

This data visualization displays every currently known moon of Jupiter, each featuring the year of discovery, discoverer and a representation of scale. Additionally, on the right are some additional insights about the moons. Finally, while all information is correct as of 2018, scientists are finding new wonders in our solar system every day; so who knows how many new Jovian moons are out there right now, held in endless revolutions, just waiting for eyes to meet them for the first time?

**79**  
Moons discovered as of 2018

**18** The number of moons that are prograde  
**61** The number of moons that are retrograde



The Voyager probes, launched in 1977, discovered three of Jupiter's large inner moons

**99.997%**  
The approx. % of the total mass in orbit around Jupiter that comes from the four Galilean moons



One of the newly discovered moons has an odd prograde orbit which crosses its path across several other retrograde moons. This means a collision is very likely, although scientists predict it could take another billion years to actually happen



As of 2018, five of the moons are considered lost  
Ganymede, Jupiter's largest moon, is actually 8% larger than the planet Mercury, making it the 9th largest object in our solar system



It's thought that several of the larger moons could feature subsurface oceans, leading to some exciting possibilities about the existence of life there  
The most moons have been found by a team led by Scott Sheppard



A German astronomer called Simon Markus independently discovered the four Galilean moons at the same time as Galileo. While he didn't receive the title of discoverer, he is responsible for their names, which are still used today

## Reading the data visualization

**Representing each moon**

- Discovery year
- Moon name
- Discoverer

**Regular satellites**

- Amalthea group
- Galilean moons

**Irregular satellites**

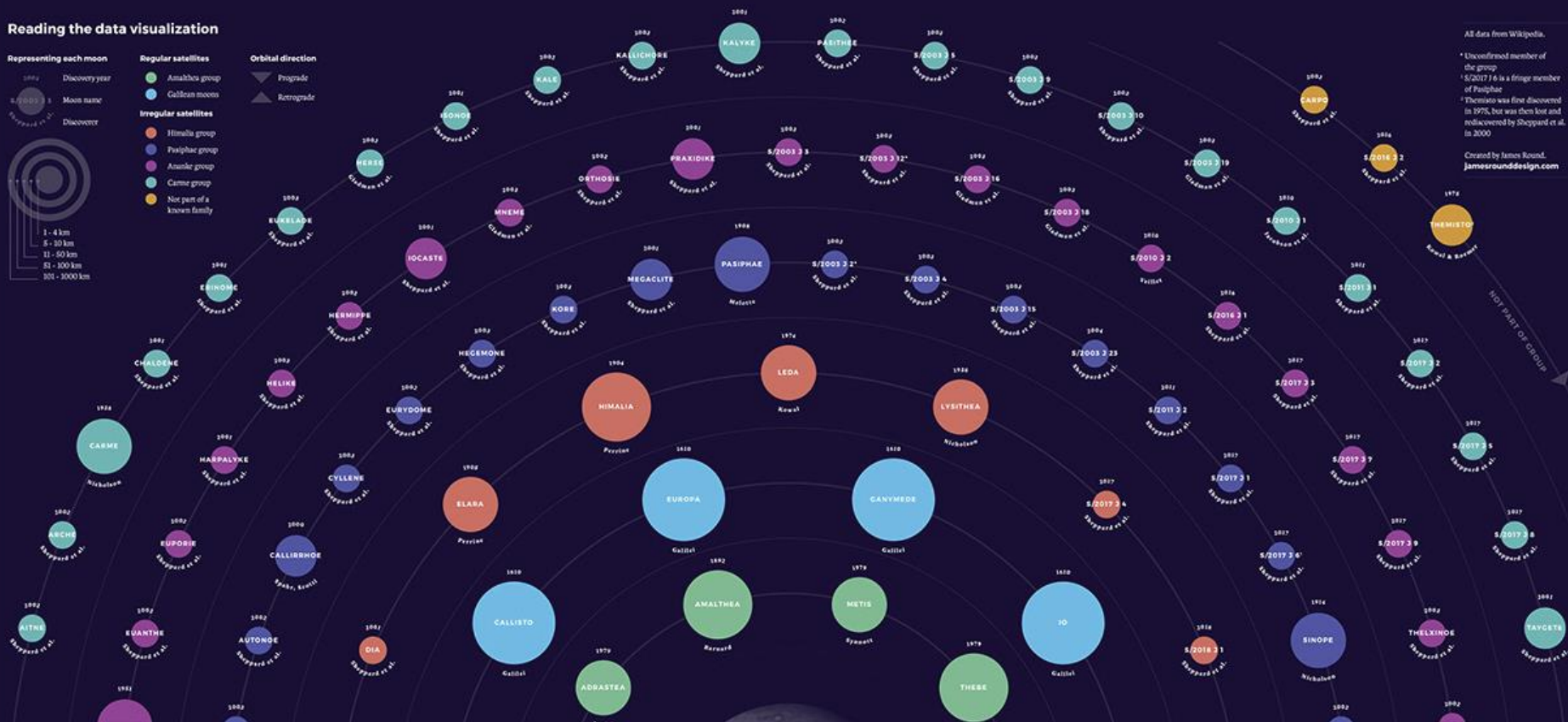
- Himalia group
- Pasiphae group
- Ananke group
- Carme group
- Not part of a known family

**Orbital direction**

- Prograde
- Retrograde

**Scale**

- 1 - 4 km
- 5 - 30 km
- 31 - 50 km
- 51 - 100 km
- 101 - 1000 km



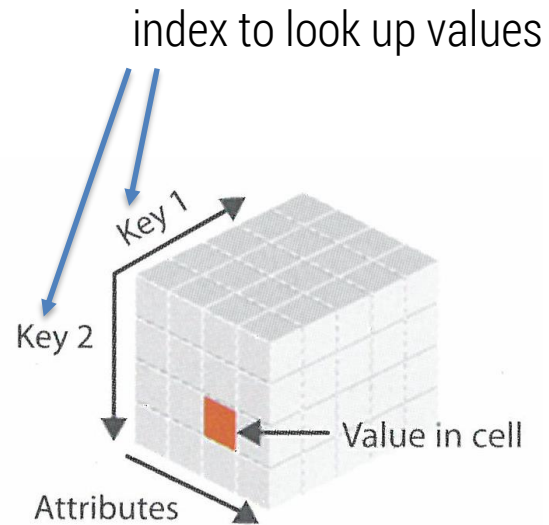
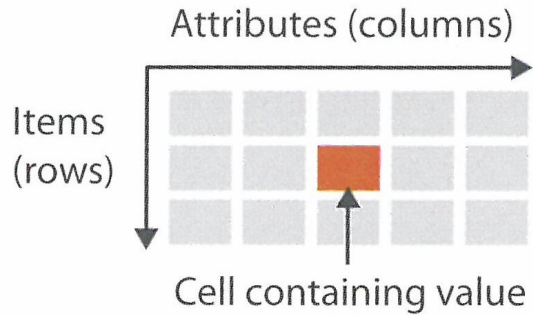
All data from Wikipedia.

\* Unconfirmed member of the group  
\* S/2017 16 is a fringe member of Pasiphae  
\* Themisto was first discovered in 1975, but was then lost and rediscovered by Sheppard et al. in 2000

Created by James Round, Jamesrounddesign.com

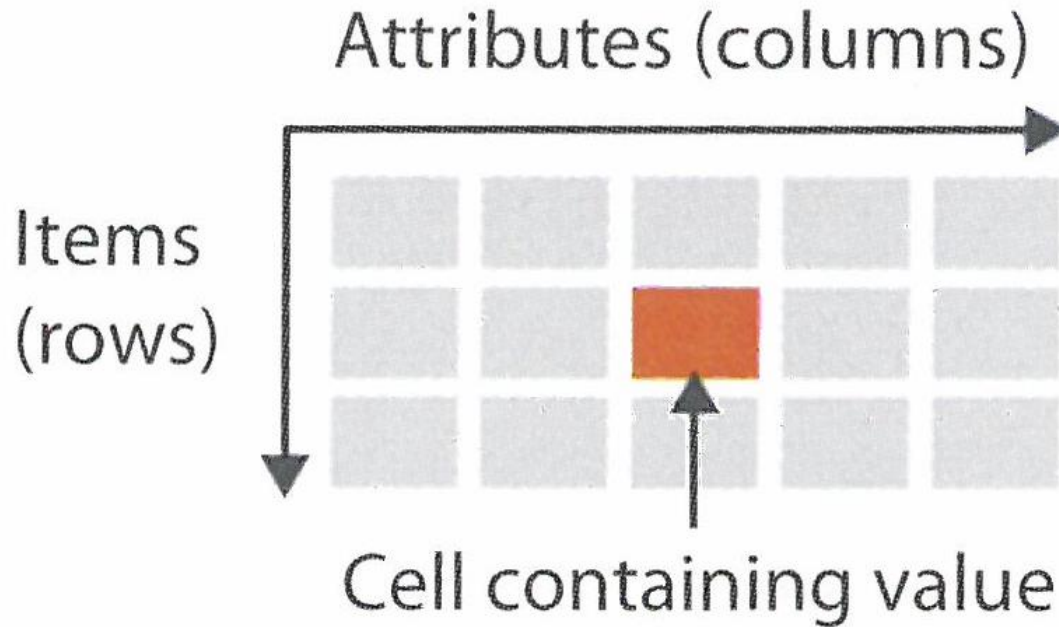
**BACK TO THE BASICS**

# DATA TABLES - TERMINOLOGY

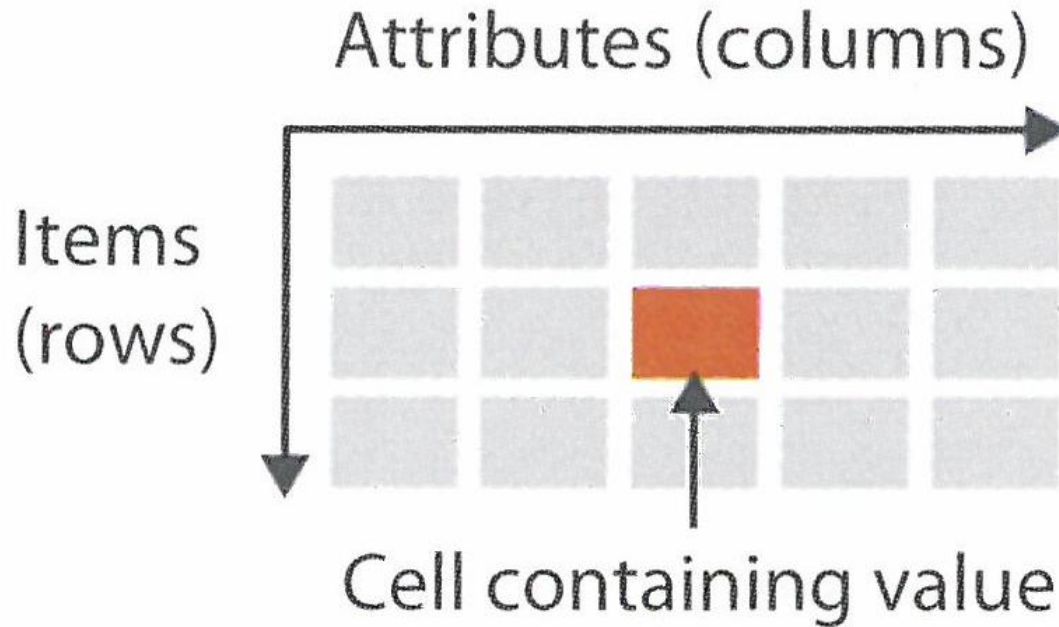




# WHAT COULD BE THE KEY HERE?



# WHAT DATA TYPE IS SUITABLE FOR A KEY?



# KEYS VS. VALUES

key attributes are also sometimes called:

- independent attribute
- dimension

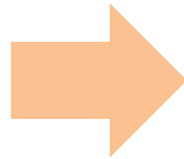
value attributes are also sometimes called:

- dependent attribute
- measure

# LEVELS

= unique values for a categorical or ordered attribute

Conference	Year	Paper.Title
InfoVis	2015	A comparative study ...
InfoVis	2015	A Linguistic Approach...
InfoVis	2015	A Psychophysical Inv...
InfoVis	2015	A Simple Approach fo...
InfoVis	2015	Acquired Codes of Me...
InfoVis	2015	AggreSet: Rich and Sc...
InfoVis	2015	AmbiguityVis: Visuali...
InfoVis	2015	Automatic Selection ...
InfoVis	2015	Beyond Memorability...
InfoVis	2015	Beyond Weber's Law:...
InfoVis	2015	Evaluation of Parallel...
InfoVis	2015	Guidelines for Effecti...
InfoVis	2015	High-Quality Ultra-Co...
InfoVis	2015	HOLA: Human-like Ort...
InfoVis	2015	How do People Make ...



CONFERENCE:  
InfoVis, Vis, SciVis, VAST

YEAR:  
1990 – 2015

PAPER.TITLE:  
>2500 different

# VISPUBDATA

## ATTRIBUTES

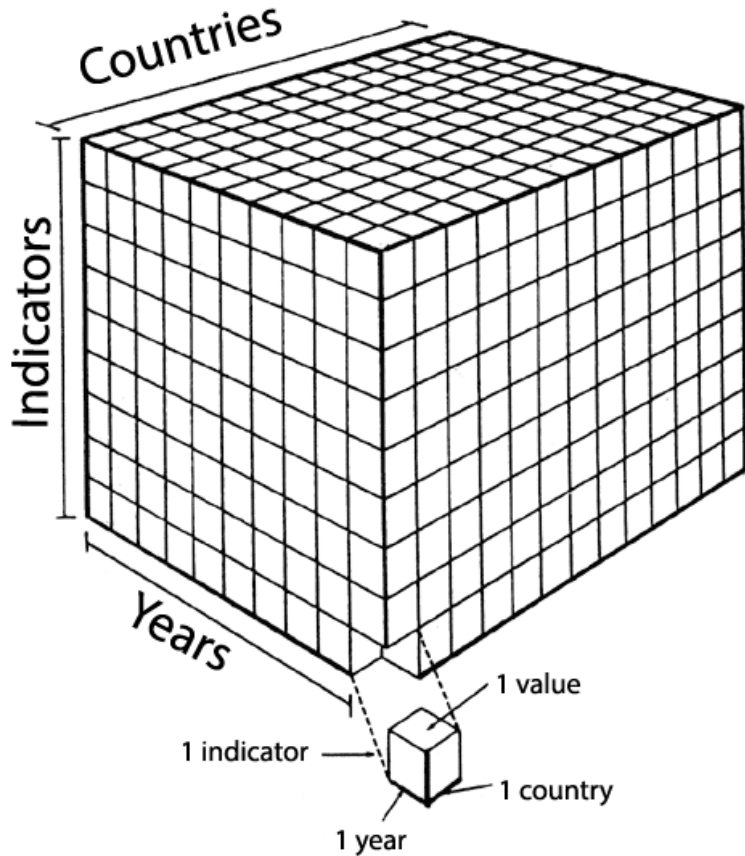


## ITEMS

#	Abc	Abc	Abc	Abc	#	#	Abc	Abc	Abc	Abc	Abc	Abc	Abc	Abc
Year	Paper.Title	Paper.DOI	Link	First.page	Last.page	Paper.type..C.conf...	Abstract	Author.Names	First.Author.Affilia...	Deduped.author.n...	References	Author.Keywords	OCR.Authors	
2015	A comparative study ...	10.1109/TVCG.2015...	http://dx.doi.org/10...	619	628	J	RadViz and star coord...	Rubio-Sanchez, M.;Ra...	;;	Rubio-Sanchez, M.,Ra...	10.1109/VAST.2010...	RadViz, Star coordina...	Rubio-S ´ Anchez, Ma...	
2015	A Linguistic Approach...	10.1109/TVCG.2015...	http://dx.doi.org/10...	698	707	J	When data categorie...	Setlur, V.,Stone, M.C.	;	Setlur, V.,Stone, M.C.	null	linguistics, natural la...	Setlur,Vidya;Stone,M...	
2015	A Psychophysical Inv...	10.1109/TVCG.2015...	http://dx.doi.org/10...	479	488	J	Physical visualization...	Jansen, Y.;Hornbaek, K.	Univ. of Copenhagen, ...	Jansen, Y.;Hornbaek, K.	10.1109/TVCG.2012...	Data physicalization, ...	Jansen,Yvonne;Hornb...	
2015	A Simple Approach fo...	10.1109/TVCG.2015...	http://dx.doi.org/10...	678	687	J	General methods for ...	Simonetto, P.,Archam...	;;	Simonetto, P.,Archam...	10.1109/TVCG.2011...	Euler diagrams, Boun...	Simonetto,Paolo;Arc...	
2015	Acquired Codes of Me...	10.1109/TVCG.2015...	http://dx.doi.org/10...	509	518	J	While information vis...	Byrne, L.;Angus, D.;W...	;;	Byrne, L.;Angus, D.;W...	10.1109/TVCG.2013...	Visual Design, Taxono...	Byrne,Lydia;Angus,D...	
2015	AggreSet: Rich and Sc...	10.1109/TVCG.2015...	http://dx.doi.org/10...	688	697	J	Datasets commonly i...	Yalcin, M.A.;Elmqvist...	Univ. of Maryland, Co...	Yalcin, M.A.;Elmqvist...	10.1109/TVCG.2011...	Multi-valued attribut...	Adil Yalcin, M;Beders...	
2015	AmbiguityVis: Visuali...	10.1109/TVCG.2015...	http://dx.doi.org/10...	359	368	J	Node-link diagrams p...	Yong Wang,Qiaomu S...	;;;;;	Yong Wang,Qiaomu S...	10.1109/TVCG.2006...	Visual Ambiguity, Vis...	Wang,Yong;Shen,Qia...	
2015	Automatic Selection ...	10.1109/TVCG.2015...	http://dx.doi.org/10...	669	677	J	Effective small multi...	Anand, A.,Talbot, J.	;	Anand, A.;Talbot, J.	10.1109/VAST.2010...	Small multiple displa...	Anand,Anushka,Talbo...	
2015	Beyond Memorability...	10.1109/TVCG.2015...	http://dx.doi.org/10...	519	528	J	In this paper we mov...	Borkin, M.A.;Bylinskii...	;;;;;	Borkin, M.;Bylinskii, Z...	10.1109/TVCG.2012...	Information visualiza...	null	
2015	Beyond Weber's Law...	10.1109/TVCG.2015...	http://dx.doi.org/10...	469	478	J	Models of human per...	Kay, M.;Heer, J.	;	Kay, M.;Heer, J.	10.1109/TVCG.2014...	Weber's law, percept...	Kay,Matthew;Heer,Je...	
2015	Evaluation of Parallel...	10.1109/TVCG.2015...	http://dx.doi.org/10...	579	588	J	The parallel coordina...	Johansson, J.;Forsell...	Norrkoping Visualiza...	Johansson, J.;Forsell...	10.1109/TVCG.2014...	Survey, evaluation, g...	Johansson,Jimmy;For...	
2015	Guidelines for Effecti...	10.1109/TVCG.2015...	http://dx.doi.org/10...	489	498	J	Semi-automatic text ...	Strobelt, H.;Oelke, D.;...	;;;	Strobelt, H.,Oelke, D.;...	10.1109/TVCG.2012...	Text highlighting tec...	Strobelt,Hendrik;Oel...	
2015	High-Quality Ultra-Co...	10.1109/TVCG.2015...	http://dx.doi.org/10...	339	348	J	Prior research into ne...	Yoghourdijan, V.;Dwy...	;;;;;	Yoghourdijan, V.;Dwy...	10.1109/TVCG.2008...	Network visualizatio...	Yoghourdijan,Vahan;	
2015	HOLA: Human-like Ort...	10.1109/TVCG.2015...	http://dx.doi.org/10...	349	358	J	Over the last 50 year...	Kieffer, S.;Dwyer, T.;...	;;;	Kieffer, S.;Dwyer, T.;...	10.1109/TVCG.2006...	Graph layout, orthog...	Kieffer,Steve;Dwyer,...	
2015	How do People Make ...	10.1109/TVCG.2015...	http://dx.doi.org/10...	499	508	J	In this paper, we wou...	Sukwon Lee,Sung-He...	Sch. of Ind. Eng., Purd...	Sukwon Lee,Sung-He...	10.1109/TVCG.2013...	Sensemaking model, l...	Lee,Sukwon;Kim,Sun...	
2015	Improving Bayesian R...	10.1109/TVCG.2015...	http://dx.doi.org/10...	529	538	J	Decades of research ...	Ottley, A.;Peck, E.M.;...	;;;;;	Ottley, A.;Peck, E.M.;...	10.1109/TVCG.2014...	Bayesian Reasoning, ...	Ottley,Alvitta;Peck,E...	
2015	Matches, Mismatche...	10.1109/TVCG.2015...	http://dx.doi.org/10...	449	458	J	The energy performa...	Brehmer, M.;Ng, J.,Ta...	;;;	Brehmer, M.,Ng, J.,Ta...	10.1109/TVCG.2011...	Design study, design ...	Brehmer,Matthew;N...	



# THE DATA CUBE



Country	Year	Child mortality	Births per woman
Afghanistan	2014	68.1	4.8
Afghanistan	2013	69.9	5.1
France	2014	3.6	2.0
France	2013	3.6	2.0
USA	2014	5.7	5.9
USA	2013	1.9	1.9

# MULTI-ATTRIBUTE DATA – OUR VIEW TODAY

n x d matrix

n attributes

d items (data points)

Country	Year	Child mortality	Births per woman
Afghanistan	2014	68.1	4.8
Afghanistan	2013	69.9	5.1
France	2014	3.6	2.0
France	2013	3.6	2.0
USA	2014	5.7	5.9
USA	2013	1.9	1.9

# ARRANGING TABULAR DATA

In Space



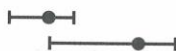
# WHY ARRANGING DATA

## ➔ Magnitude Channels: Ordered Attributes

Position on common scale



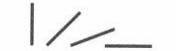
Position on unaligned scale



Length (1D size)



Tilt/angle



Area (2D size)



Depth (3D position)



Color luminance



Color saturation



Curvature



Volume (3D size)



Same

Same

Same

Most  
Effectiveness  
Least

## ➔ Identity Channels: Categorical Attributes

Spatial region



Color hue



Motion



Shape



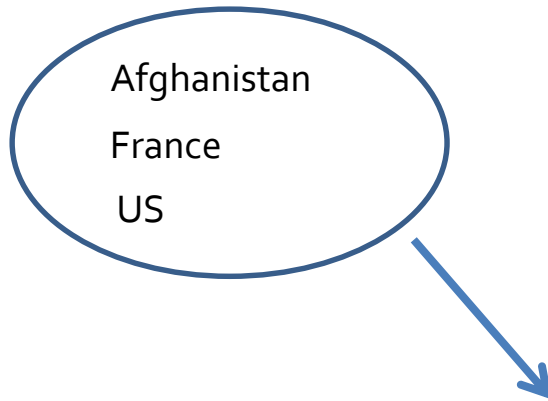
# QUANTITATIVE VALUES

# APPROACH

- Let's start with two attributes:  
country & income per person

Country	Income per person
Afghanistan	850
France	29500
US	41000

# 1. FIND A LAYOUT

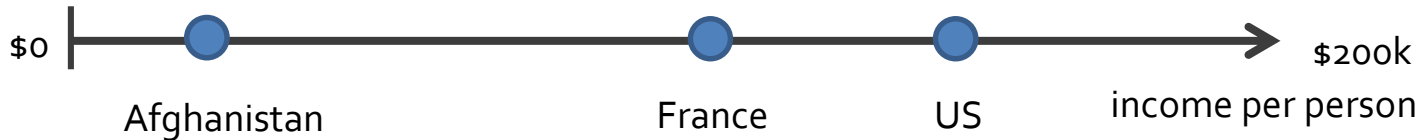


Country	Income per person
Afghanistan	850
France	29500
US	41000



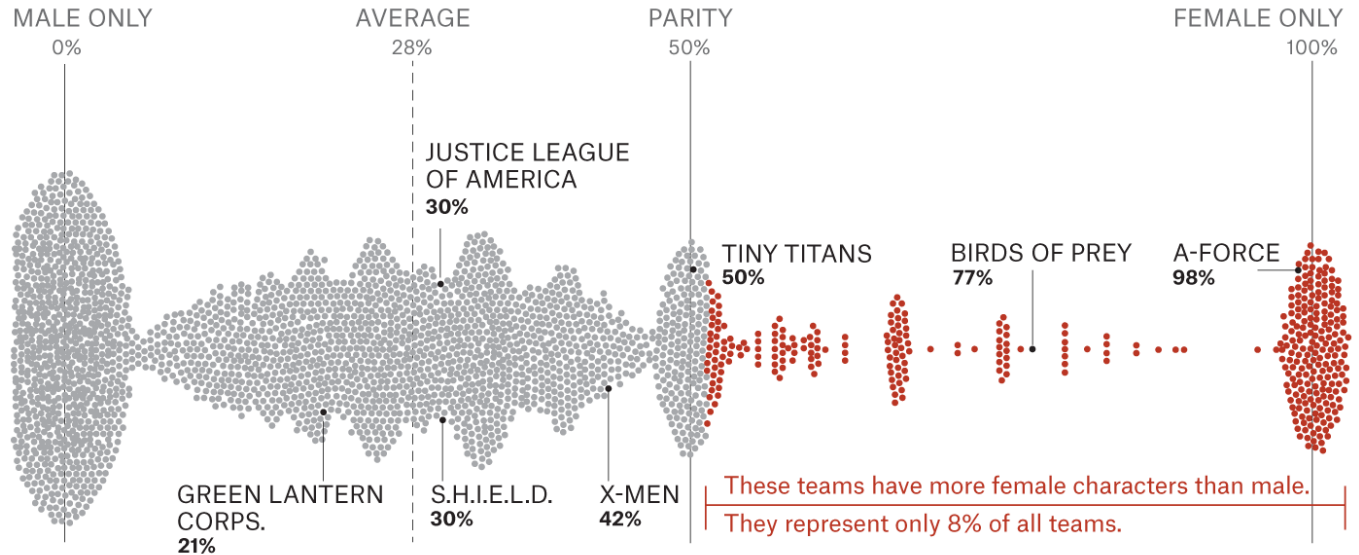
## 2. CHOOSE A VISUAL ENCODING & MARK

E.g. position + circle





# Analyzing the Gender Representation of 34,476 Comic Book Characters

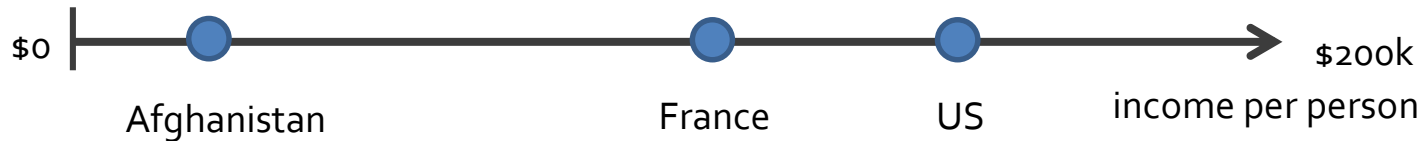


Female percentage of every team  
Each dot represents one of 2,862 teams in DC and Marvel.

# 1. FIND A LAYOUT

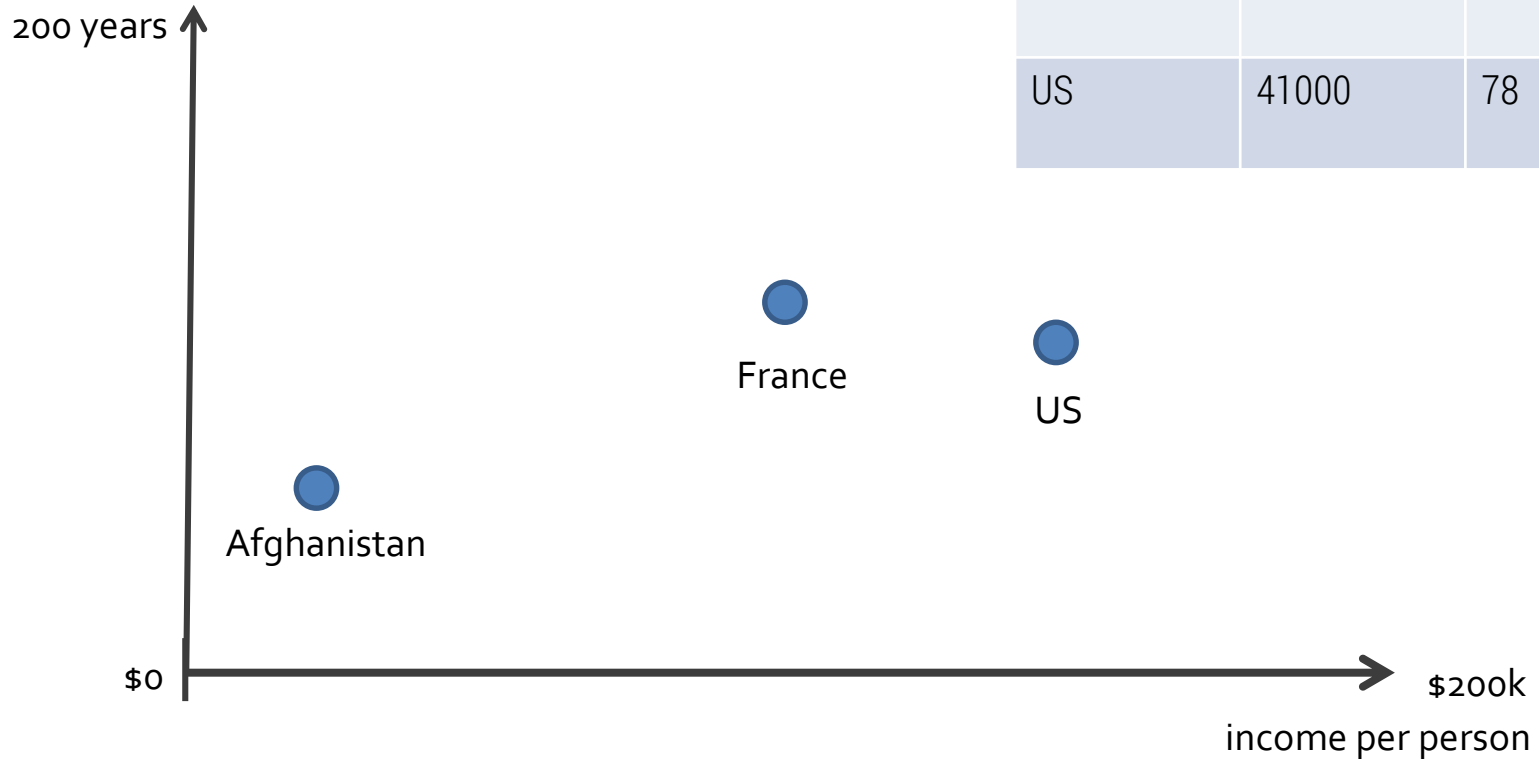
Country	Income per person	Life expectancy
Afghanistan	850	57
France	29500	81
US	41000	78

How do we extend this to 3 data attributes?



# 1. FIND A LAYOUT

Country	Income per person	Life expectancy
Afghanistan	850	57
France	29500	81
US	41000	78

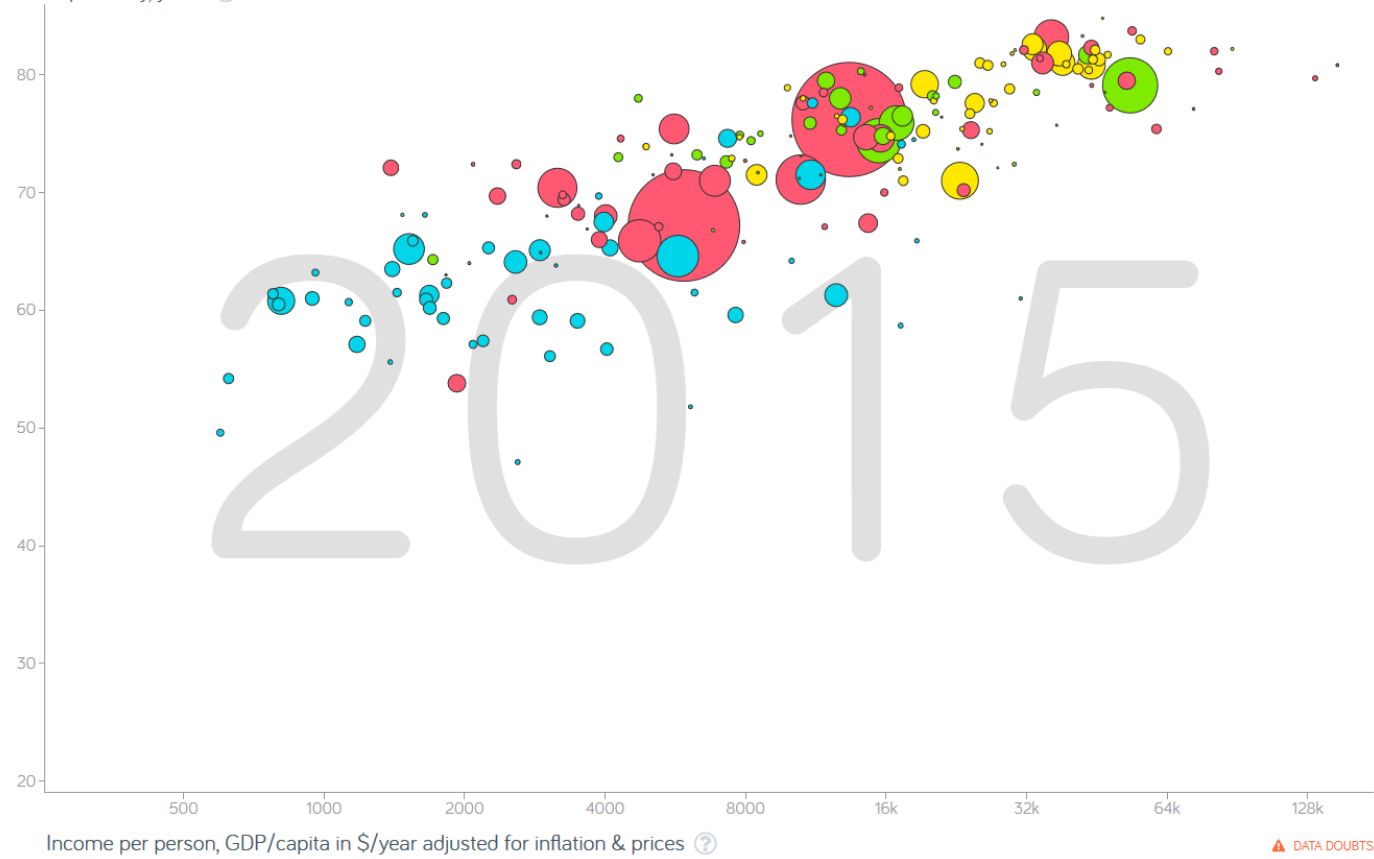




# SCATTERPLOTS

- two quantitative values
- horizontal and vertical spatial dimensions
- mark type = point

Life expectancy, years ?



Color World Regions ?

Select Search...

- Afghanistan
- Albania
- Algeria
- Andorra
- Angola
- Antigua and Barbuda
- Argentina
- Armenia
- Aruba
- Australia
- Austria
- Azerbaijan
- Bahamas
- Bahrain
- Bangladesh
- Barbados
- Belarus
- Belgium
- Belize
- Benin

Size Population ?

Zoom 🔍 🔍 🔍 100%

⚙️ 📏 🖨️

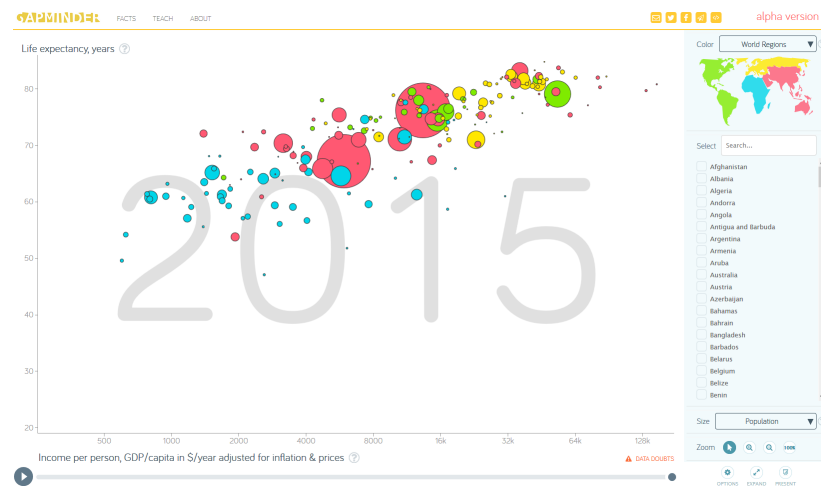
OPTIONS EXPAND PRESENT

when marks are sized, the chart is often called a bubble chart or bubble plot

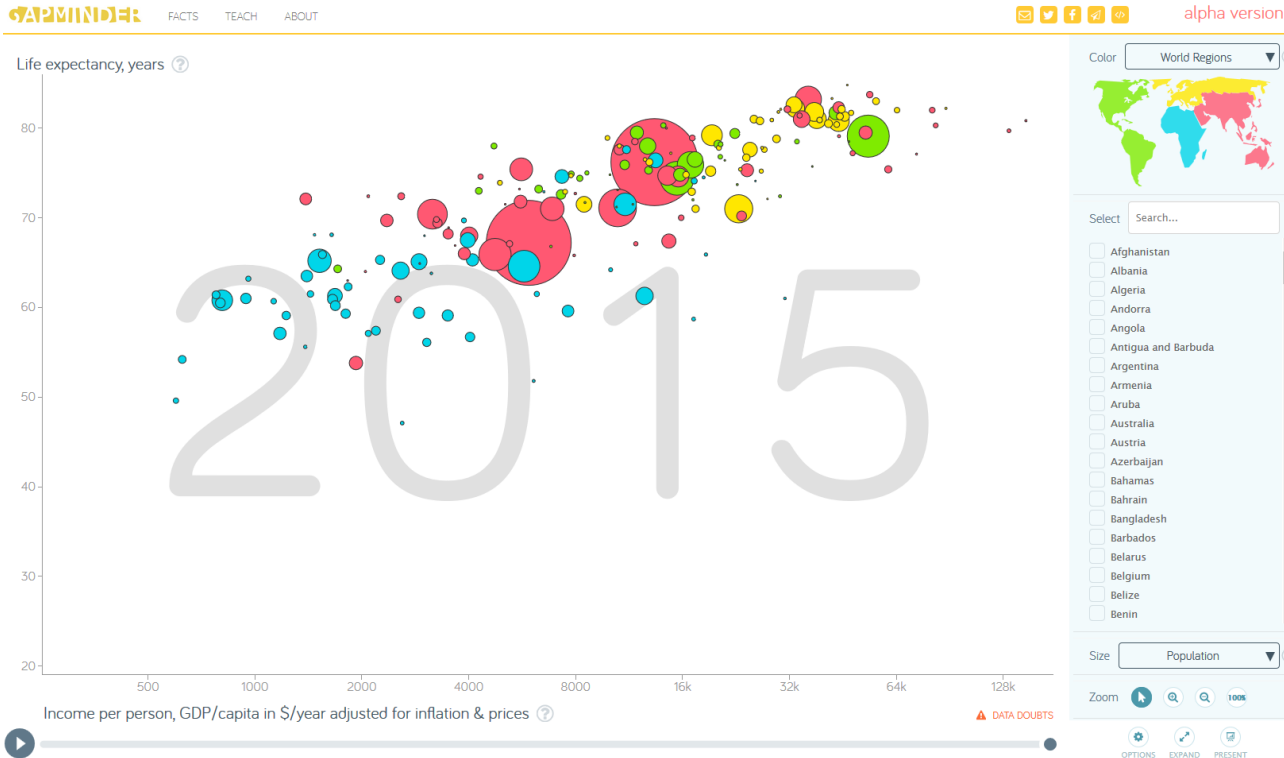


# TASKS

- find trends
- find outliers
- show distribution
- show correlation
- locate clusters



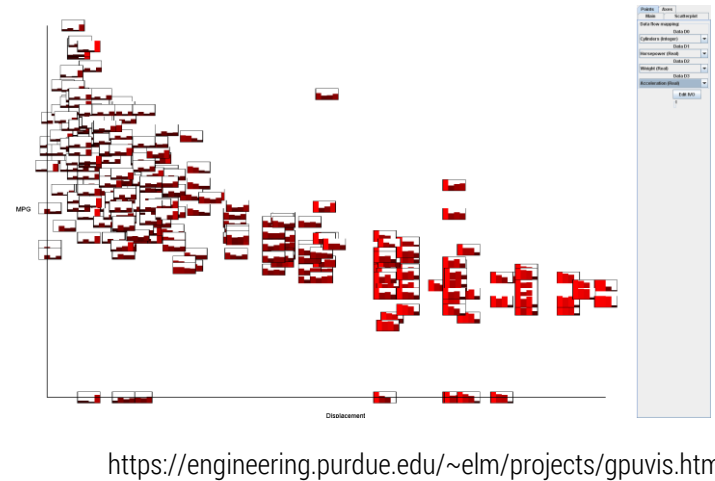
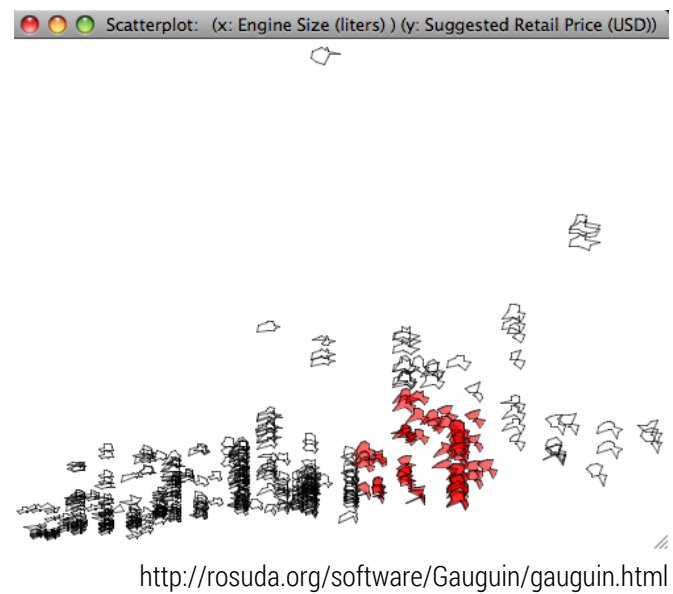
# how many items are reasonable to put on a scatterplot?



# GLYPHS

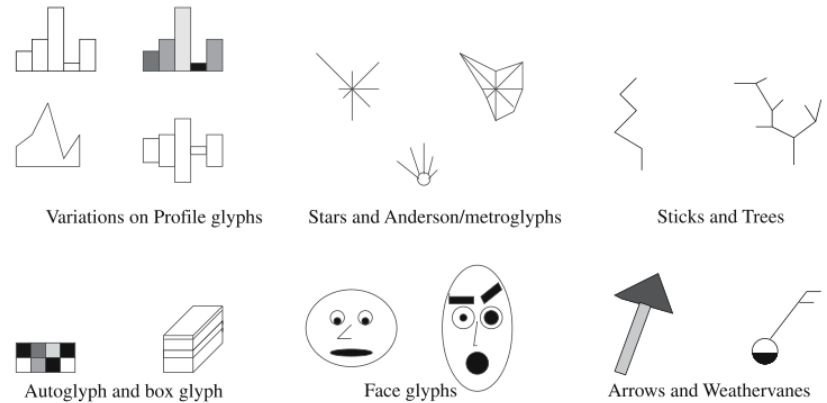
marks can be replaced with glyphs

glyphs are themselves composed of multiple marks



# GLYPHS

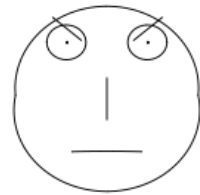
- Small composite visual representations of multi-dimensional data points
- Characterized generally by lack of reference structures (grid lines, axes labels, ...)



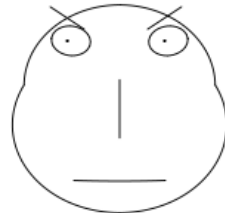
From Ward, 2002

A taxonomy of glyph placement strategies for multidimensional data visualization

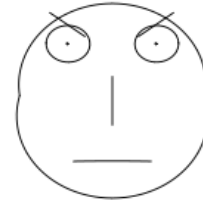
# EXAMPLE: CHERNOFF FACES



AARONSON, L.H.



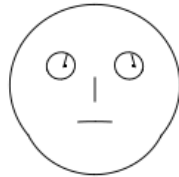
ALEXANDER, J.M.



ARMENTANO, A.J.



BERDON, R.I.



BRACKEN, J.J.



BURNS, E.B.



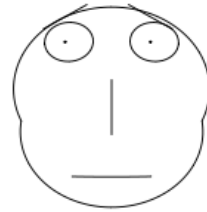
CALLAHAN, R.J.



COHEN, S.S.



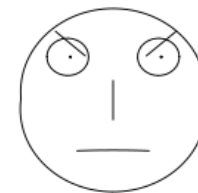
DALY, J.J.



DANNEHY, J.F.



DEAN, H.H.



DEVITA, H.J.

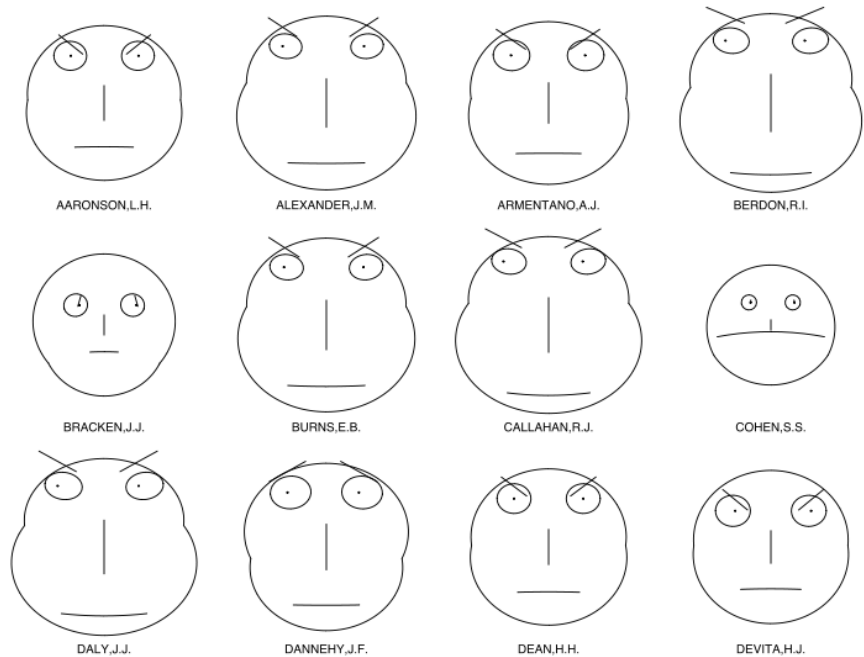
Image source: Wikipedia

Herman Chernoff, [The Use of Faces to Represent Points in K-Dimensional Space Graphically](#), 1973.



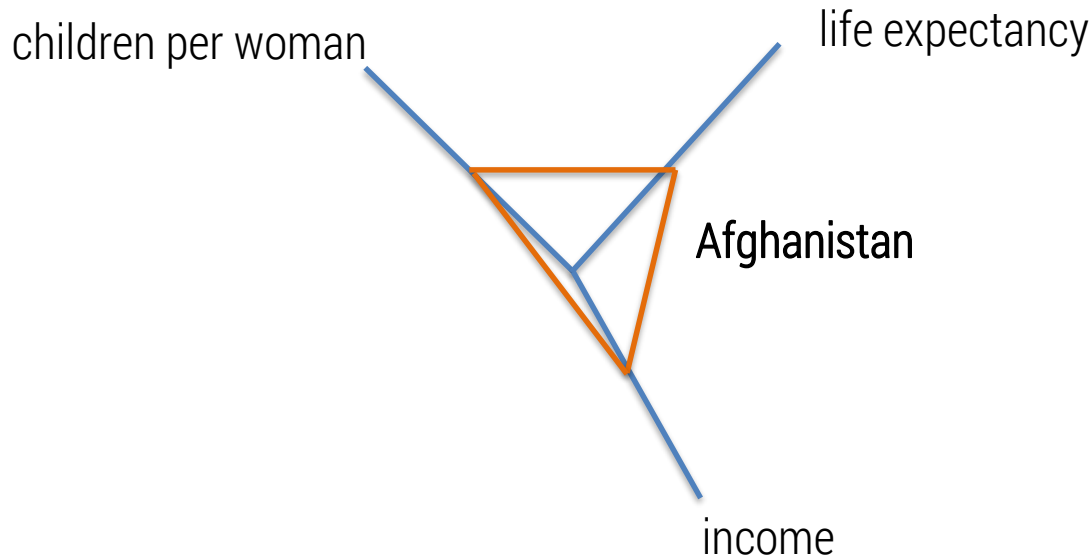
# CHERNOFF FACES

- features of a human face encode data values (e.g. slant of eye brows, size of eyes, ...)
- reasoning: humans are good at differentiating faces and reading face features
- problem: chernoff faces have generally been found not to be very effective



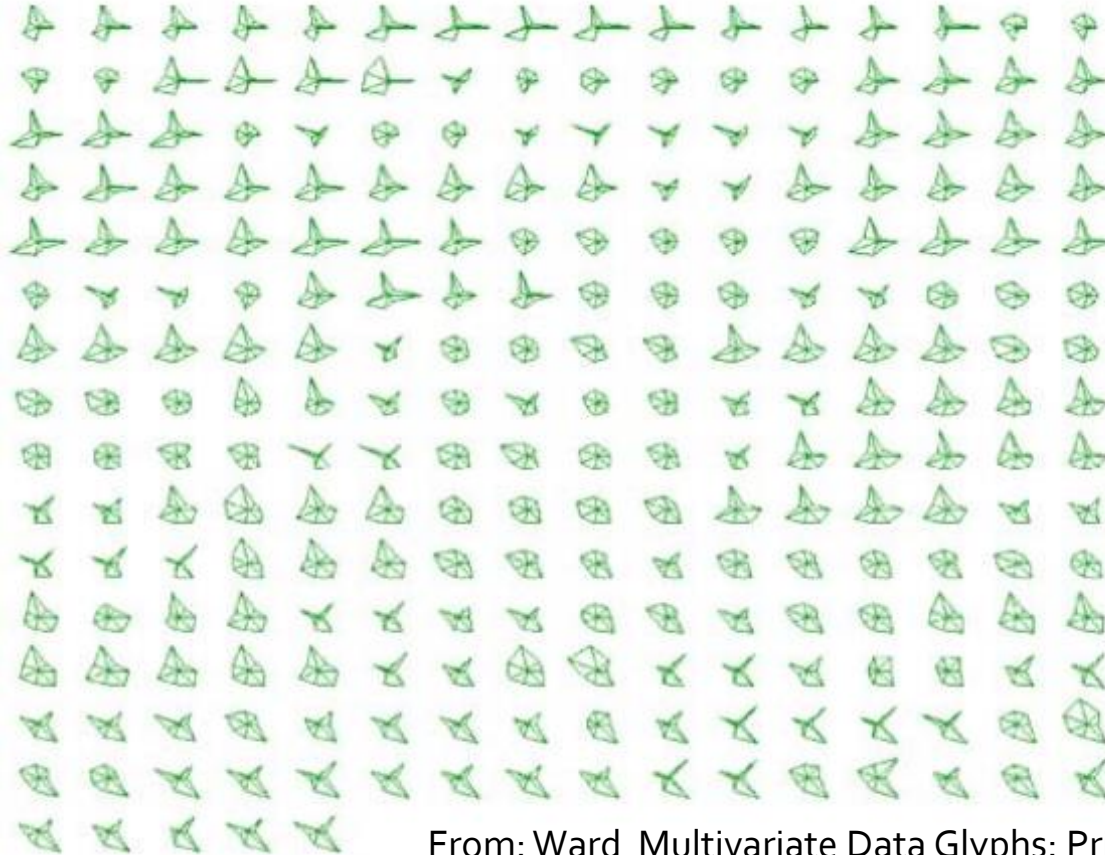
# EXAMPLE: STAR GLYPHS

- Lay out dimension in radial fashion
- Draw each point as a ring



(not real data, here)

# STAR GLYPHS



From: Ward Multivariate Data Glyphs: Principles and Practice. Handbook of Data Visualization (2008)

# It's gettin hot out here

<http://www.studioterp.nl/its-gettin-hot>

## 2015: WARMEST DECEMBER

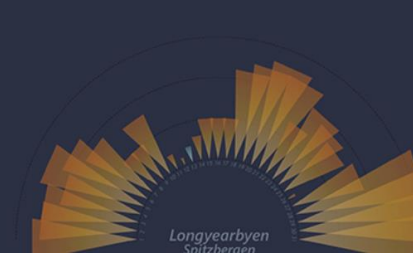
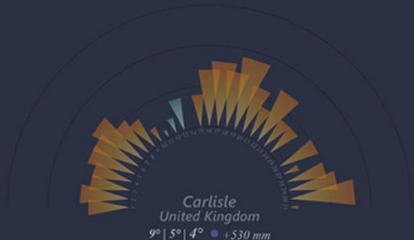
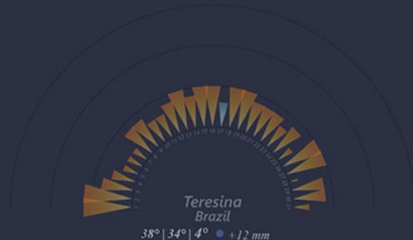
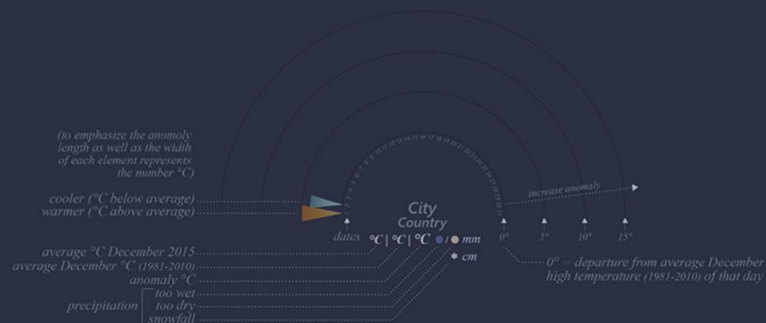
HOW TO READ IT

Across the globe, record warm temperatures were observed over every continent, including a large swath of eastern North America, southern Mexico through northern South America, western and central Europe, most of southern Africa, parts of central and southeastern Asia, and a large section of southeastern Australia.

The link between the tumultuous weather events experienced around the world in December is likely to be down to the natural phenomenon known as El Niño making the effects of man-made climate change worse. The 2015 El Niño is one of the strongest on record, leading to record temperatures, rainfall and weather extremes.

During December, the globally-averaged land surface temperature was almost 2°C above the 20th century average. This was the highest for December in the 1880–2015 record, surpassing the previous record of 2006 by 0.5°C. The December temperature departure from average was also the highest departure among all months in the historical record and the first time a monthly departure has reached little over +1°C from the 20th century average.

This visualization shows 8 places around the globe chosen for their location in areas where anomalies occurred. Shown are the number of °C departing from the average temperature of each December day.



# SHOW CATEGORICAL REGIONS

Separate, Order, and Align

# CATEGORICAL VALUES

- spatial position is an ordered magnitude visual channel
- categorical attributes are unordered identities (no magnitude)
- cannot be encoded with spatial position
- BUT: can be differentiated with a spatial region

# REGIONS

- contiguous bounded areas
- distinct from one another
- need to be separated, ordered, and aligned



# LIST ALIGNMENT

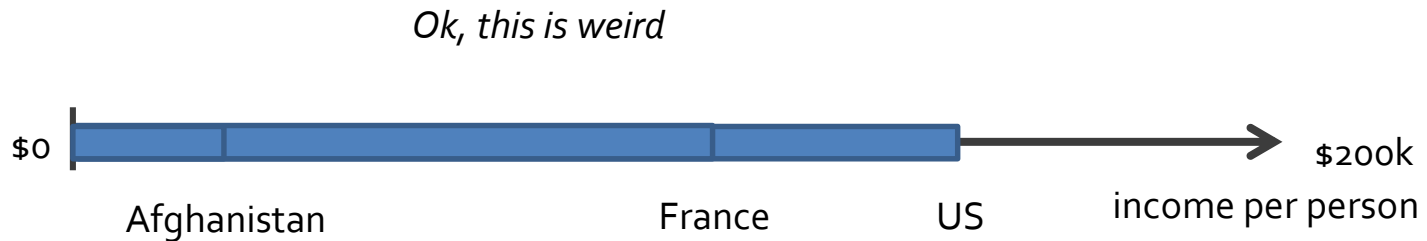
ONE KEY



# LIST ALIGNMENT

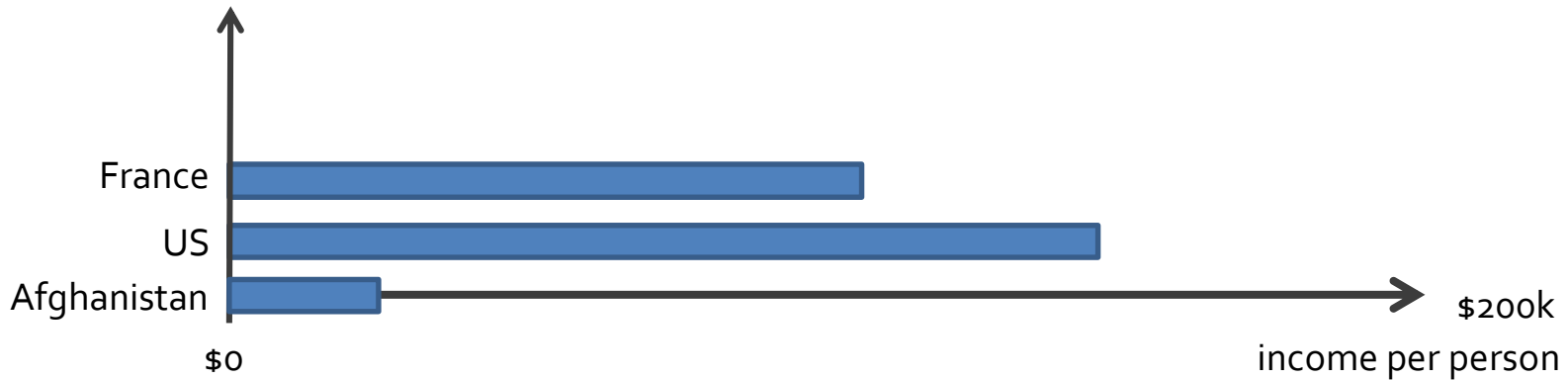
separate into regions by key

E.g. length + rectangle



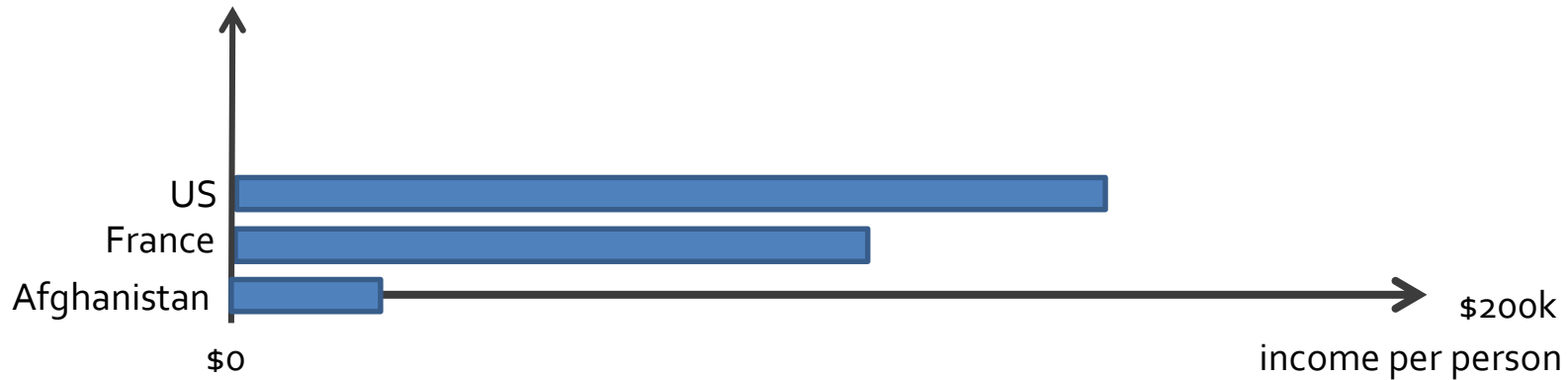
# ALIGN

align regions of key categorical values along one axis in a common frame



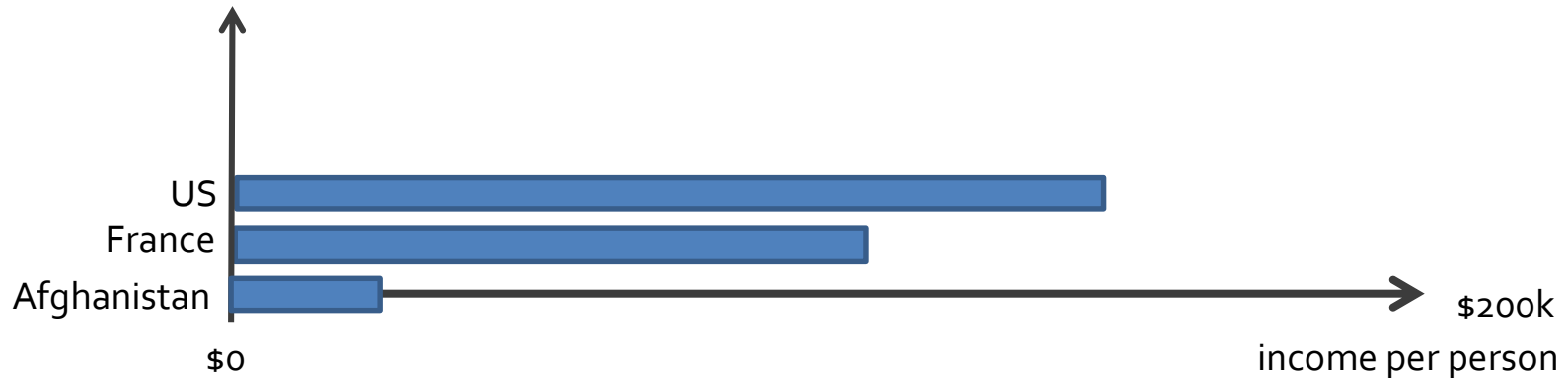
# ORDER

- using a derived attribute such as alphabet
- and/or using dependent data values

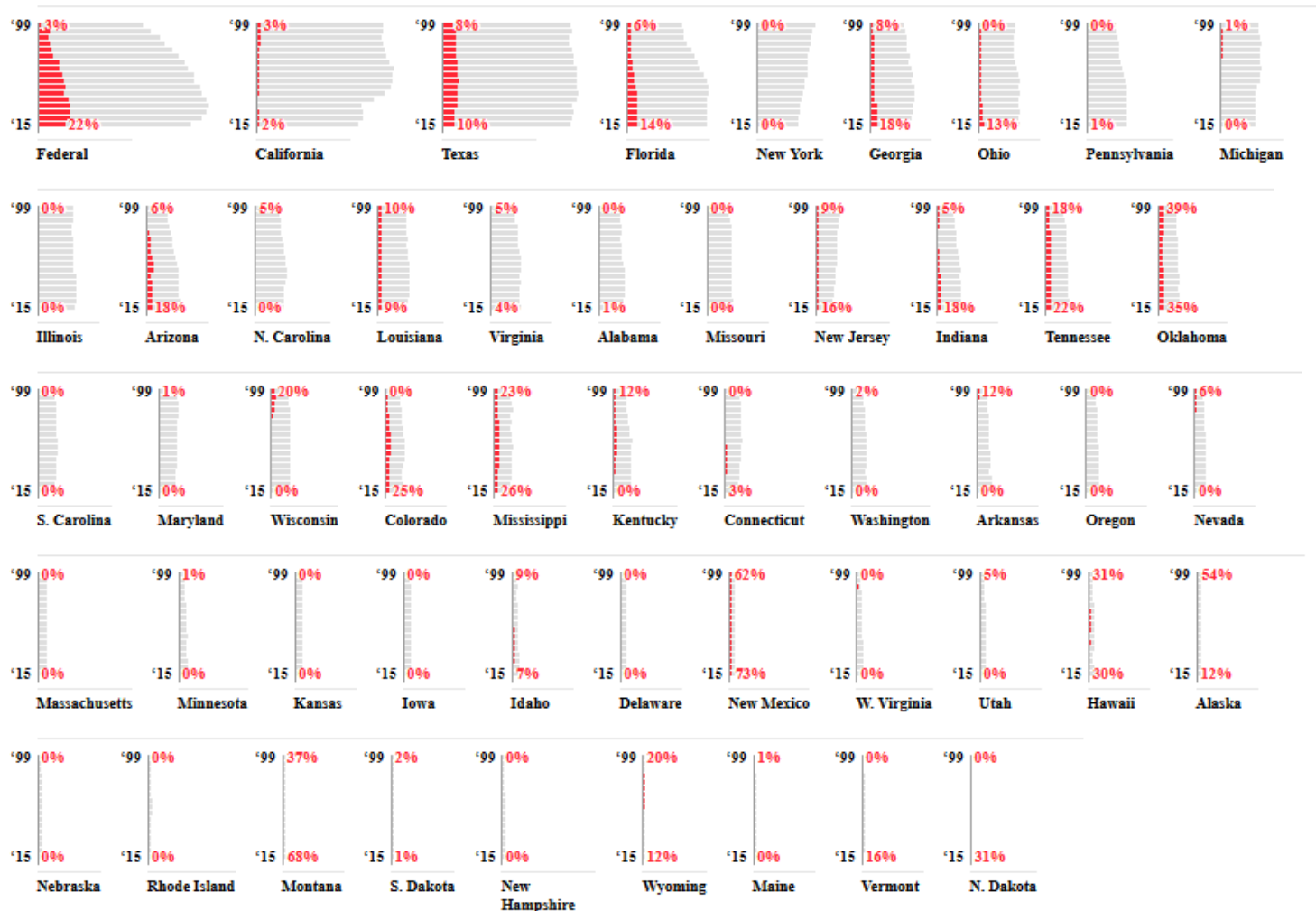


# BAR CHARTS

DATA	one quantitative value attribute, one categorical key attribute
ENCODE	line marks, express value attribute with aligned vertical position (length), separate key attribute with horizontal position
TASK	lookup and compare values
SCALE	key attribute: dozens to hundreds of levels

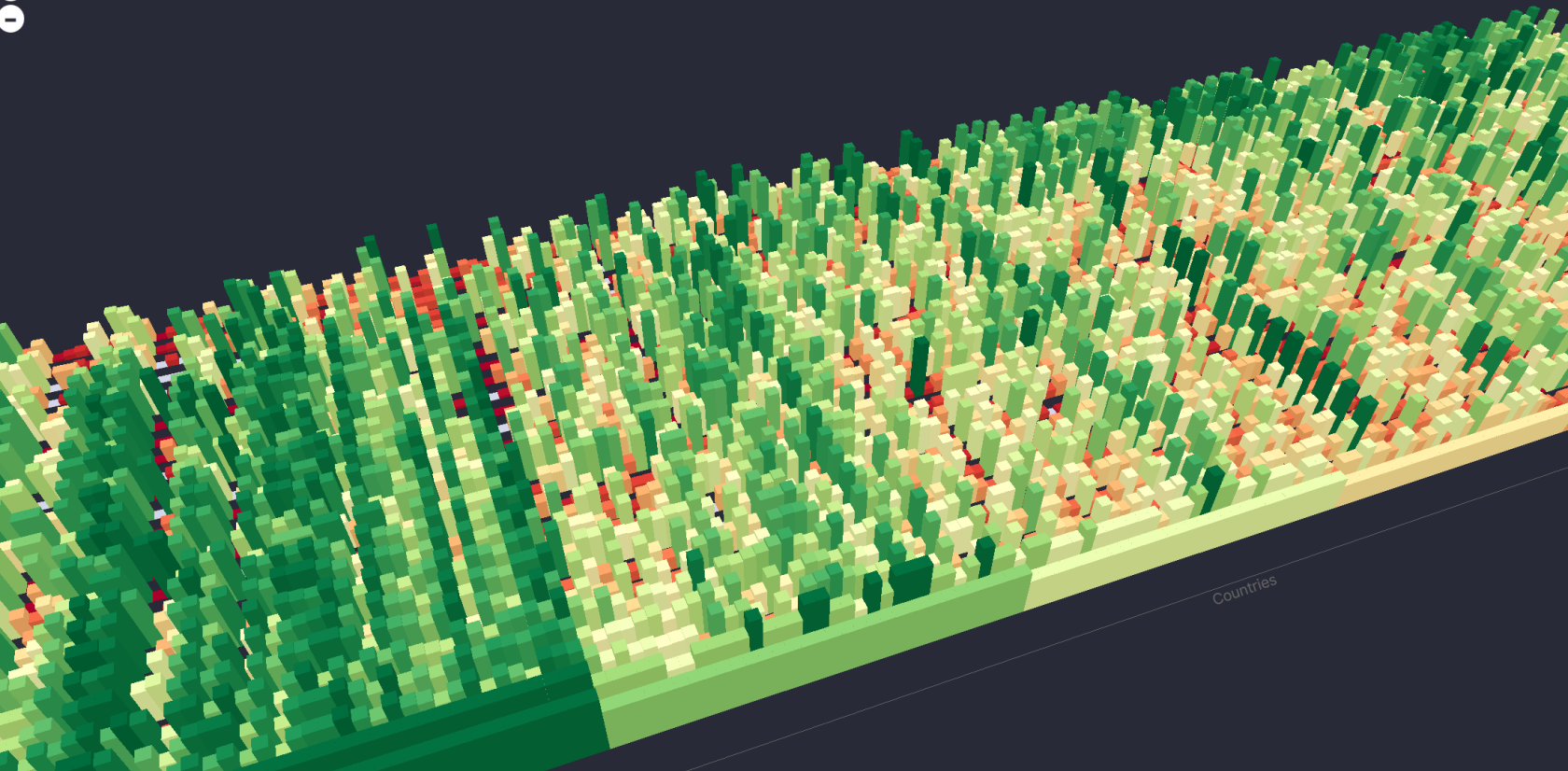


US Inmates held in **Private** vs. **Public** Prisons, by Jurisdiction



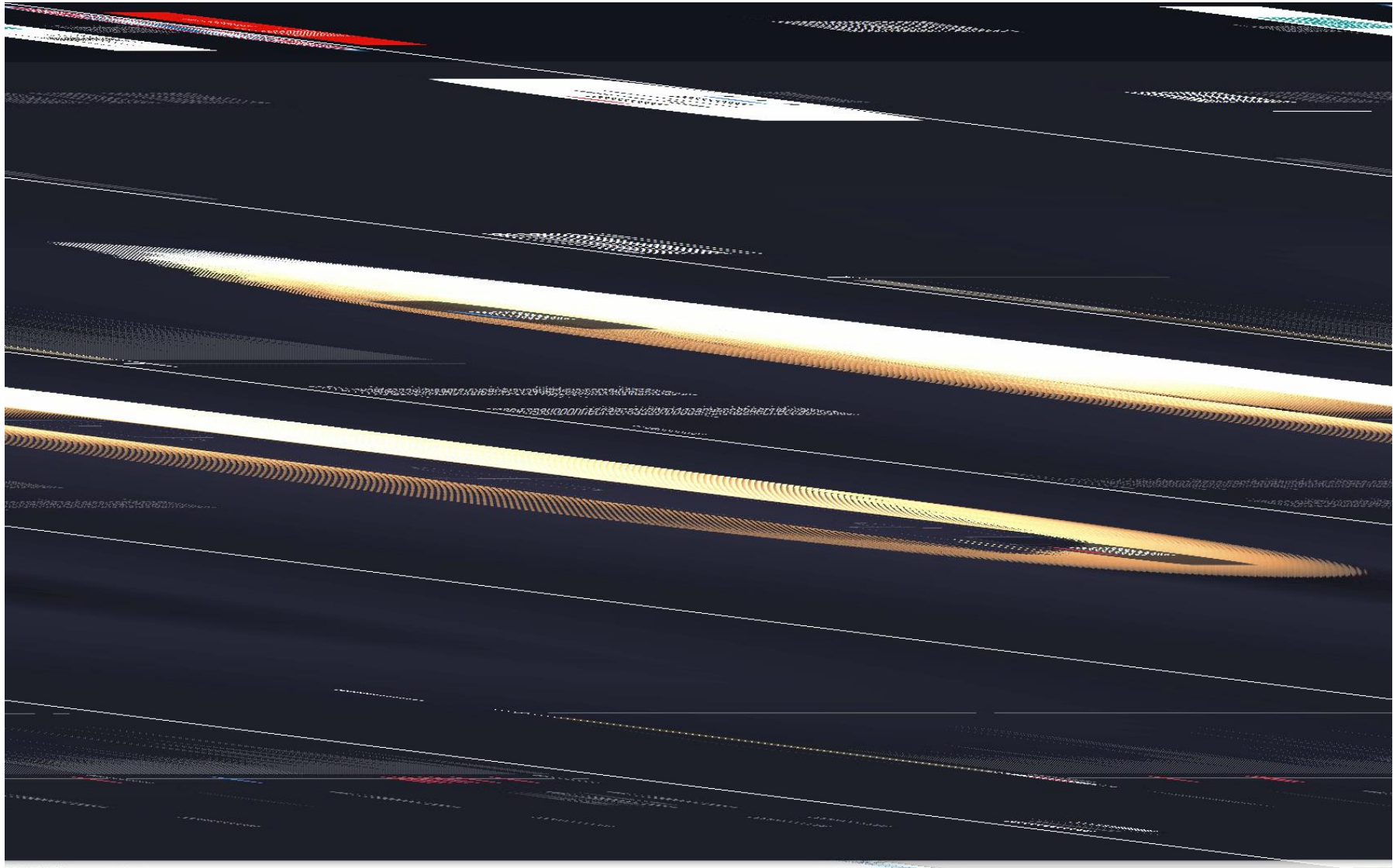
<https://pudding.cool/2017/03/incarceration/index.html>

[Source](#) | [Download Data](#)



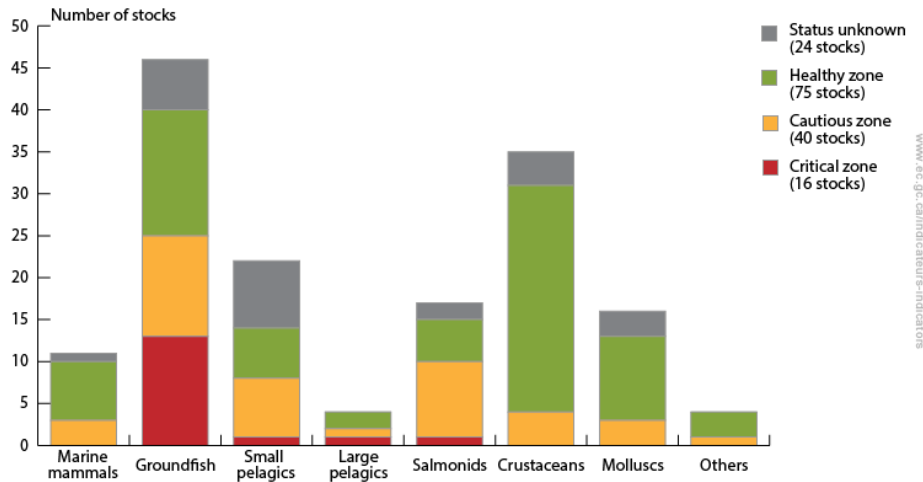
Percentile Value  
Red = Green Continents

- 1. **civil liberties score**  
*out of 7 (lower = better)*  
*Source: Freedom House, 2017*
- 2. political rights score
- 3. rule of law
- 4. control of corruption
- 5. political stability & absence of violence
- 6. regulatory quality
- 7. government effectiveness
- 8. government integrity score
- 9. human development index
- 10. health expenditure per person
- 11. financial freedom score
- 12. health expenditure % of GDP
- 13. property rights score
- 14. overall economic freedom score
- 15. judicial effectiveness score
- 16. government spending score
- 17. school life expectancy (years)
- 18. tax burden score
- 19. GDP per capita (PPP)
- 20. sustainable economic development assessment
- 21. government expenditure (% of GDP)
- 22. women MPs (% of all MPs)
- 23. GDP (billions PPP)
- 24. unemployment (%)
- 25. GDP growth (annual %)
- 26. population
- 27. surface area (km<sup>2</sup>)



<https://reimaginethegame.economist.com>

# ALTERNATIVE



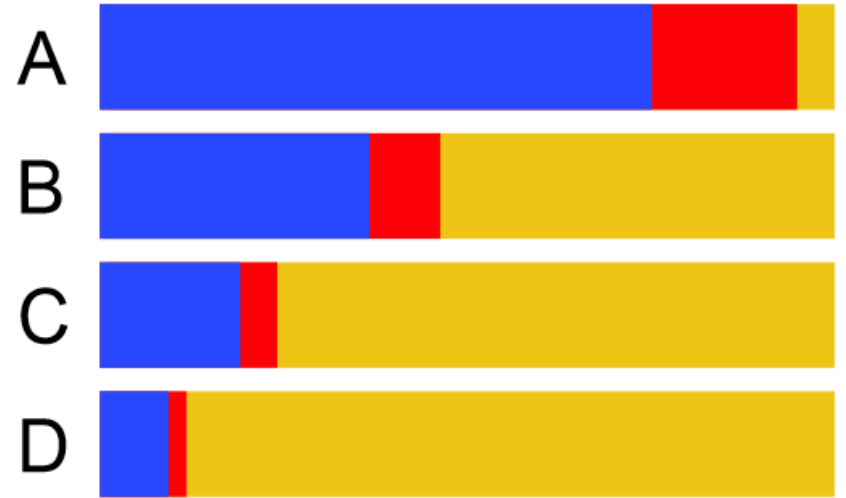
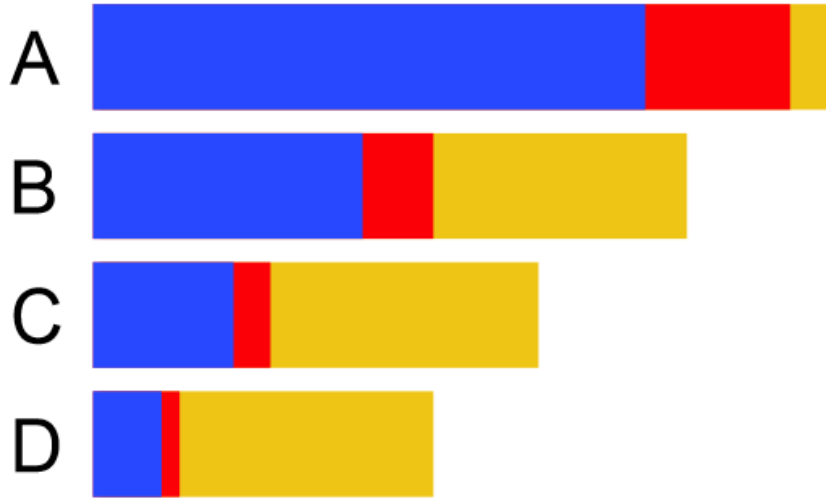
<https://www.ec.gc.ca/indicateurs-indicators/default.asp?lang=en&n=1BCD421B-1>

## Stacked bar chart

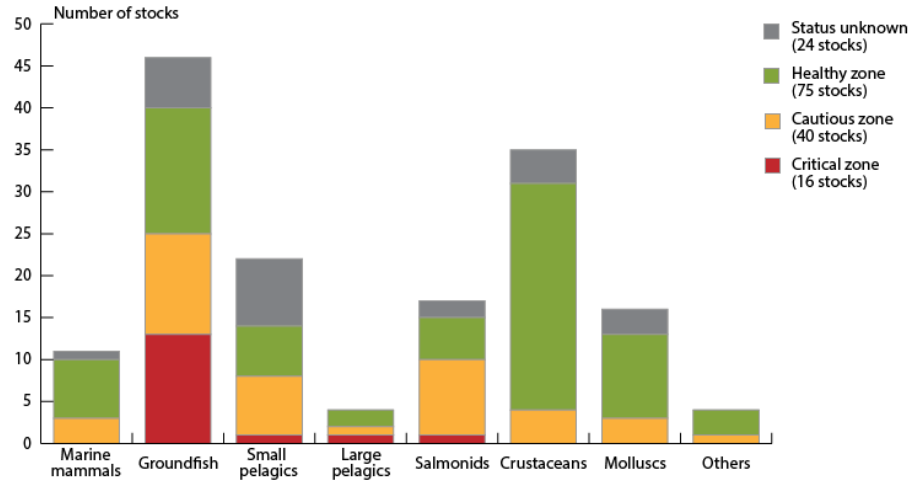
- each bar is a composite glyph
- each bar part encodes a value
- composite glyphs arranged as a list according to primary key
- color used to distinguish secondary key
- typically used for absolute values (use a normalized stacked bar for proportions)



# STACKED BARS VS. NORMALIZED STACKED BARS



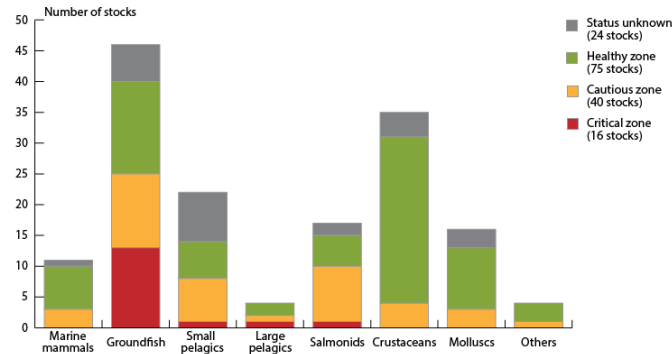
# STACKED BARS



- ADVANTAGE
  - can compare totals and lowest level well
- DISADVANTAGE
  - upper levels of secondary key require comparison against non-aligned scale

# STACKED BARS

DATA	MD table; one quantitative value attribute, two categorical key attributes
ENCODE	bar glyph: length-encoded subcomponents for each level of secondary key attribute separate bars by category of primary key
TASK	part-to-whole relationship, lookup values, find trends
SCALE	key attribute (main axis): dozens to hundreds of levels key attribute (stacked glyph axis): several to one dozen





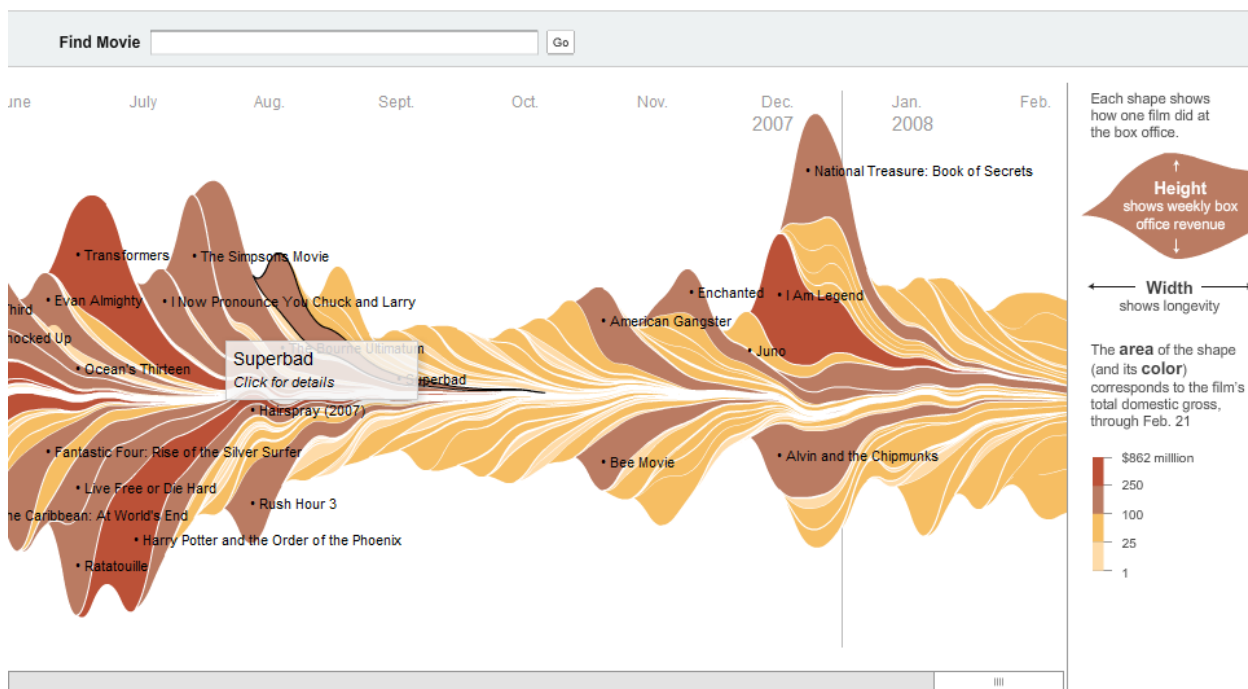
# STREAMGRAPH

February 23, 2008

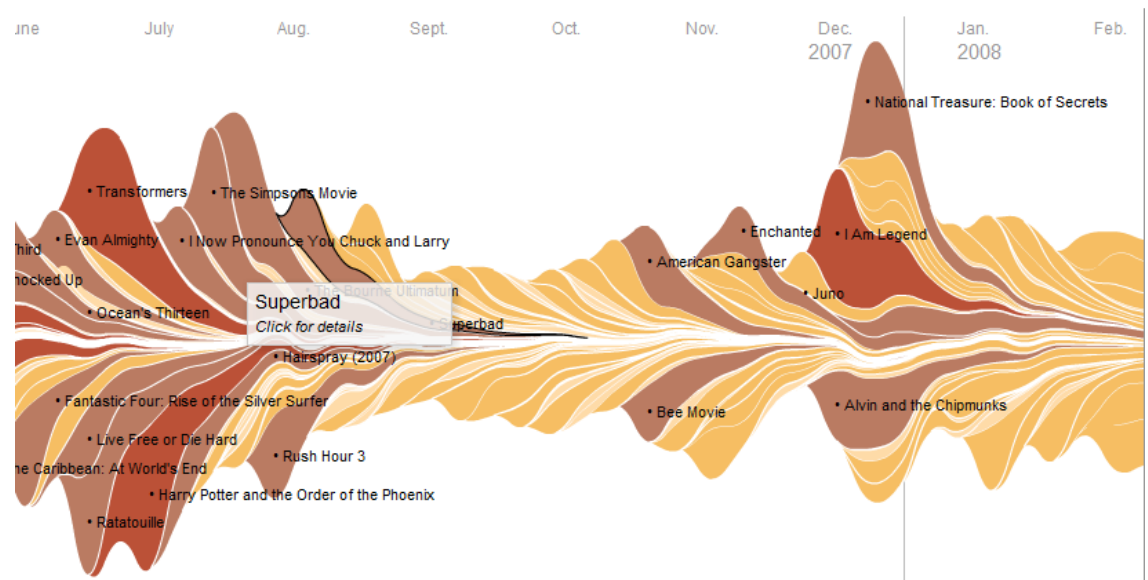
SIGN IN TO E-MAIL OR SAVE THIS | [FEEDBACK](#)

## The Ebb and Flow of Movies: Box Office Receipts 1986 — 2008

Summer blockbusters and holiday hits make up the bulk of box office revenue each year, while contenders for the Oscars tend to attract smaller audiences that build over time. Here's a look at how movies have fared at the box office, after adjusting for inflation.

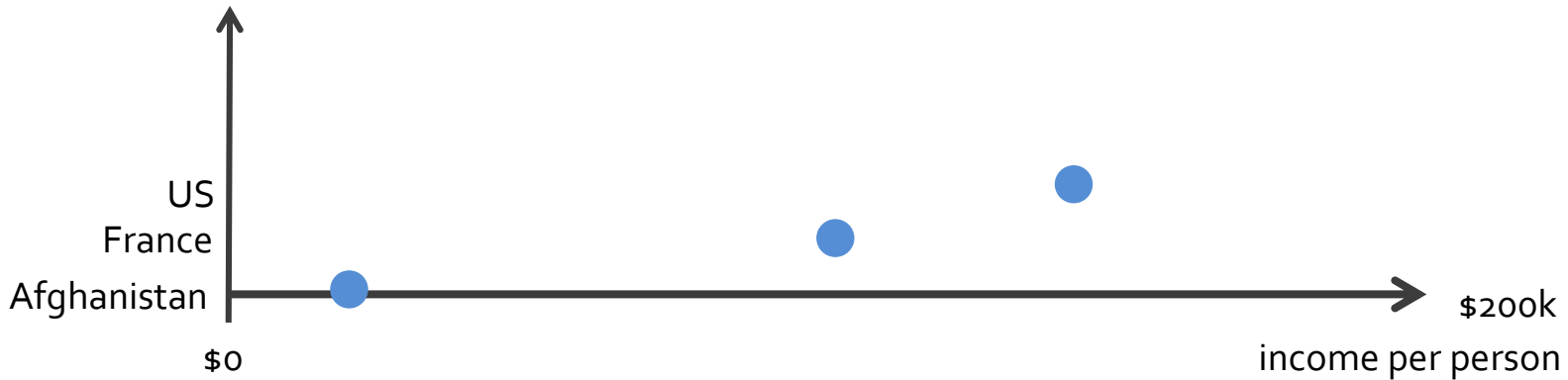
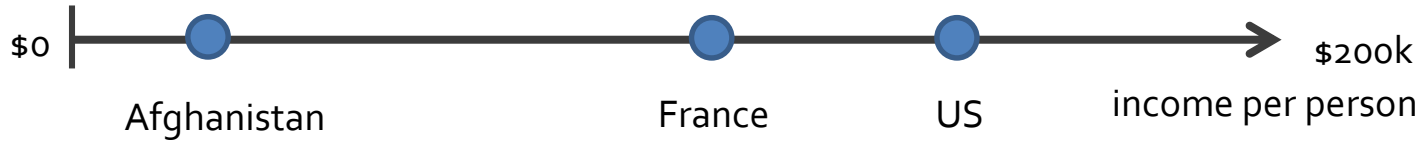


DATA	MD table; one quantitative value attribute (e.g. counts), one ordered key attribute (e.g. time), one categorical key attribute (e.g. film)
DERIVE	order of layers is derived from a quantitative attribute
ENCODE	use derived geometry to show layers across time, layer height encodes count
SCALE	key attributes (time, main axis): hundreds of time points key attributes (short axis): dozens to hundreds





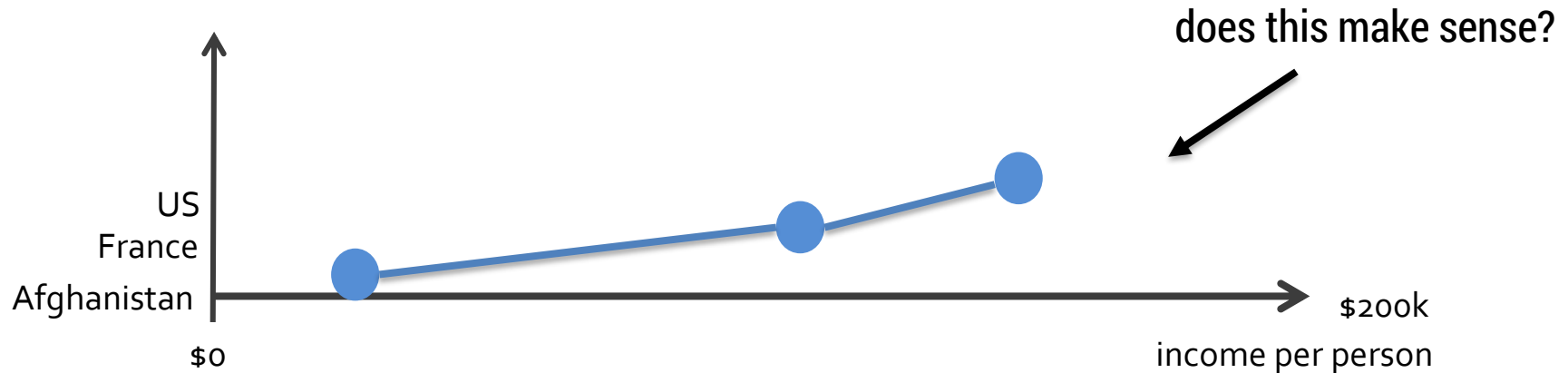
# DOT CHART/PLOT



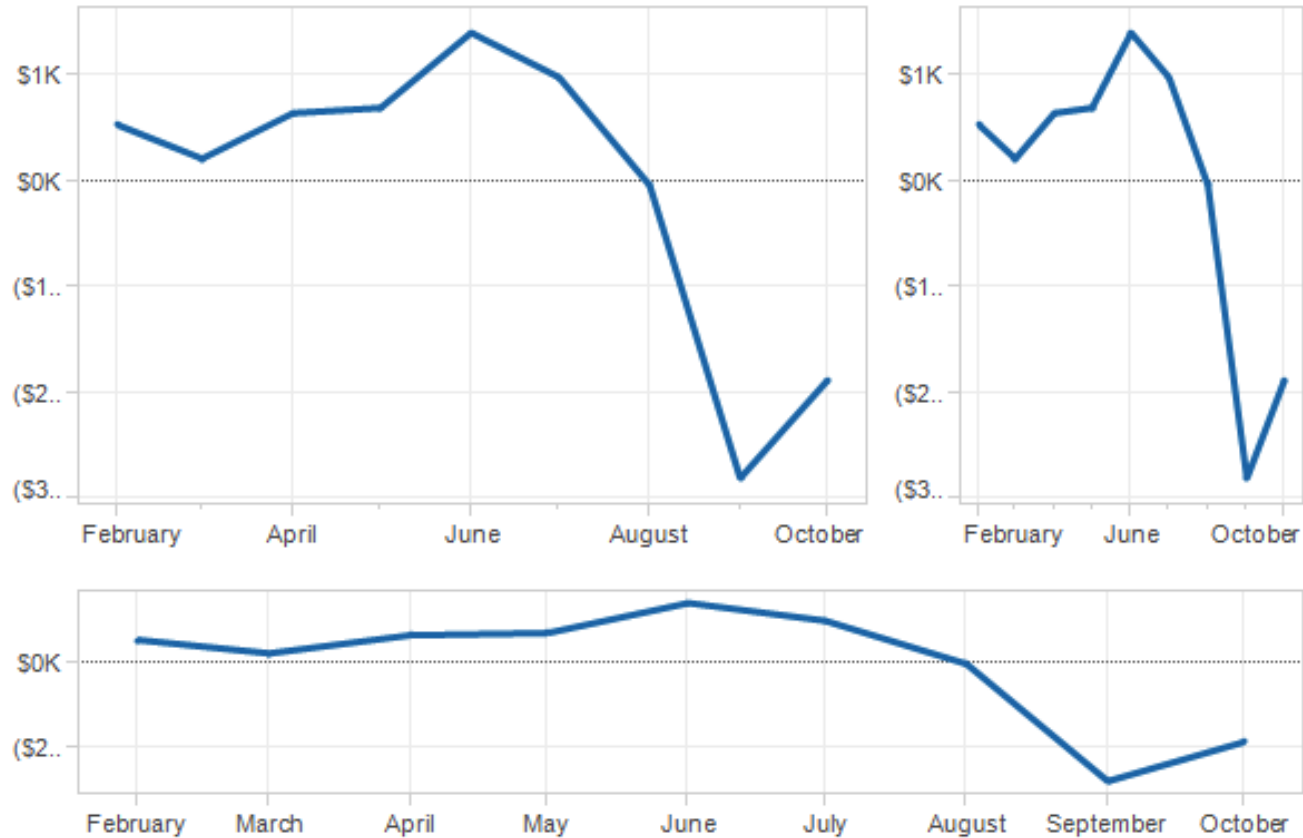


# LINE CHART

augment with line connection marks  
emphasize the ordering and show trends  
should not be used with categorical keys



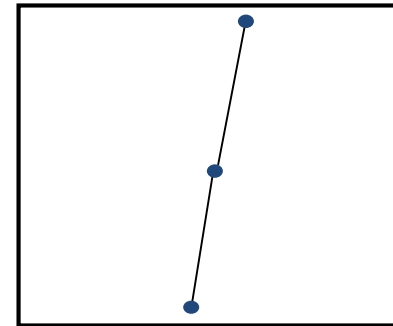
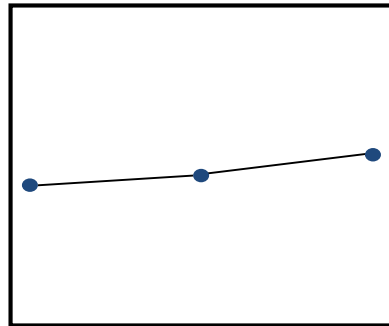
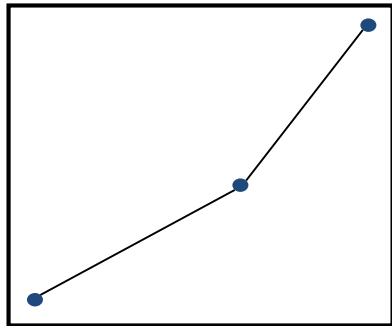
# ASPECT RATIO SELECTION



# BANKING TO 45°

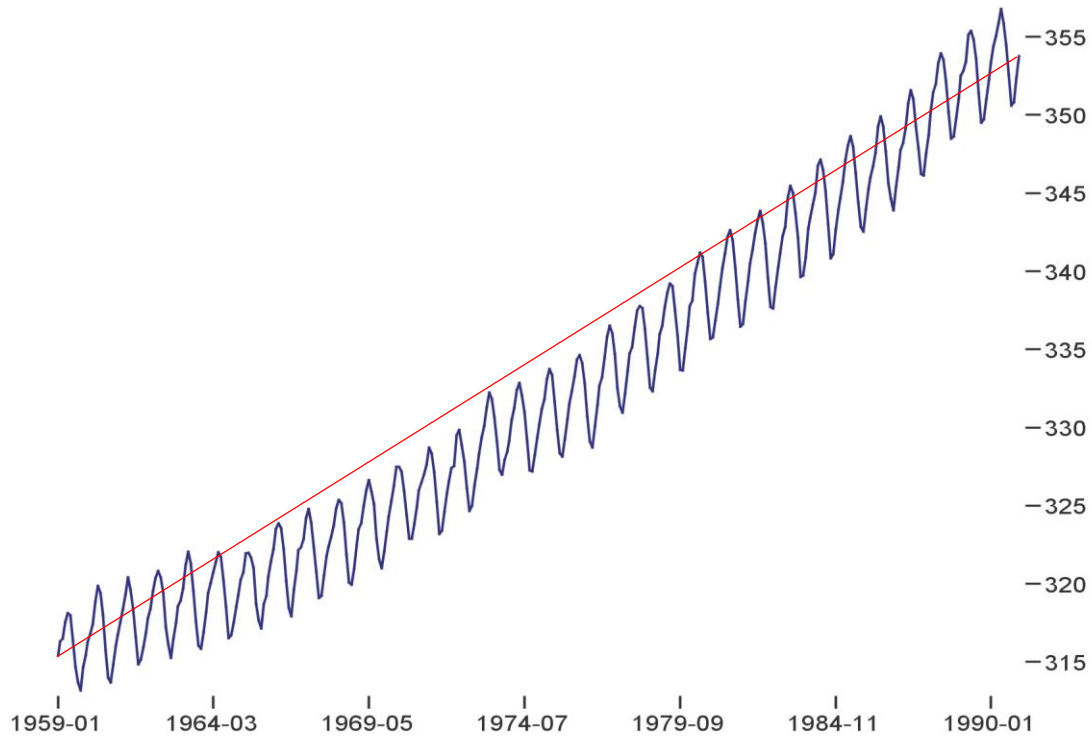
[Cleveland]

TO FACILITATE PERCEPTION OF TRENDS,  
MAXIMIZE THE DISCRIMINABILITY OF LINE  
SEGMENT ORIENTATIONS

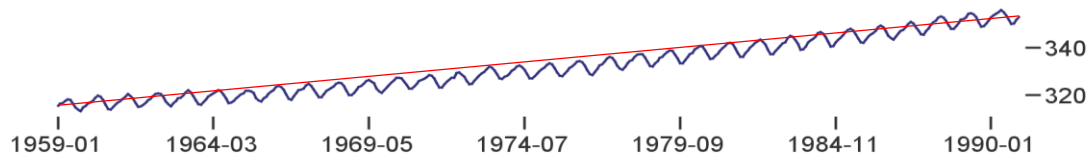


TWO SEGMENTS ARE MAXIMALLY DISCRIMINABLE WHEN THEIR AVG ABSOLUTE ANGLE IS  
45°

OPTIMIZE THE *ASPECT RATIO* TO BANK TO 45°

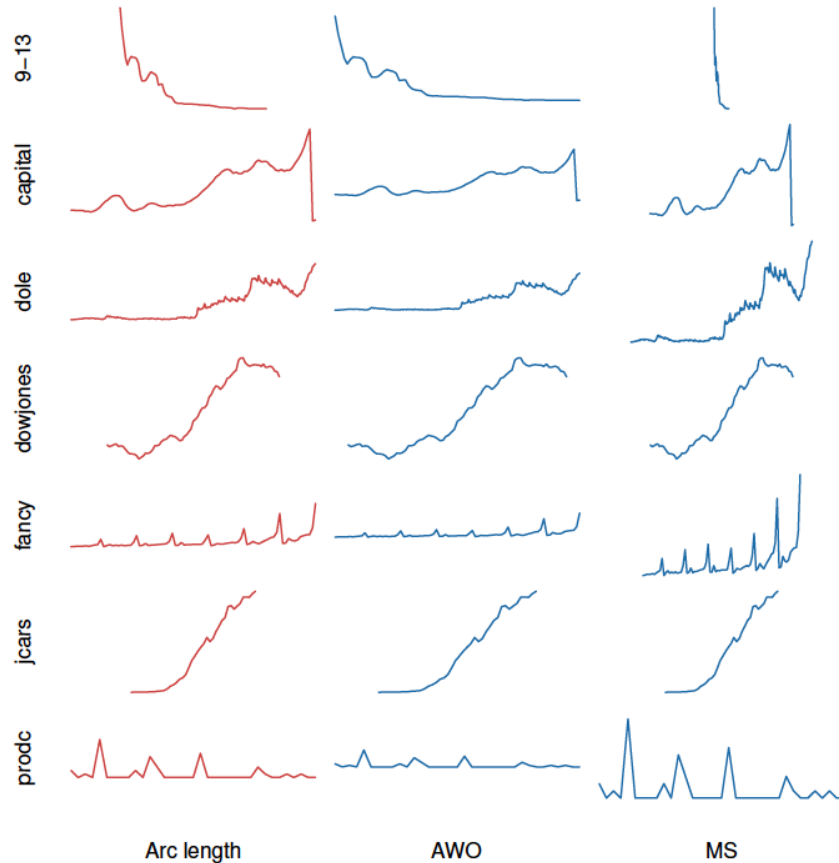


ASPECT RATIO = 1.17



ASPECT RATIO = 7.87

# ALTERNATIVE METHODS

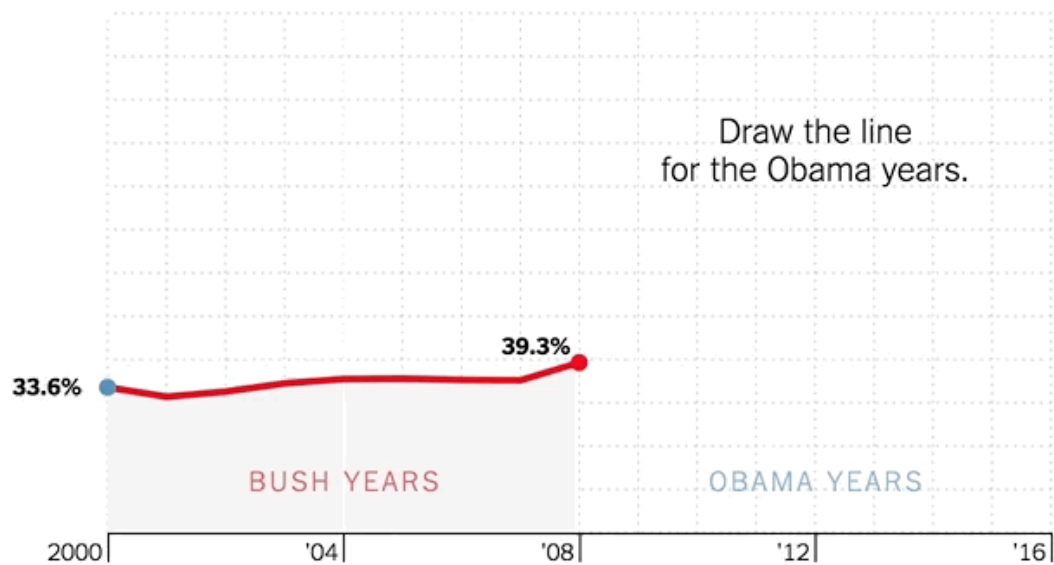


Practical advice:

CHOOSE AN **ASPECT RATIO** THAT  
EMPHASIZES THE IMPORTANT DETAILS  
FOR YOUR TASK

[TALBOT ET AL, 2011]

Under Mr. Obama, the **national debt** as a percentage of the gross domestic product ...

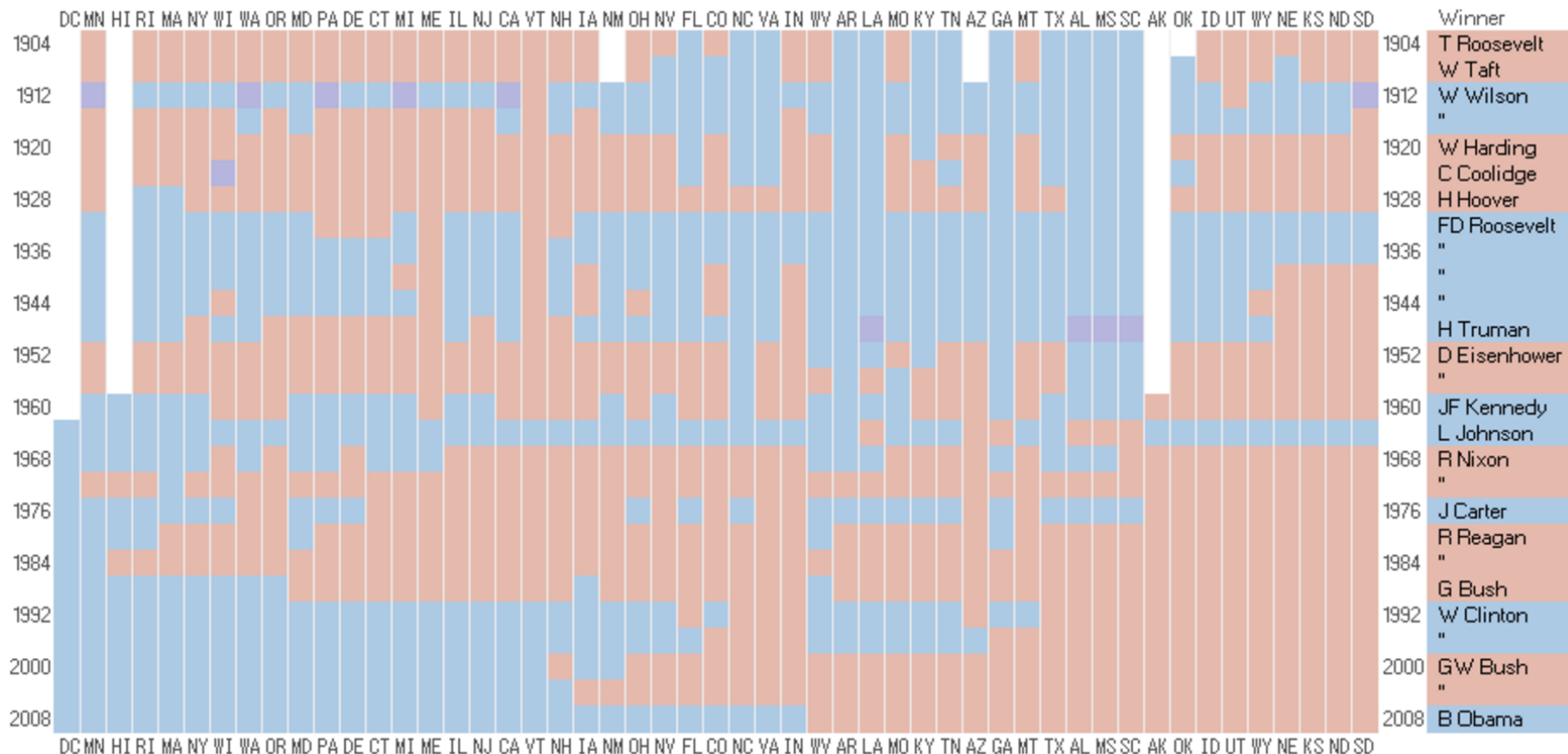


Show me how I did.

Numbers

# MATRIX ALIGNMENT

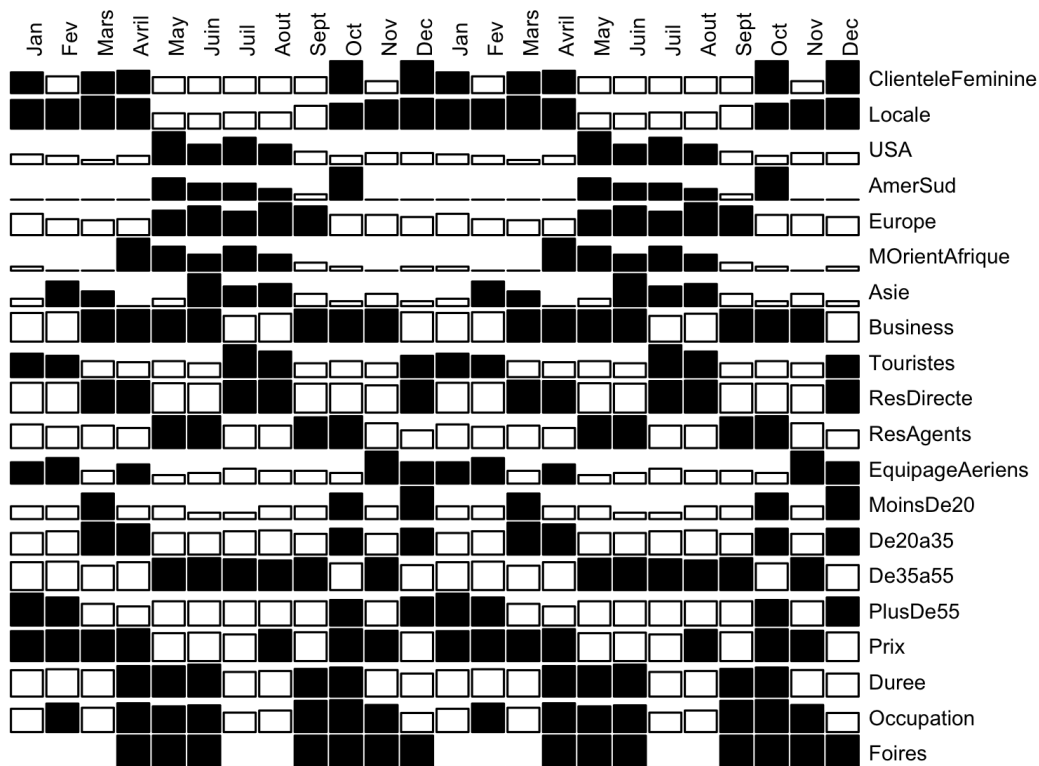
Two keys



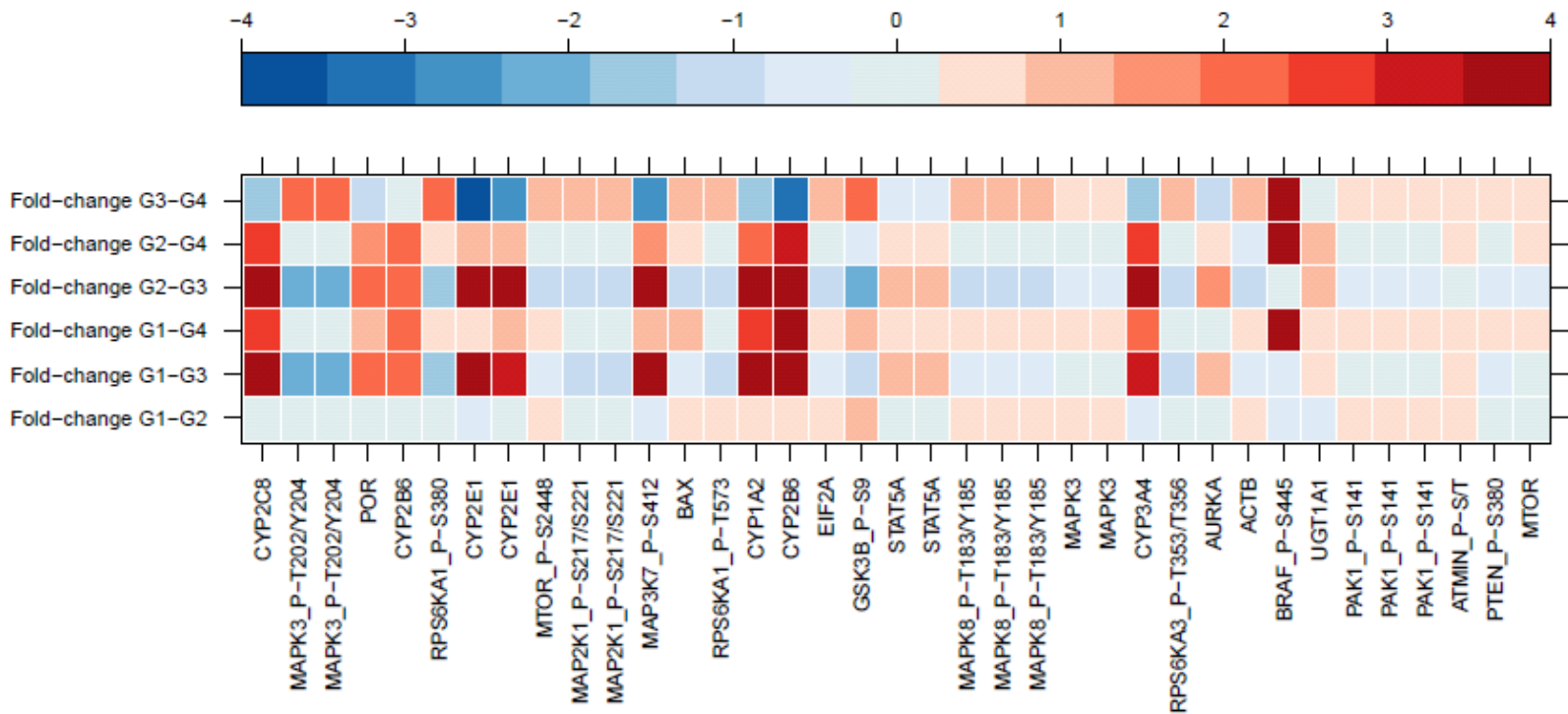


# HEATMAP

## Hotel 2

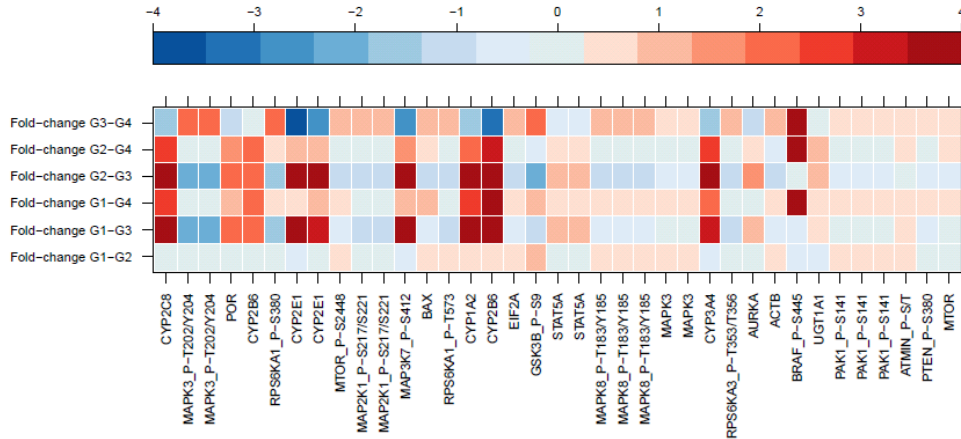


# HEATMAP

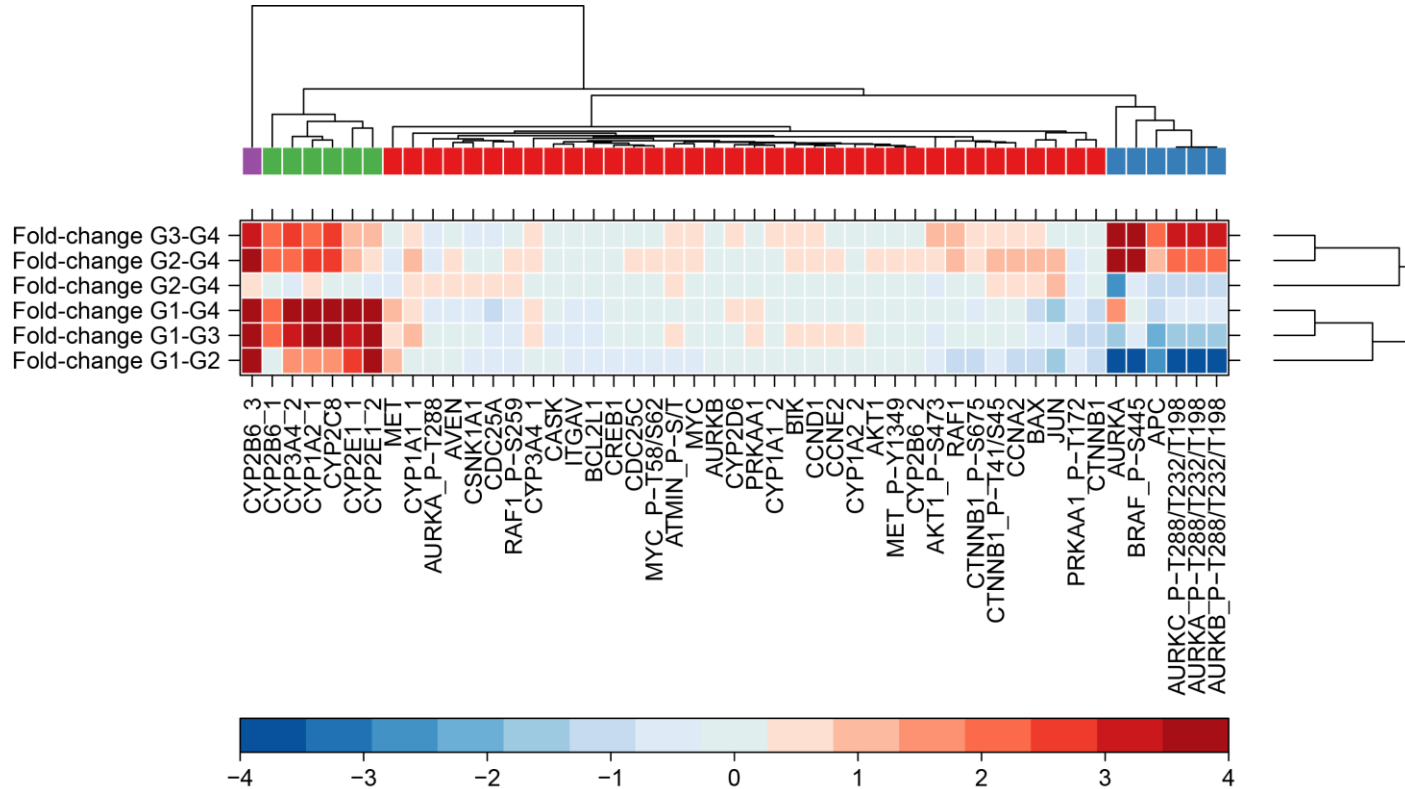


# HEATMAP

DATA	Table; two categorical key attributes, one quantitative value attribute
ENCODE	2D matrix alignment of area marks, e.g. with diverging color map
TASK	find clusters, outliers; summarize
SCALE	items: ~1 million (on 1000x1000px), categorical attribute levels: hundreds, quantitative attribute levels: 3-11



# CLUSTERED HEATMAP



# BACK TO OUR ORIGINAL EXAMPLE

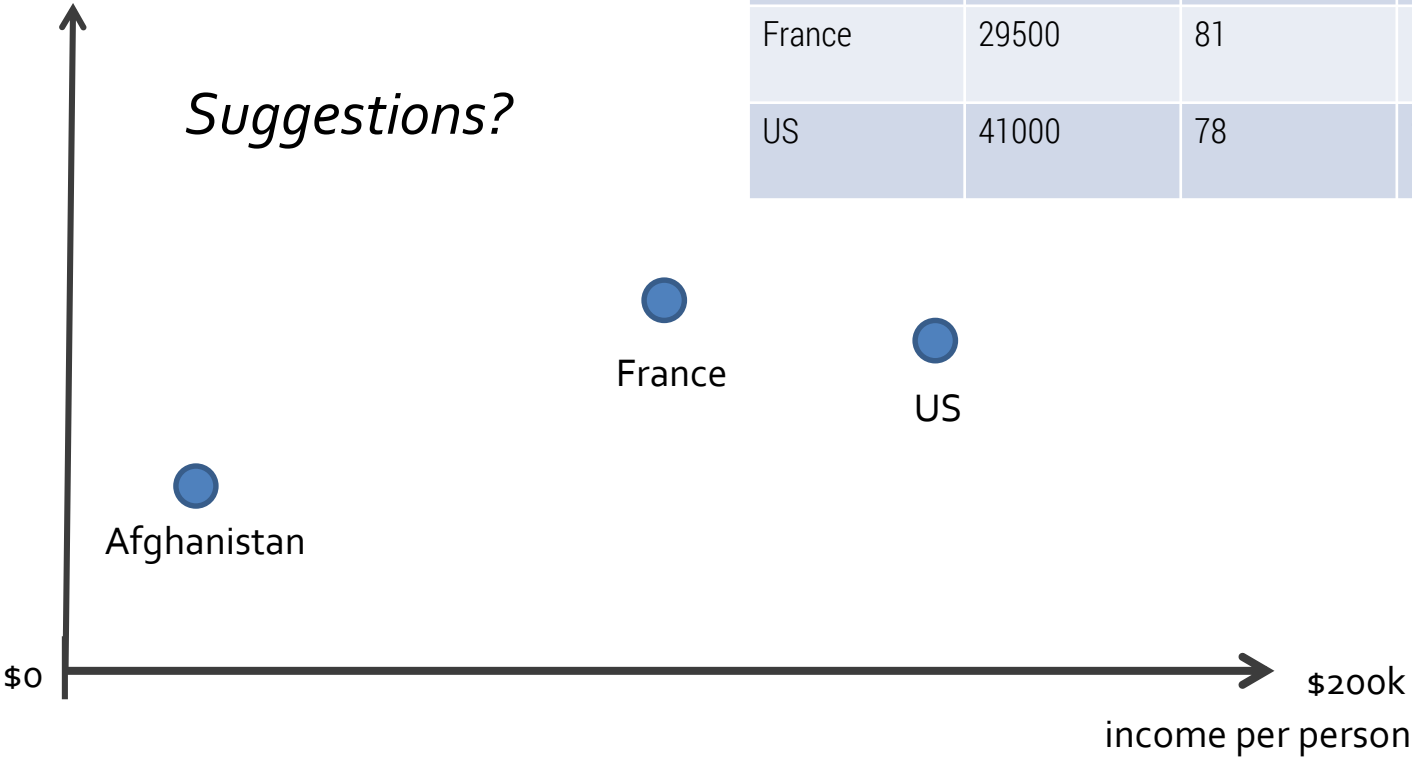
Country	Income per person	Life expectancy	Children per woman
Afghanistan	850	57	7.1
France	29500	81	1.9
US	41000	78	2.1

now with 4 attributes

Country	Income per person	Life expectancy	Children per woman
Afghanistan	850	57	7.1
France	29500	81	1.9
US	41000	78	2.1

200 years

*Suggestions?*



\$0

\$200k

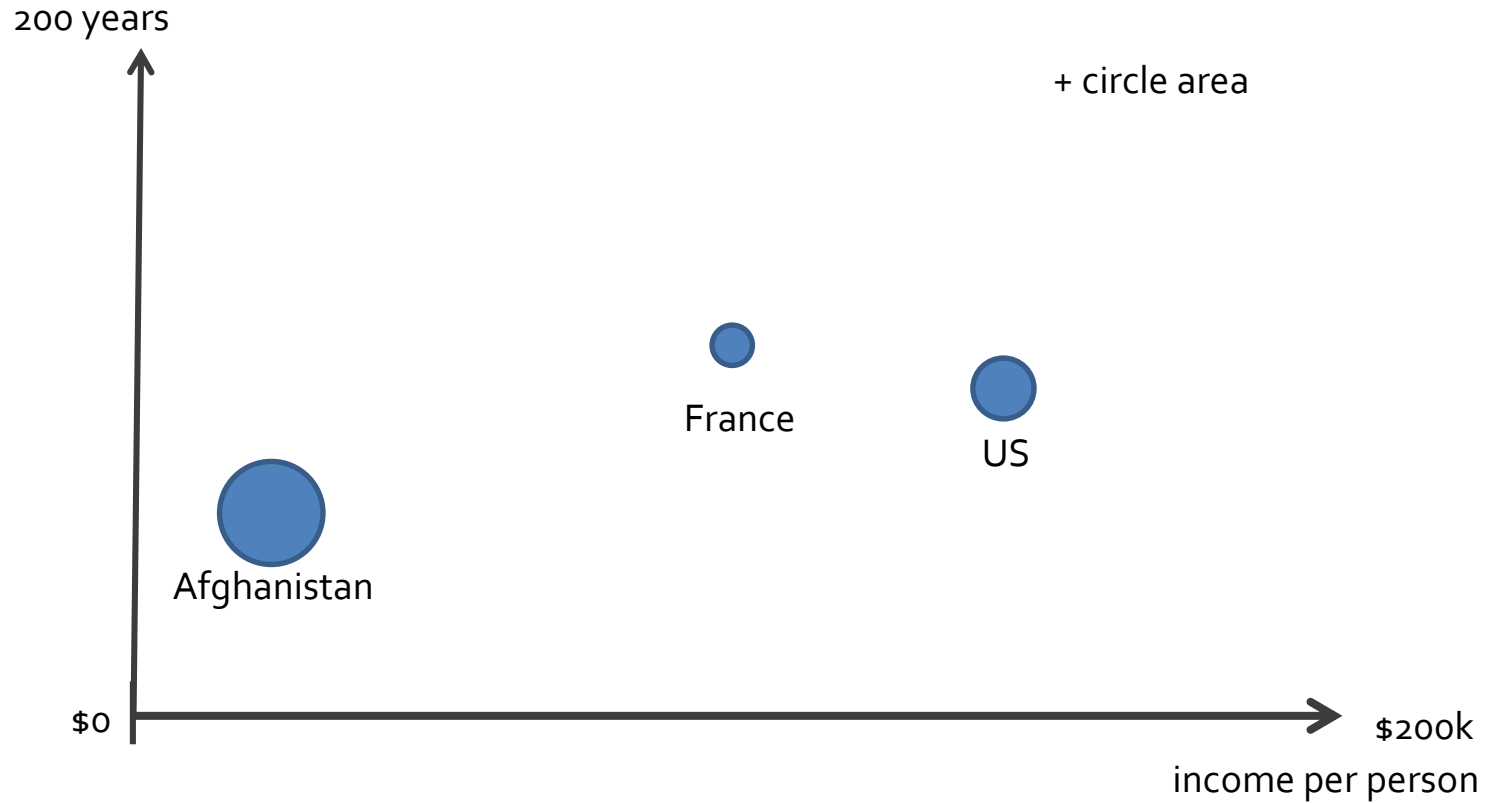
income per person

Afghanistan

France

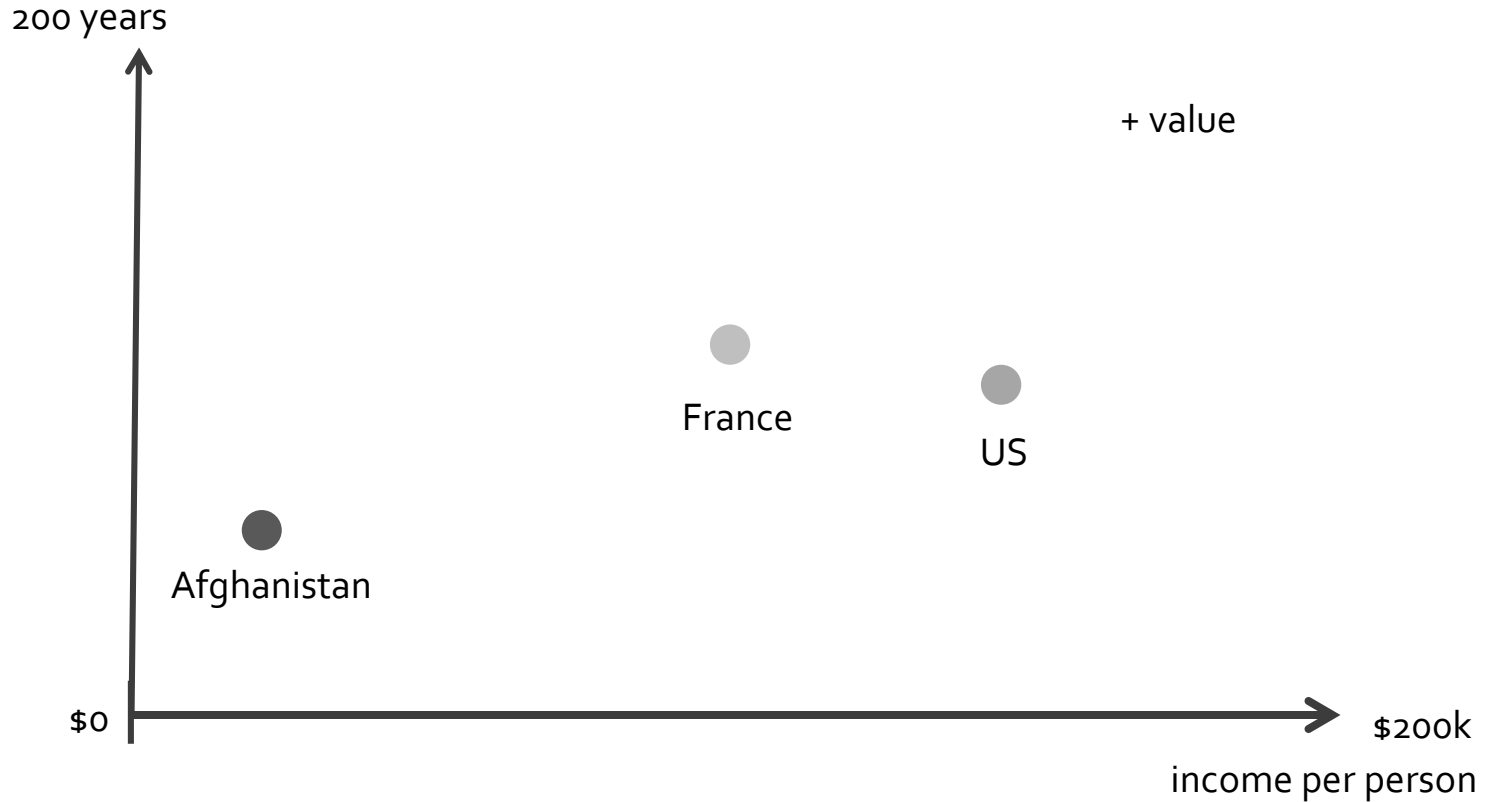
US

# ADD ANOTHER VISUAL ENCODING



Problem:  
Does not scale well to more attributes

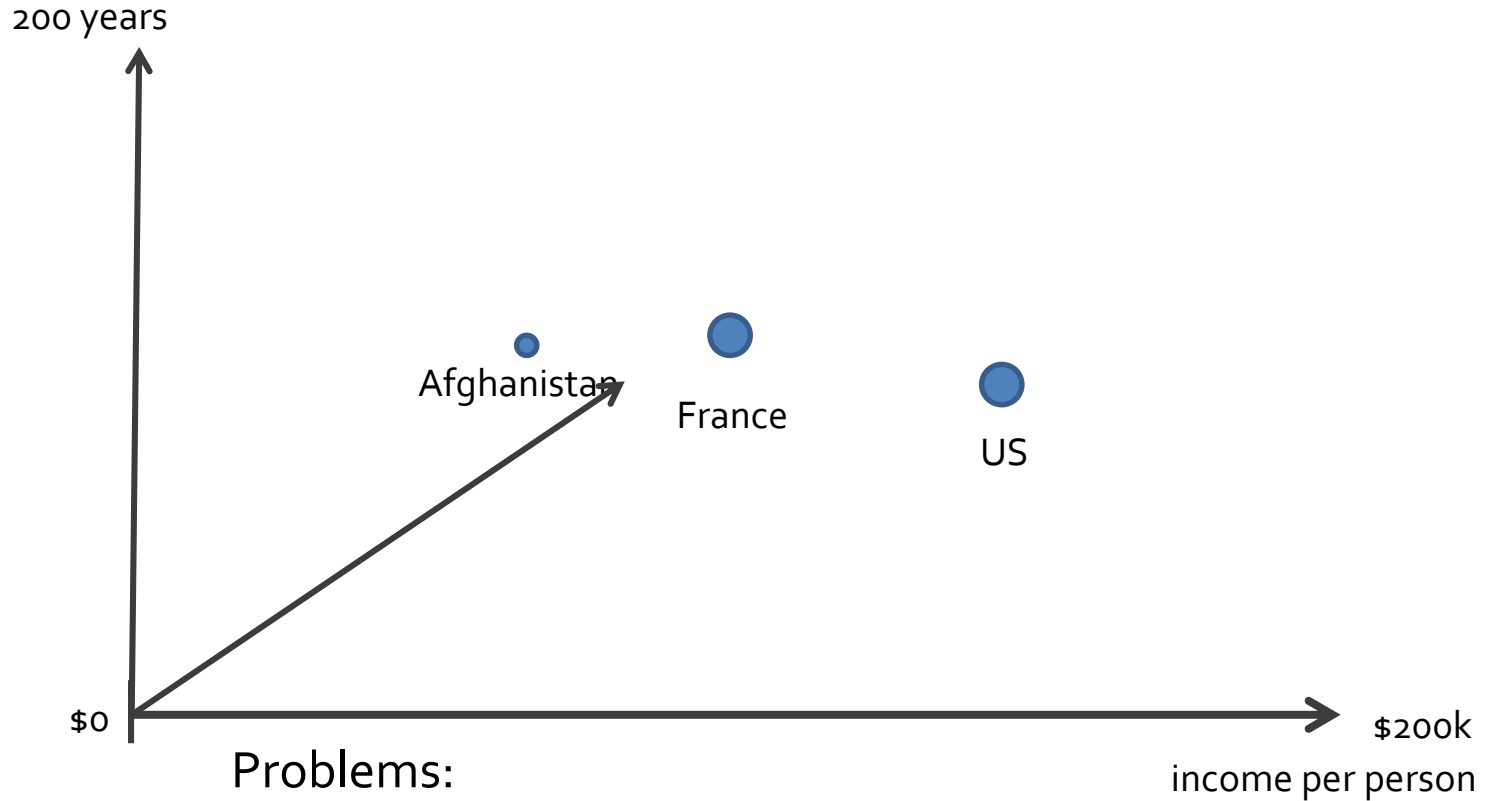
# ADD ANOTHER VISUAL ENCODING



Problem:  
Does not scale well to more attributes



# ADD AN AXIS

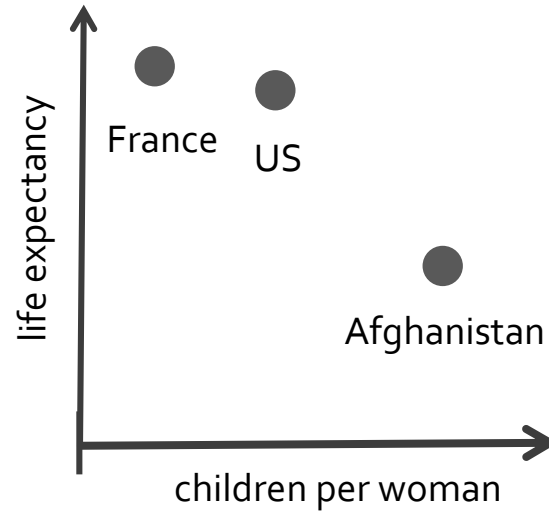
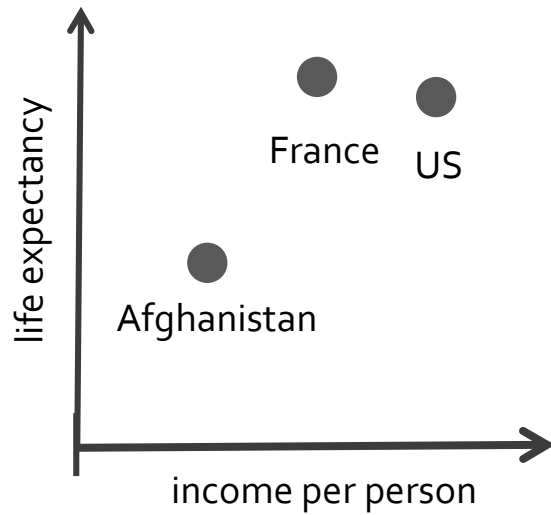


Problems:

Occlusion, perspective distortion, does not scale

→ Not usually recommended

# ADD AN AXIS



# SCATTERPLOT MATRIX

This idea scales relatively well

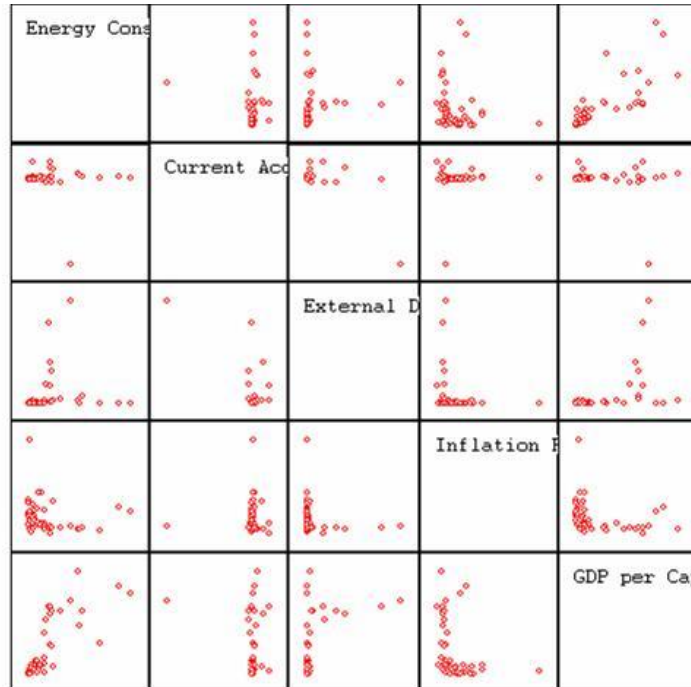


Image Source: Wikipedia

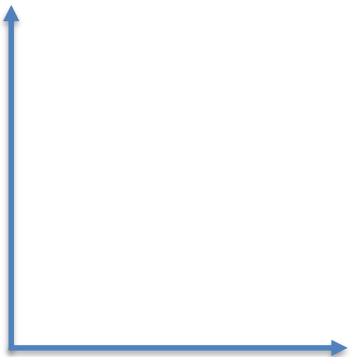
# GraphDice: A System for Exploring Multivariate Social Networks

A. Bezerianos  
F. Chevalier  
P. Dragicevic  
N. Elmqvist  
J-D. Fekete

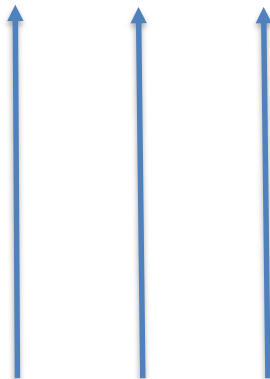
INRIA  
École Centrale Paris  
Purdue University

# SPATIAL AXIS ORIENTATION

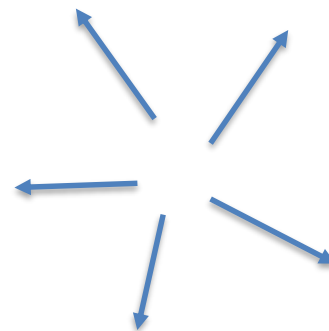
An additional design choice



rectilinear



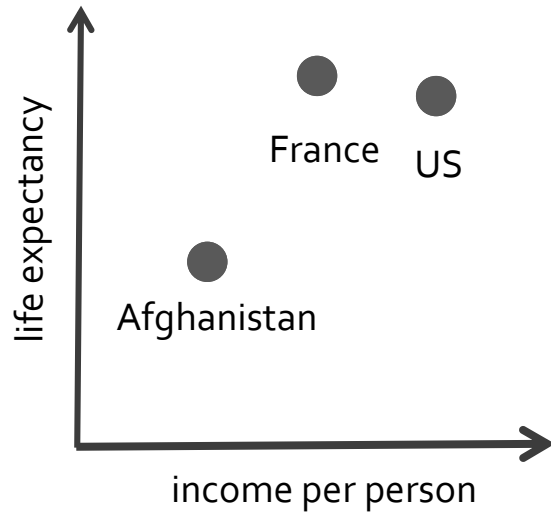
parallel



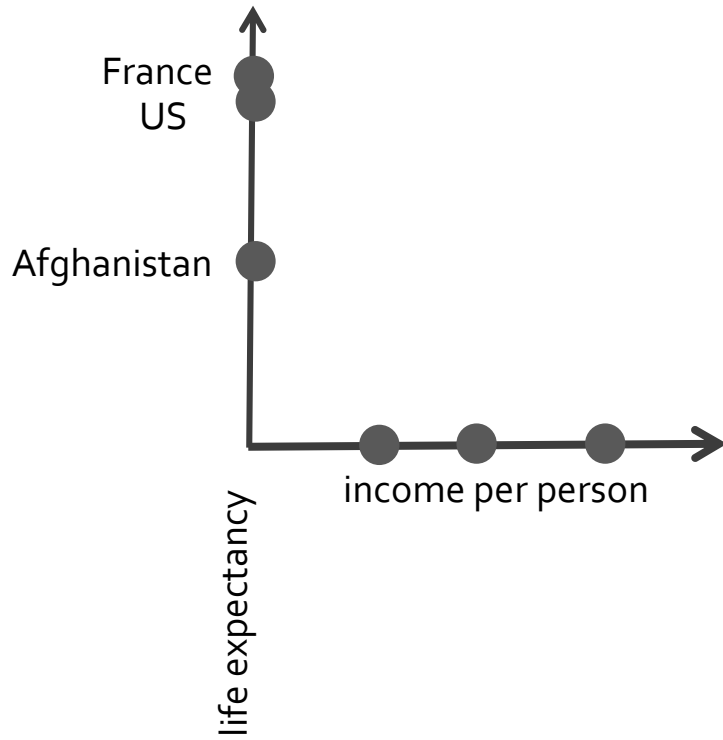
radial

# *parallel coordinates*

Back to our original example

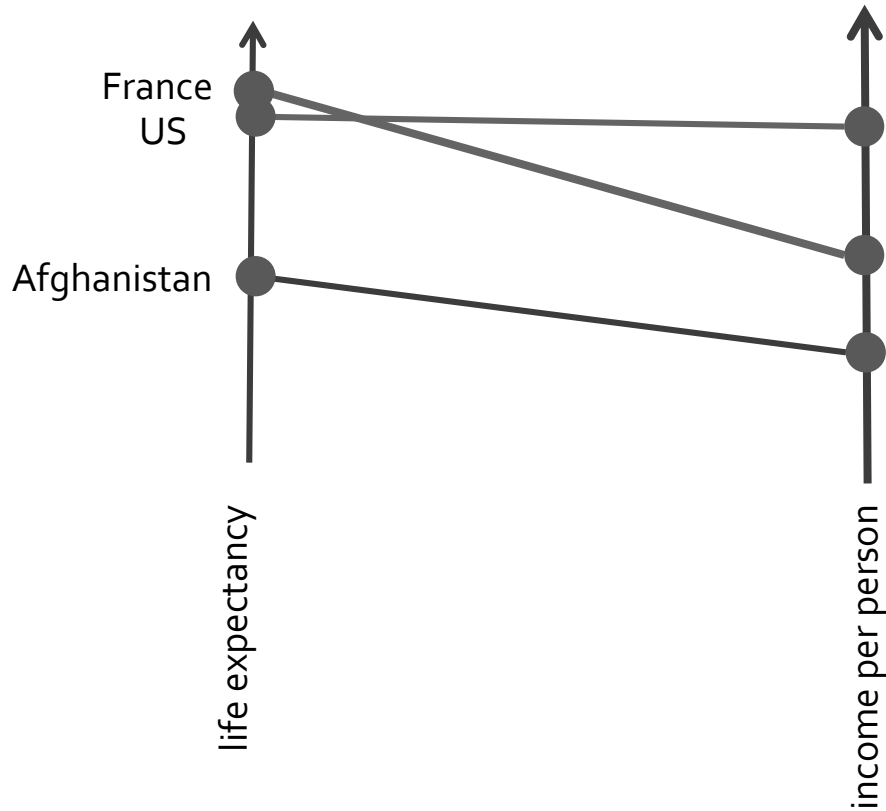


# *Parallel Coordinates*





# *parallel coordinates*



- show correlations between neighboring axes

# MULTIDIMENSIONAL DETECTIVE

Alfred Inselberg\*, Multidimensional Graphs Ltd<sup>†</sup>  
&  
Computer Science Department  
Tel Aviv University, Israel  
aiisreal@math.tau.ac.il

## Abstract

The display of multivariate datasets in parallel coordinates, transforms the search for *relations* among the variables into a 2-D pattern recognition problem. This is the basis for the application to *Visual Data Mining*. The Knowledge Discovery process together with some general guidelines are illustrated on a dataset from the production of a VLSI chip. The special strength of parallel coordinates is in modeling **relations**. As an example, a simplified Economic Model is constructed with data from various economic sectors of a real country. The visual model shows the interrelationship and dependencies between the sectors, circumstances where there is competition for the same resource, and feasible economic policies. Interactively, the model can be used to do trade-off analyses, discover sensitivities, do approximate optimization, monitor (as in a Process) and Decision Support.

## Introduction

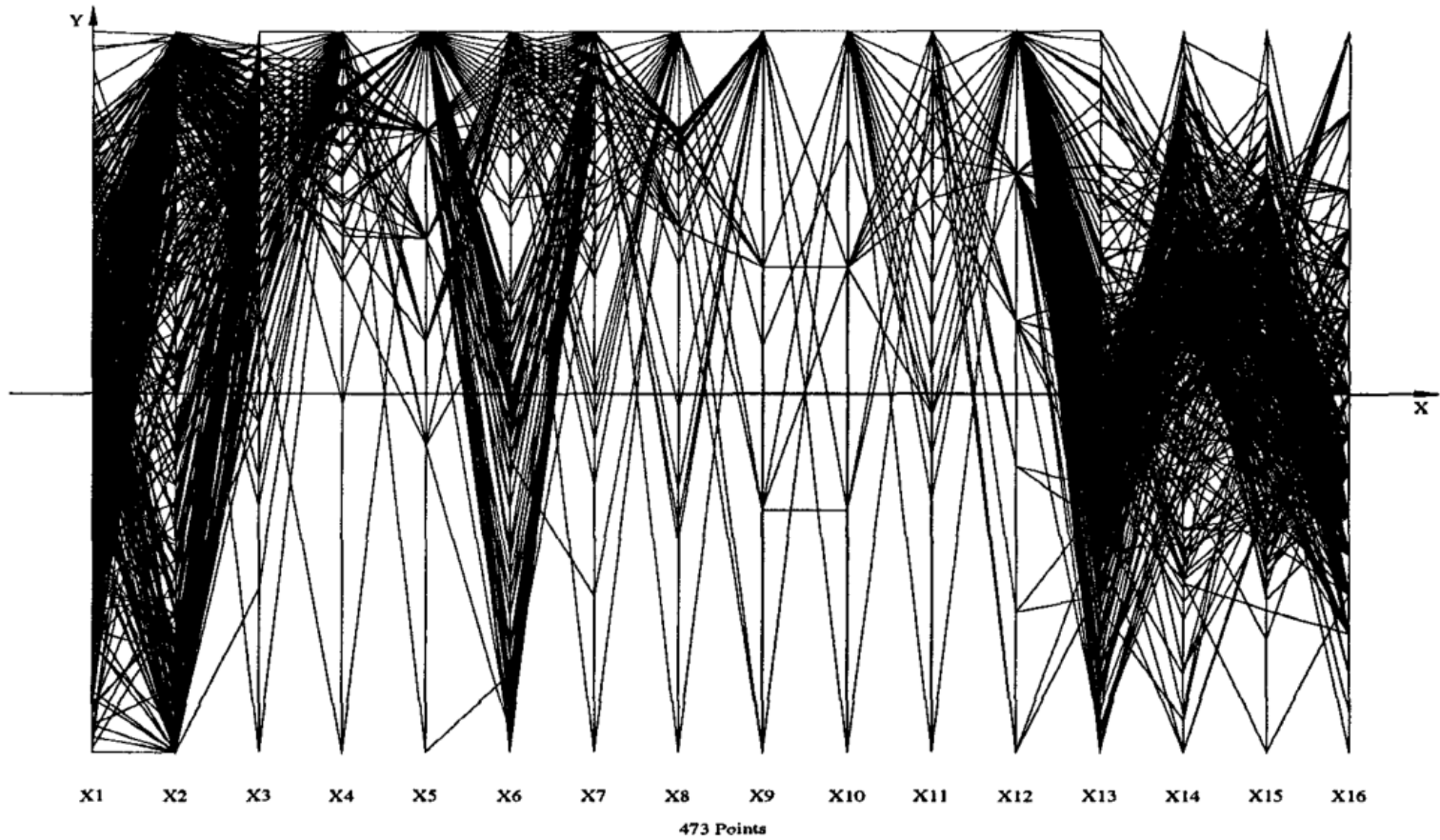
In Geometry parallelism, which does not require a notion of angle, rather than orthogonality is the more fundamental concept. This, together with the fact that orthogonality "uses-up" the plane very

fast, was the inspiration in 1959 for "Parallel" Coordinates. The systematic development began in 1977 [4]. The goals of the program were and still are (see [6] and [5] for short reviews) the visualization of multivariate/multidimensional problems without loss of information and having the properties:

1. Low representational complexity. Since the number of axes,  $N$  equals the number of dimensions (variables) the complexity is  $O(N)$ ,
2. Works for any  $N$ ,
3. Every variable is treated uniformly (unlike "Chernoff Faces" and various types of "glyphs"),
4. The displayed object can be recognized under projective transformations (i.e. rotation, translation, scaling, perspective),
5. The display easily/intuitively conveys information on the properties of the  $N$ -dimensional object it represents,
6. The methodology is based on rigorous mathematical and algorithmic results.

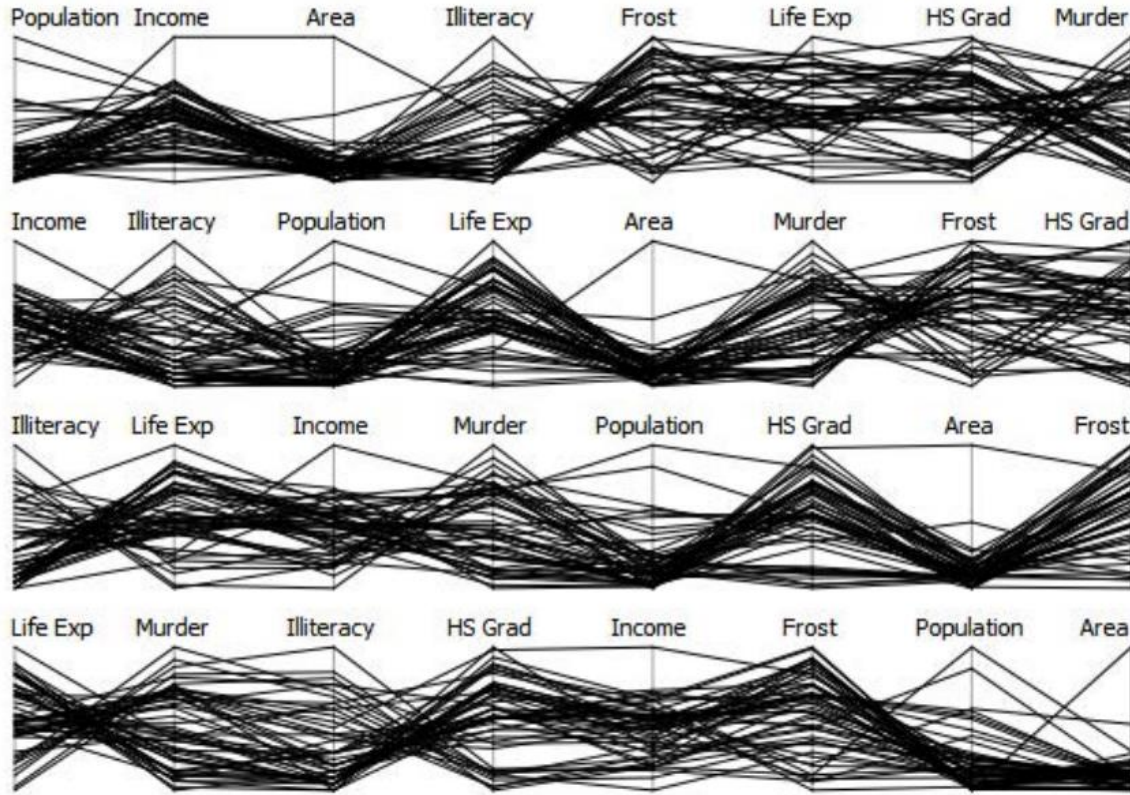
Parallel coordinates (abbr.||-coords) transform multivariate relations into 2-D patterns, a property that is well suited for Visual Data Mining.

\* Senior Fellow San Diego SuperComputing Center  
<sup>†</sup>36A Yehuda Halevy Street, Raanana 43556, Israel



Original Example from Inselberg 1997

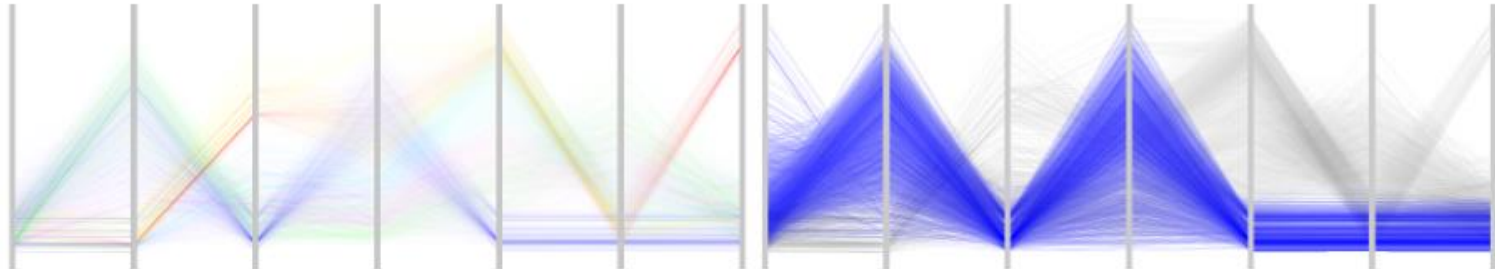
# THE ORDER OF AXES MATTERS



Eurographics 2013, STAR Report  
J. Heinrich, D. Weiskopf

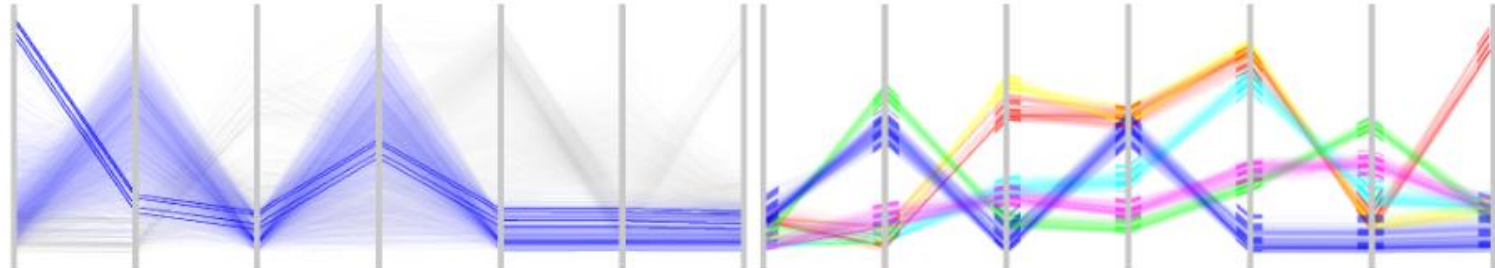
# REDUCE CLUTTER - HIGHLIGHT CLUSTERS

Lots of work on this. For example:



(a) A linear transfer function has been applied to the high-precision texture in order to prevent cluttering and to provide overview of the data.

(b) A logarithmic transfer function is applied to a selected cluster. The structure is preserved and emphasis is put on the low density regions.



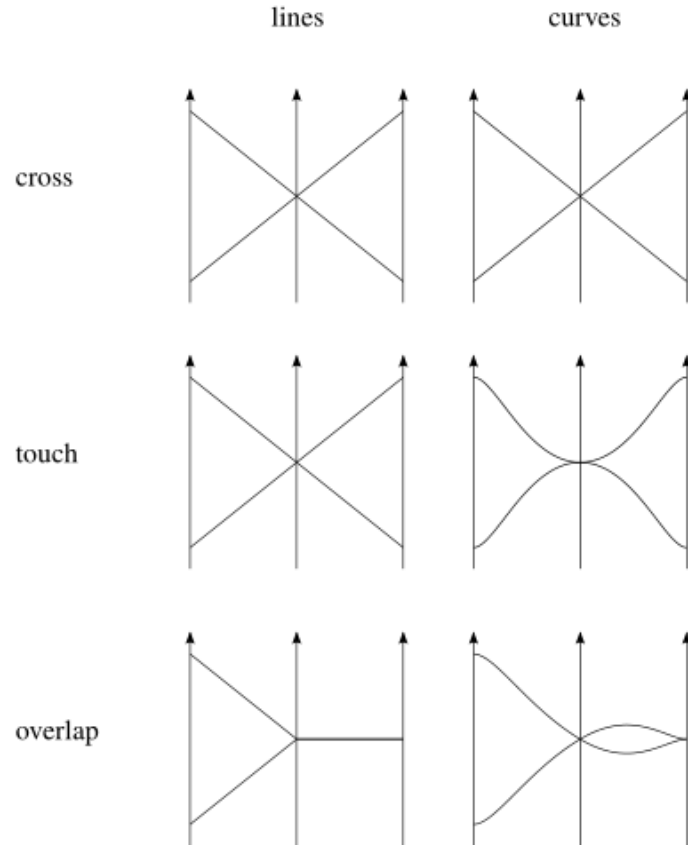
(c) Local cluster outliers are enhanced. A square root transfer function is used and the outliers are visible even through high-density regions.

(d) A complementary view of the clusters with uniform bands. 'Feature animation' presents statistics about the clusters and acts as a guidance.

Revealing Structure within Clustered Parallel Coordinates Displays, InfoVis 2005

# HOW TO DRAW THE LINES

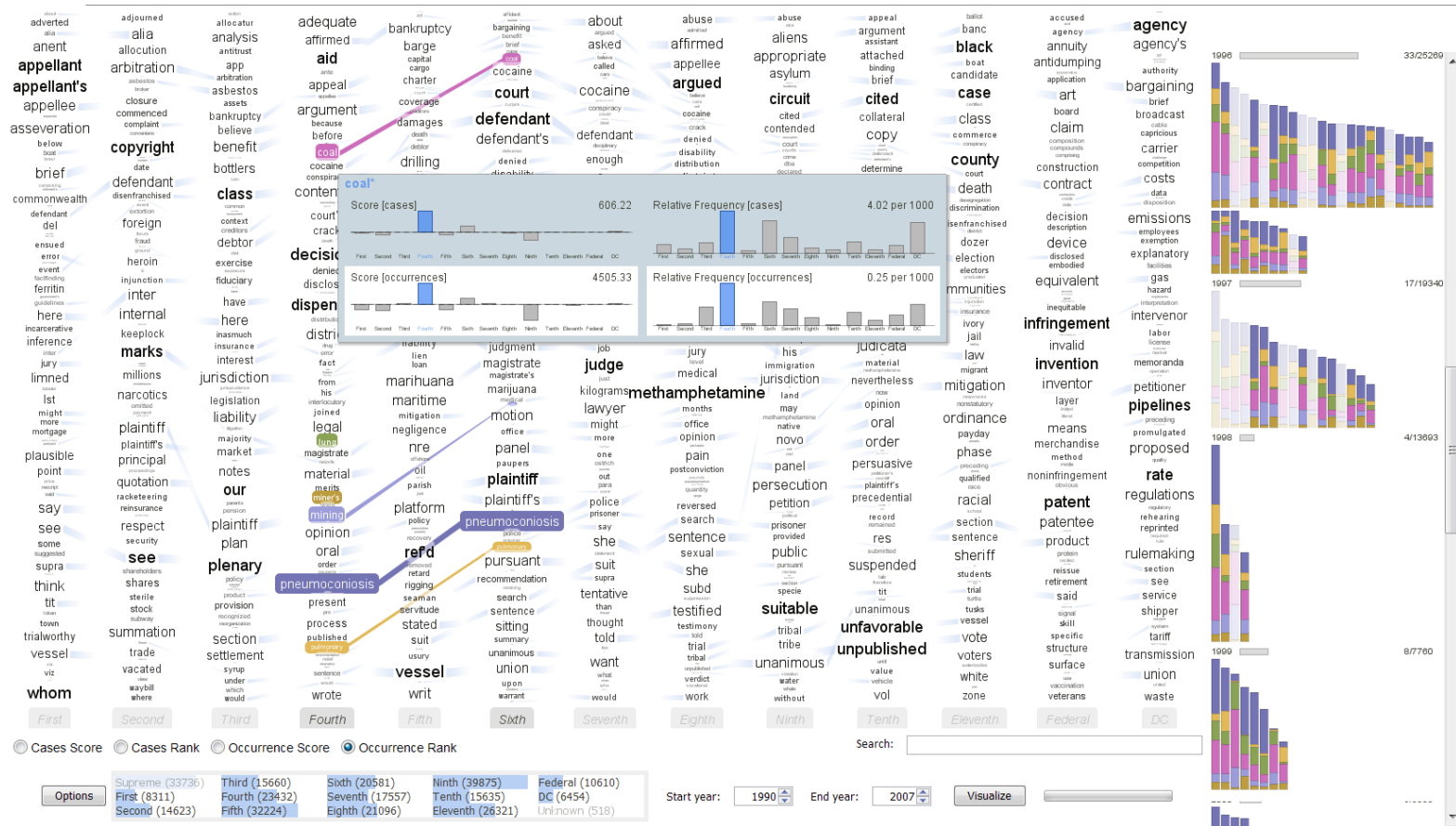
Goal: avoid ambiguity



Eurographics 2013, STAR Report  
J. Heinrich, D. Weiskopf

# COMBINE WITH OTHER VISUALIZATION TECHNIQUES

Parallel Tag Clouds to Explore Faceted Text Corpora (Collins et al., VAST 2009)



# THERE IS MUCH MORE ON THIS...

Start here if you want more information

EUROGRAPHICS 2013/ M. Sbert, L. Szirmay-Kalos

STAR – State of The Art Report

## State of the Art of Parallel Coordinates

J. Heinrich and D. Weiskopf

Visualization Research Center, University of Stuttgart

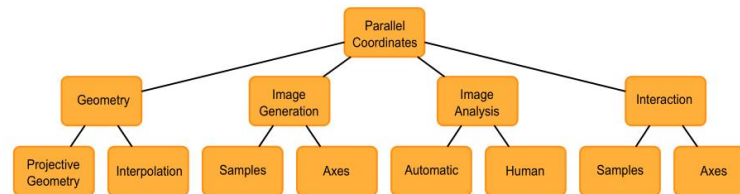


Figure 1: Taxonomy of topics for parallel coordinates in the scientific literature. The first-level nodes each represent a section in this paper, where the scope and definition of each topic will be explained.

### Abstract

*This work presents a survey of the current state of the art of visualization techniques for parallel coordinates. It covers geometric models for constructing parallel coordinates and reviews methods for creating and understanding visual representations of parallel coordinates. The classification of these methods is based on a taxonomy that was established from the literature and is aimed at guiding researchers to find existing techniques and identifying white spots that require further research. The techniques covered in this survey are further related to an established taxonomy of knowledge-discovery tasks to support users of parallel coordinates in choosing a technique for their problem at hand. Finally, we discuss the challenges in constructing and understanding parallel-coordinates plots and provide some examples from different application domains.*

Categories and Subject Descriptors (according to ACM CCS): I.3.3 [Computer Graphics]: Picture/Image Generation—Line and curve generation



# Scattering Points in Parallel Coordinates

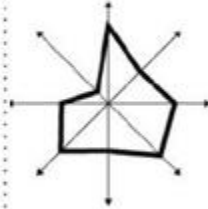
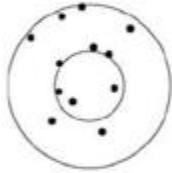
Xiaoru Yuan,<sup>1</sup> Peihong Guo,<sup>1</sup> He Xiao,<sup>1</sup> Hong Zhou,<sup>2</sup> Huamin Qu<sup>2</sup>

1. Key Laboratory of Machine Perception (MOE), School of EECS, Peking University

2. Department of Computer Science and Engineering at Hong Kong University of Science and Technology,  
Clear Water Bay, Kowloon, Hong Kong

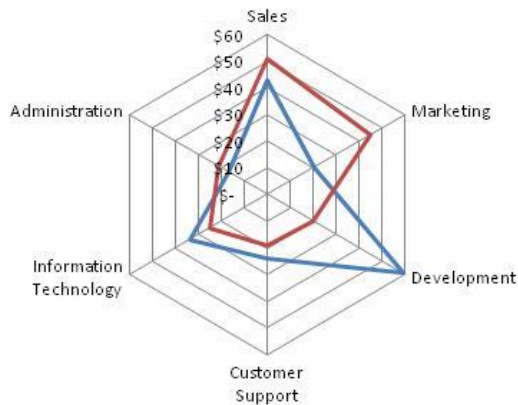
# RADIAL AXES

Polar

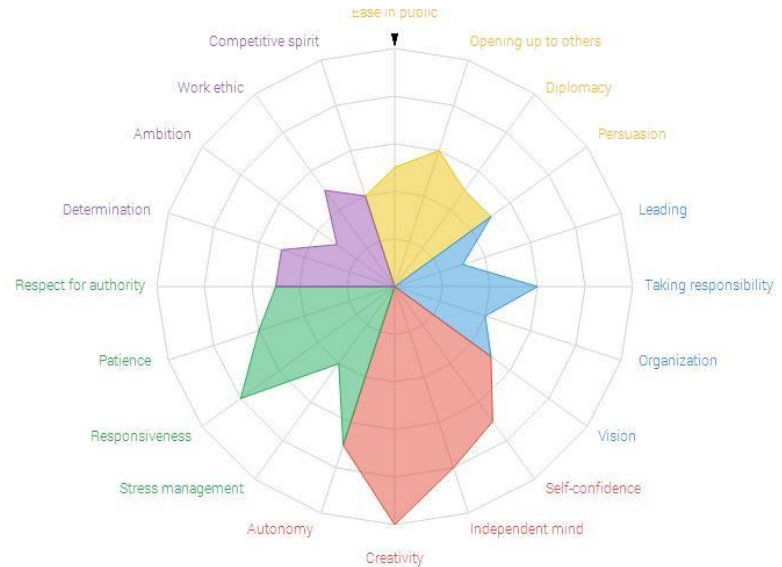


# EXAMPLE: STAR PLOT

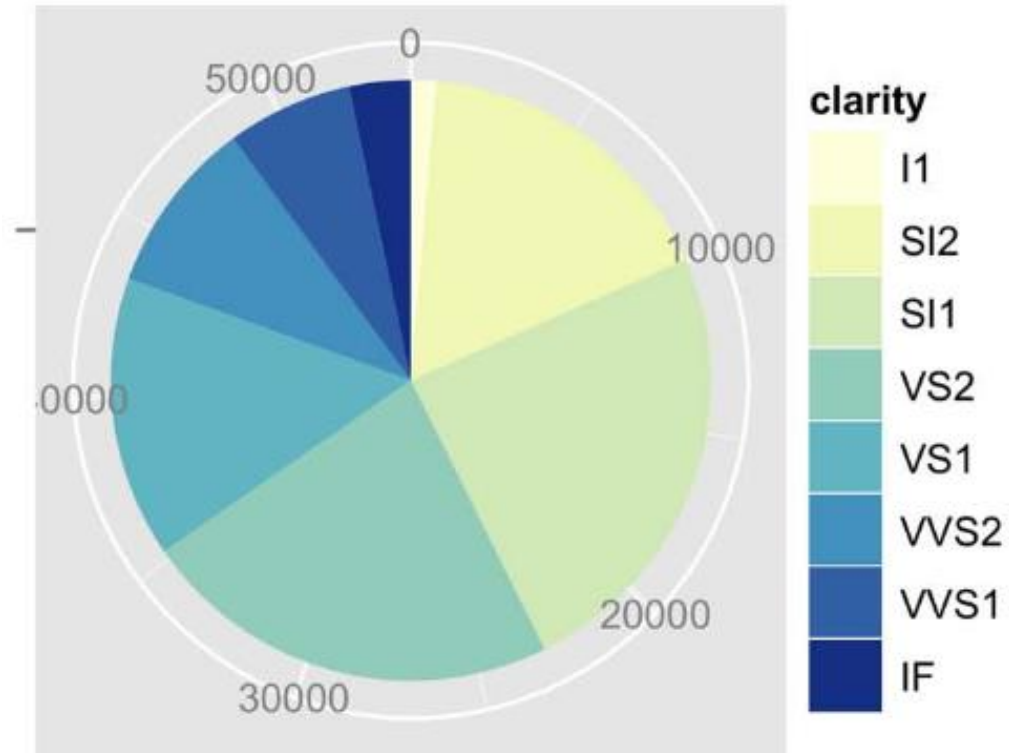
- = radial line chart



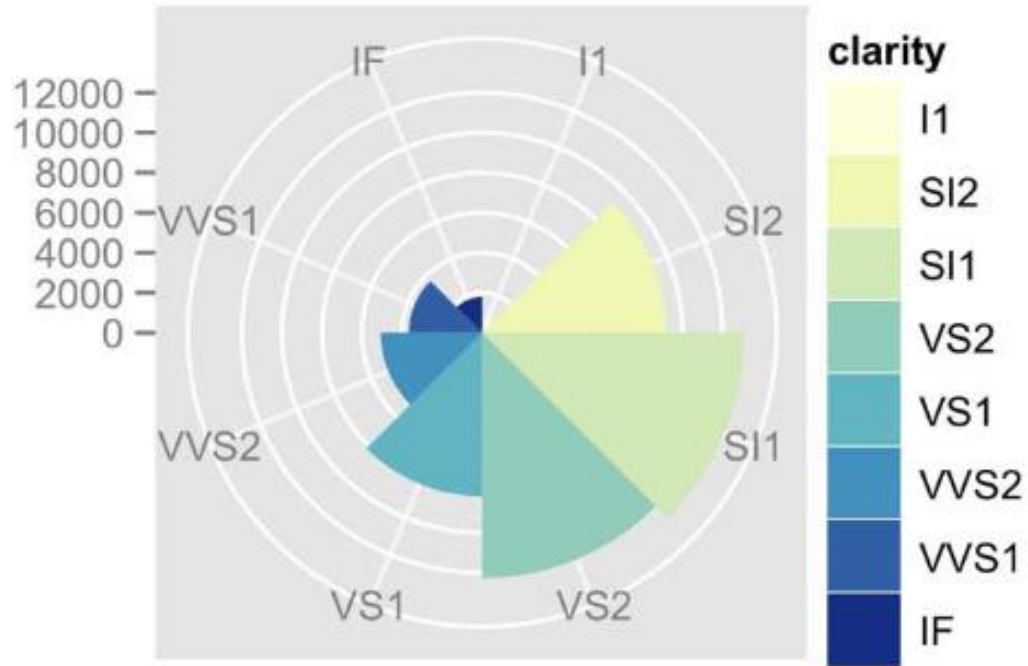
— Allocated Budget  
— Actual Spending



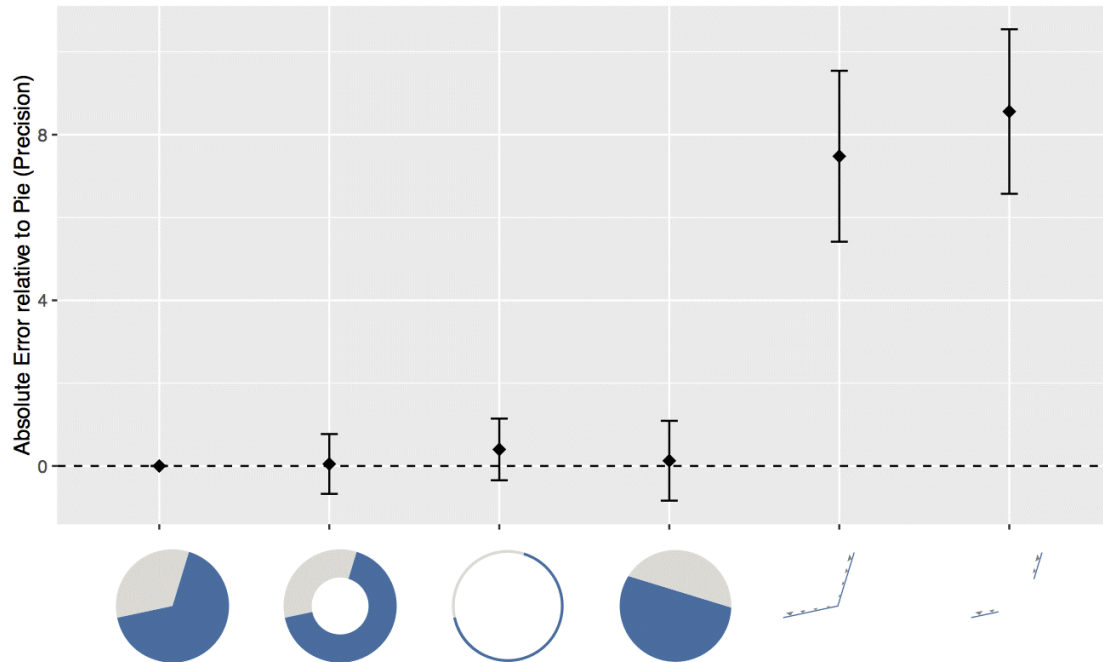
# PIE CHARTS



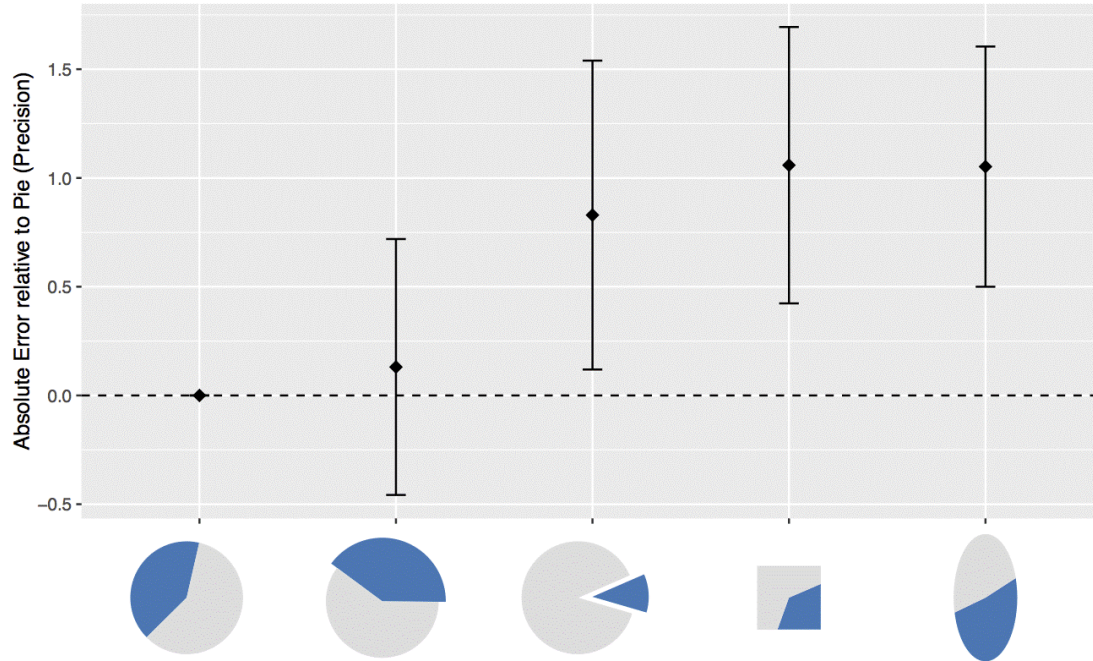
# POLAR AREA CHARTS



# HOW DO PEOPLE READ PIE CHARTS?



# HOW DO PEOPLE READ PIE CHARTS?



**WHAT IS ONE DIMENSION IS TIME?**

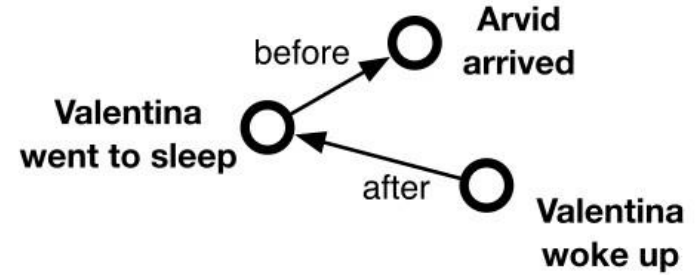


# TIME...

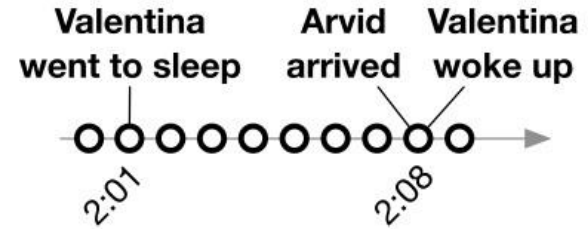
- ...IS JUST ANOTHER DATA DIMENSION
- WHY BOTHER?
- WHAT DATA TYPE IS IT?
  - NOMINAL?
  - ORDINAL?
  - QUANTITATIVE?

# DATA TYPE

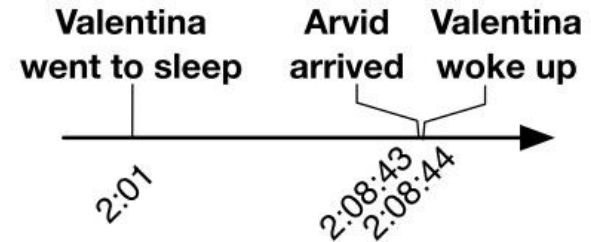
**ORDINAL**



**QUANTITATIVE**  
**DISCRETE**



**CONTINUOUS**  
(WITHIN THE LIMITS OF A COMPUTER)



# TIME IS PARTICULAR

- **PERIODICITY**
  - NATURAL: DAYS, SEASONS
  - SOCIAL: WORKING HOURS, HOLIDAYS
  - BIOLOGICAL: SLEEP, ETC.
- **MANY SUBDIVISIONS (UNITS)**
  - YEARS, MONTHS, DAYS, WEEKS, H, M, S
- **SPECIFIC MEANING**
  - NOT CAPTURED BY DATA TYPE
  - ASSOCIATIONS, CONVENTIONS
  - TIME VISUALIZATIONS OFTEN CONSIDERED AS A SEPARATE TYPE



# TIME IS PARTICULAR

- SHNEIDERMAN'S TAXONOMY OF DATA TYPES
  - 1D DATA
  - 2D DATA
  - 3D DATA
  - TEMPORAL DATA
  - MULTI-DIMENSIONAL DATA
  - TREE DATA
  - NETWORK DATA

# VISUALIZING TIME

Of 4000 randomly sampled graphics from  
15 newspapers and magazines ('74-'80),  
75% were time series.



**EDWARD TUFTE**

# DEFINITION

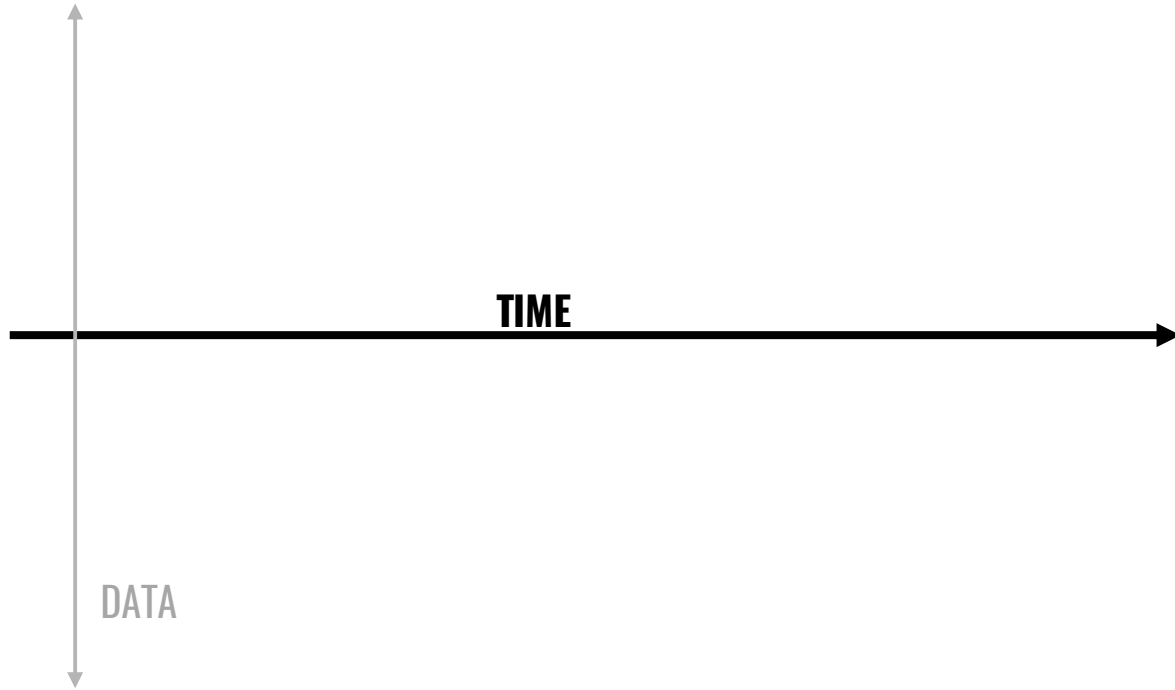
A TIME SERIES IS A SEQUENCE OF DATA POINTS, MEASURED (TYPICALLY) AT SUCCESSIVE POINTS IN TIME (OFTEN) SPACED AT UNIFORM TIME INTERVALS.

A SET OF OBSERVATIONS  $X_T$ , EACH ONE BEING RECORDED AT A SPECIFIC TIME  $T$

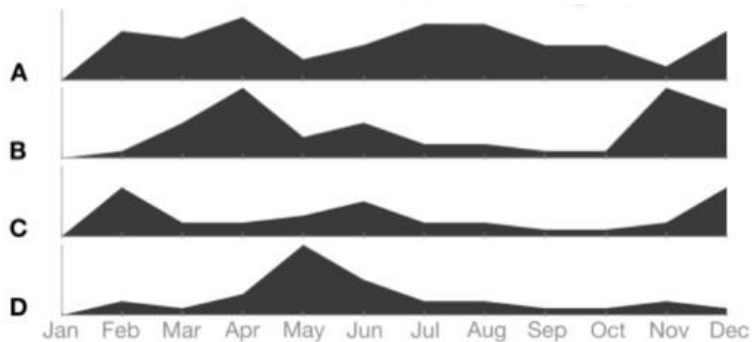
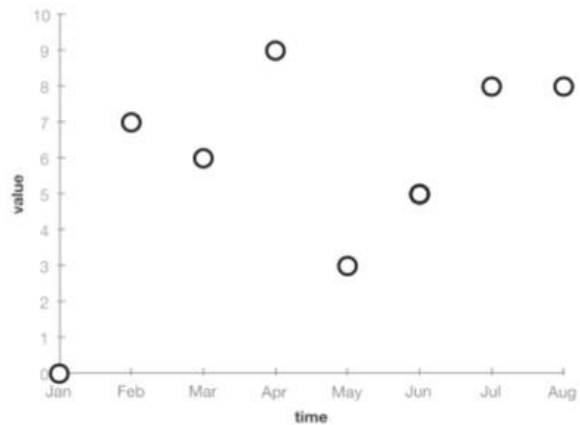
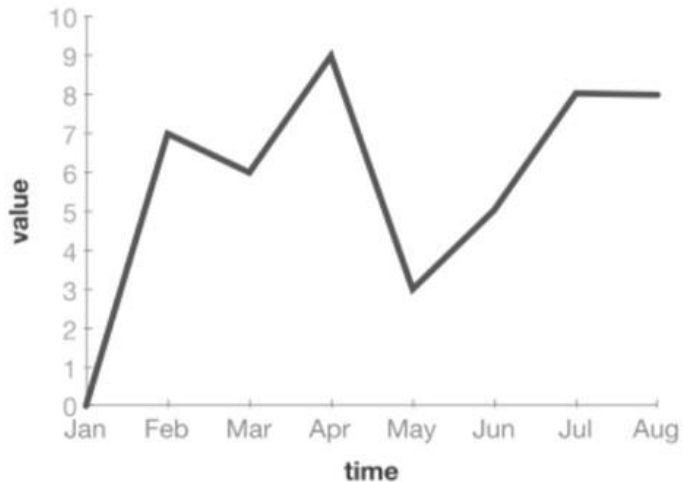
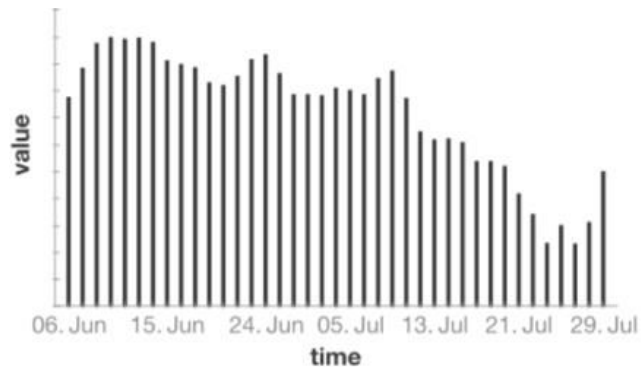
# MAPPING DATA TO AN AXIS



# MAPPING TIME TO AN AXIS



# SIMPLE CHARTS



# OTHER DATA TYPES



# OTHER DATA TYPES - ORDINAL

## RANK CHART

**MOST HIGHLY-REGARDED BRANDS BY UK'S PROMINENT LEADERS**

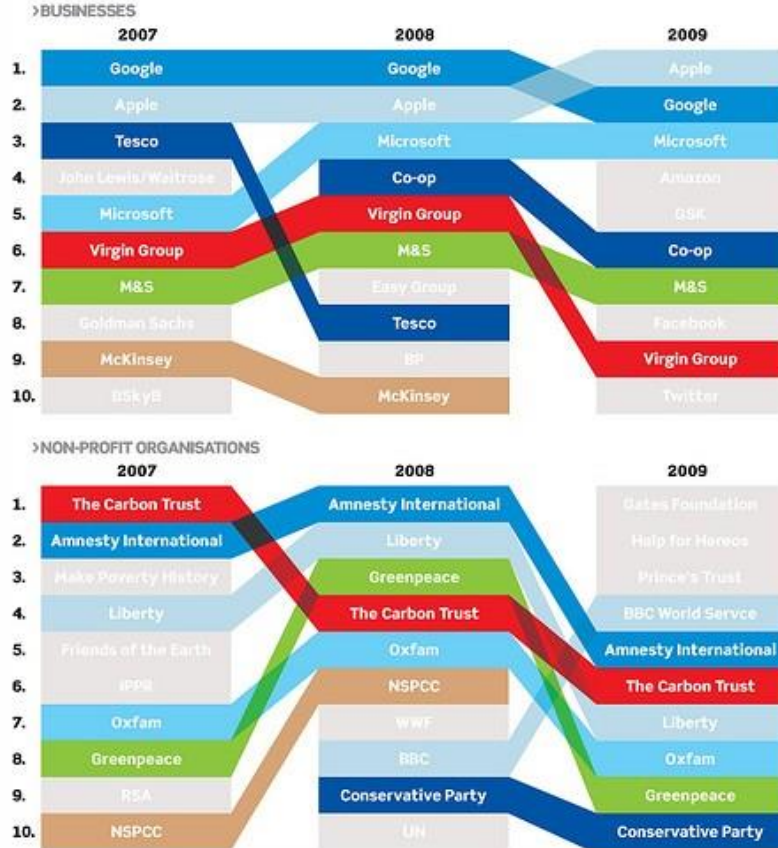
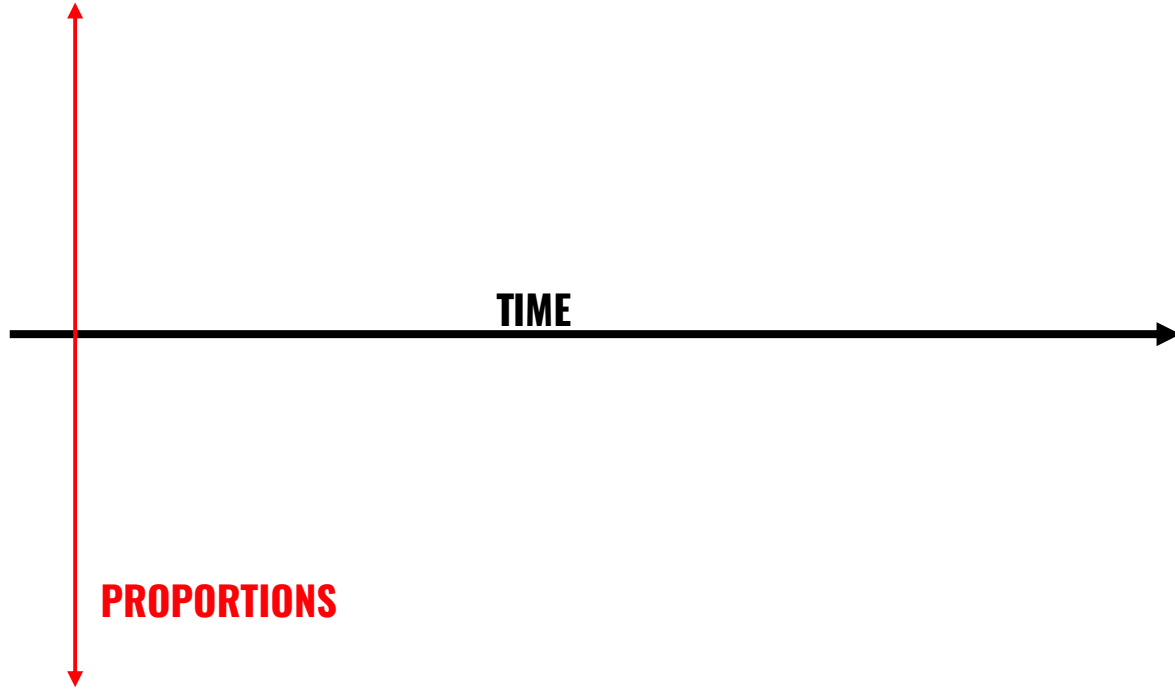


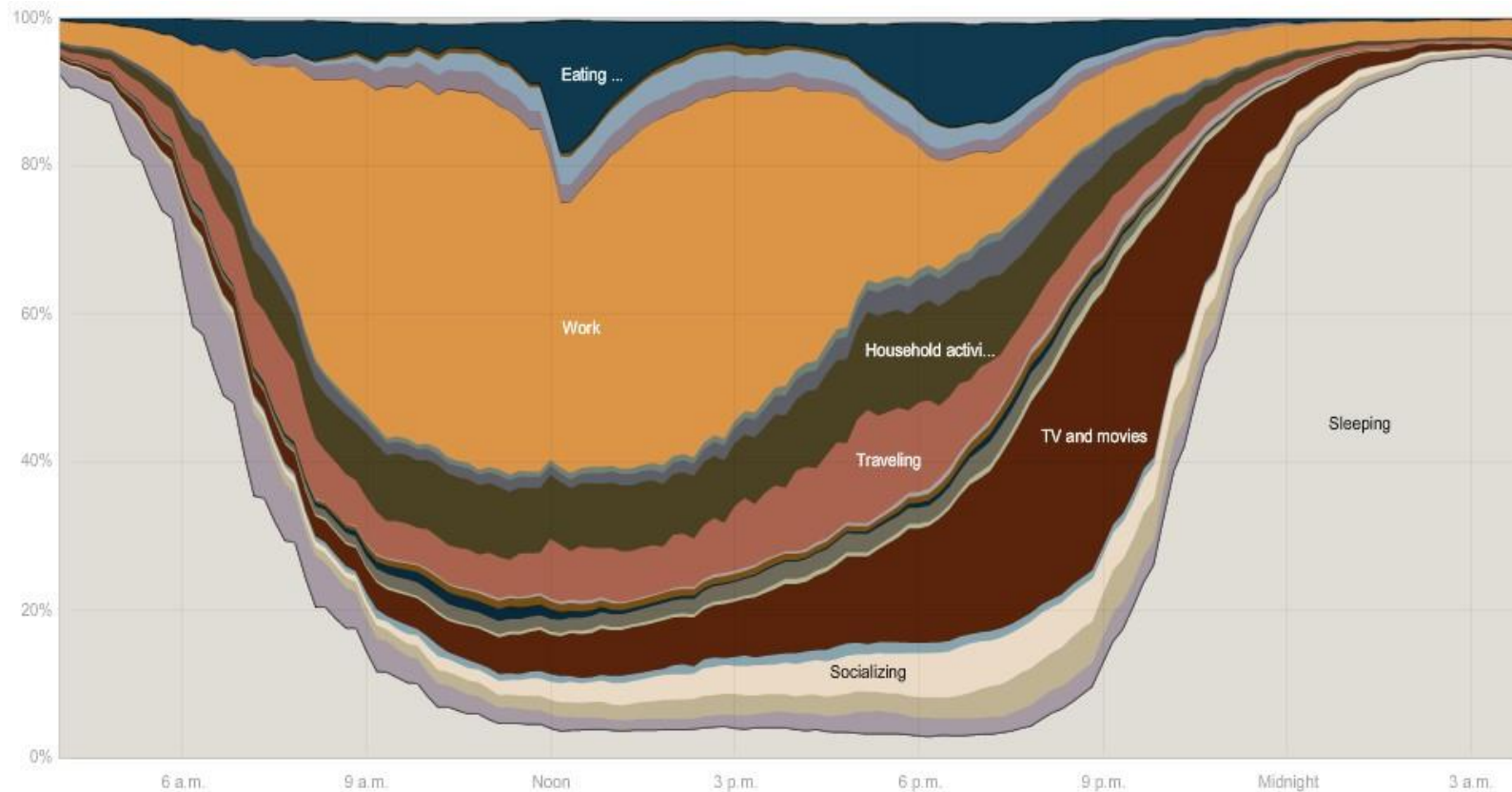
Chart showing the top ten brands' standing over the last three years

# OTHER DATA TYPES



# PROPORTIONS

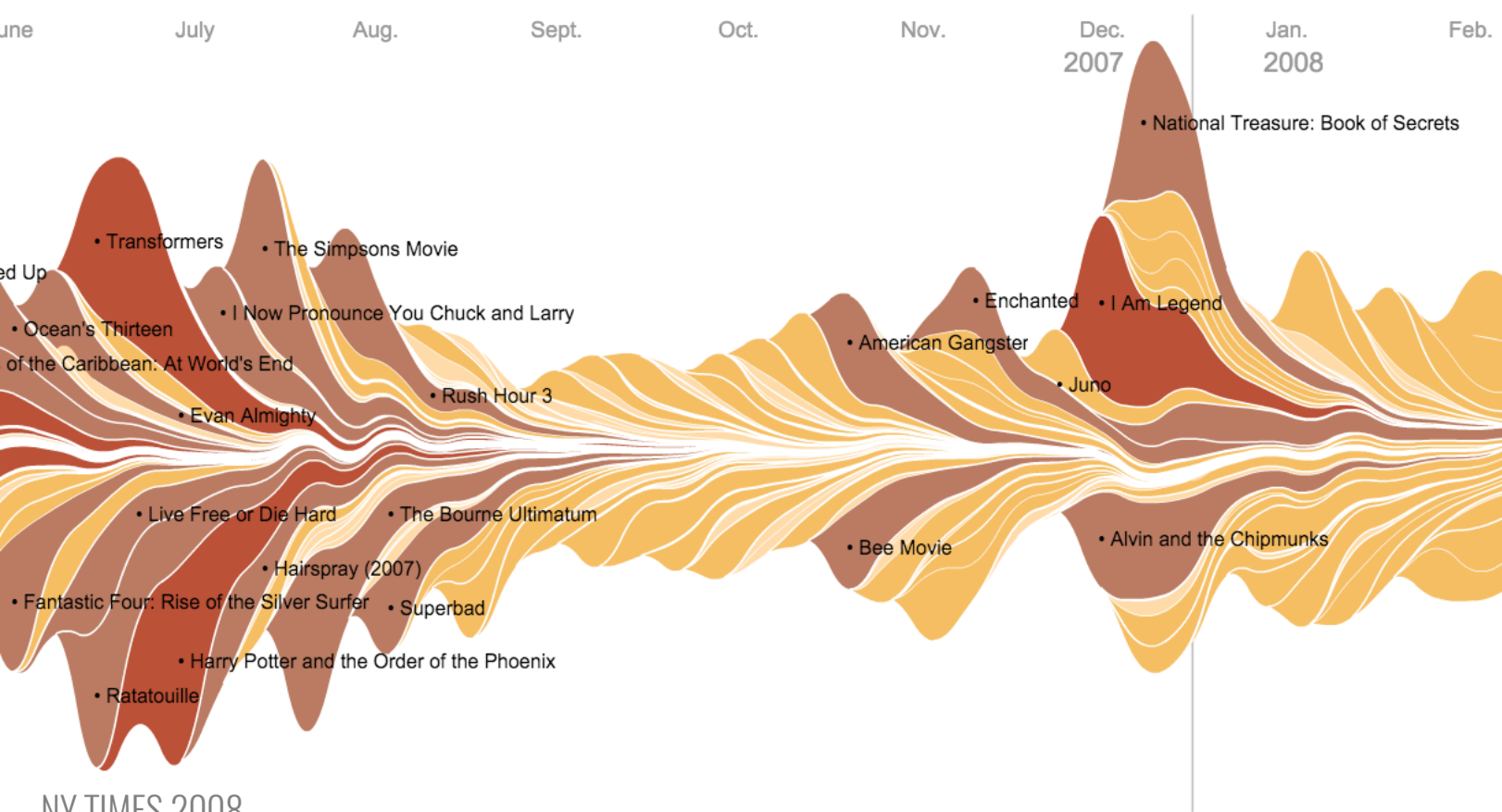
## STACKED AREA CHART



NY TIMES 2009

# PROPORTIONS

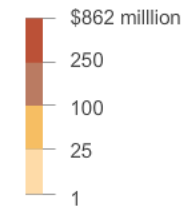
## STREAMGRAPHS



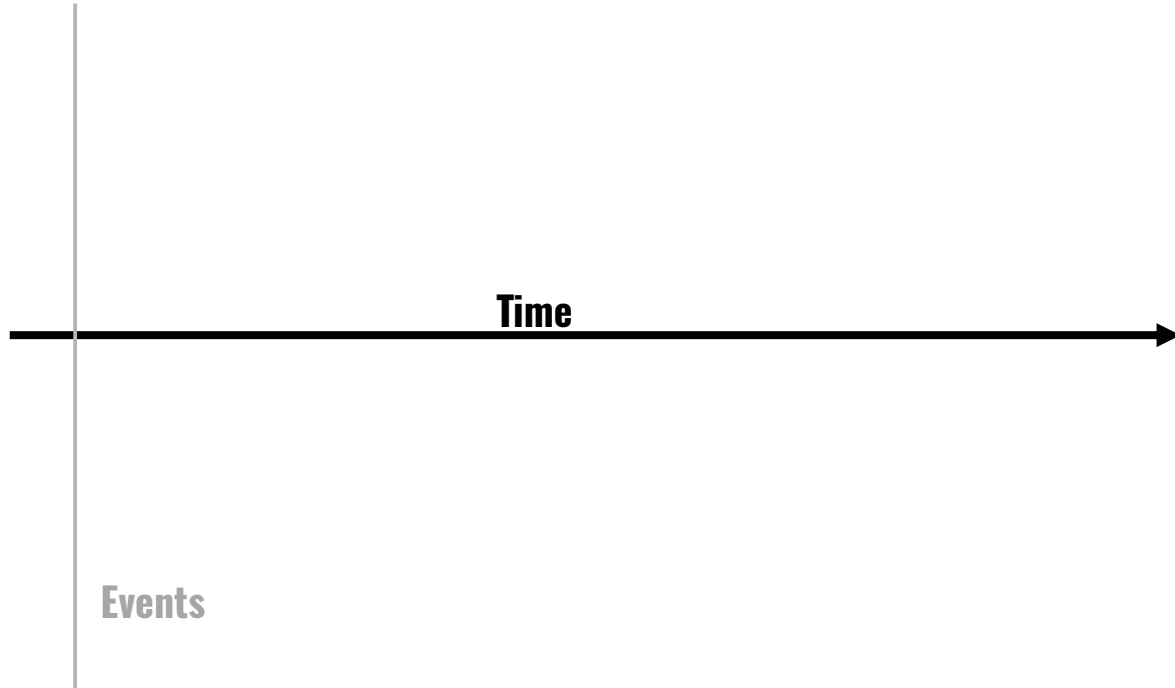
Each shape shows how one film did at the box office.



The **area** of the shape (and its **color**) corresponds to the film's total domestic gross, through Feb. 21



# OTHER DATA TYPES





# OTHER DATA TYPES - EVENTS

LIKE OBSERVATIONS IN TIME-SERIES

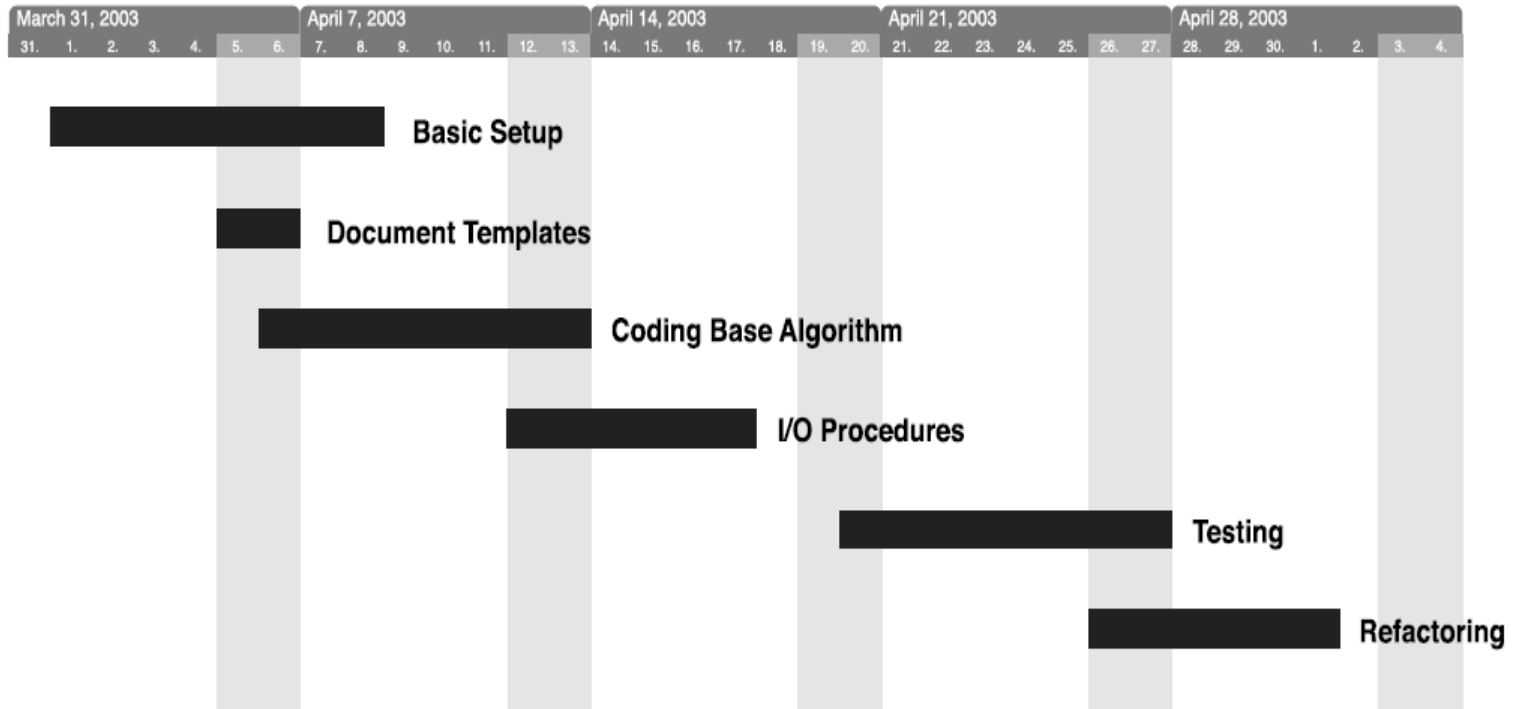
- DATA POINTS WITH A TIME STAMP

BUT

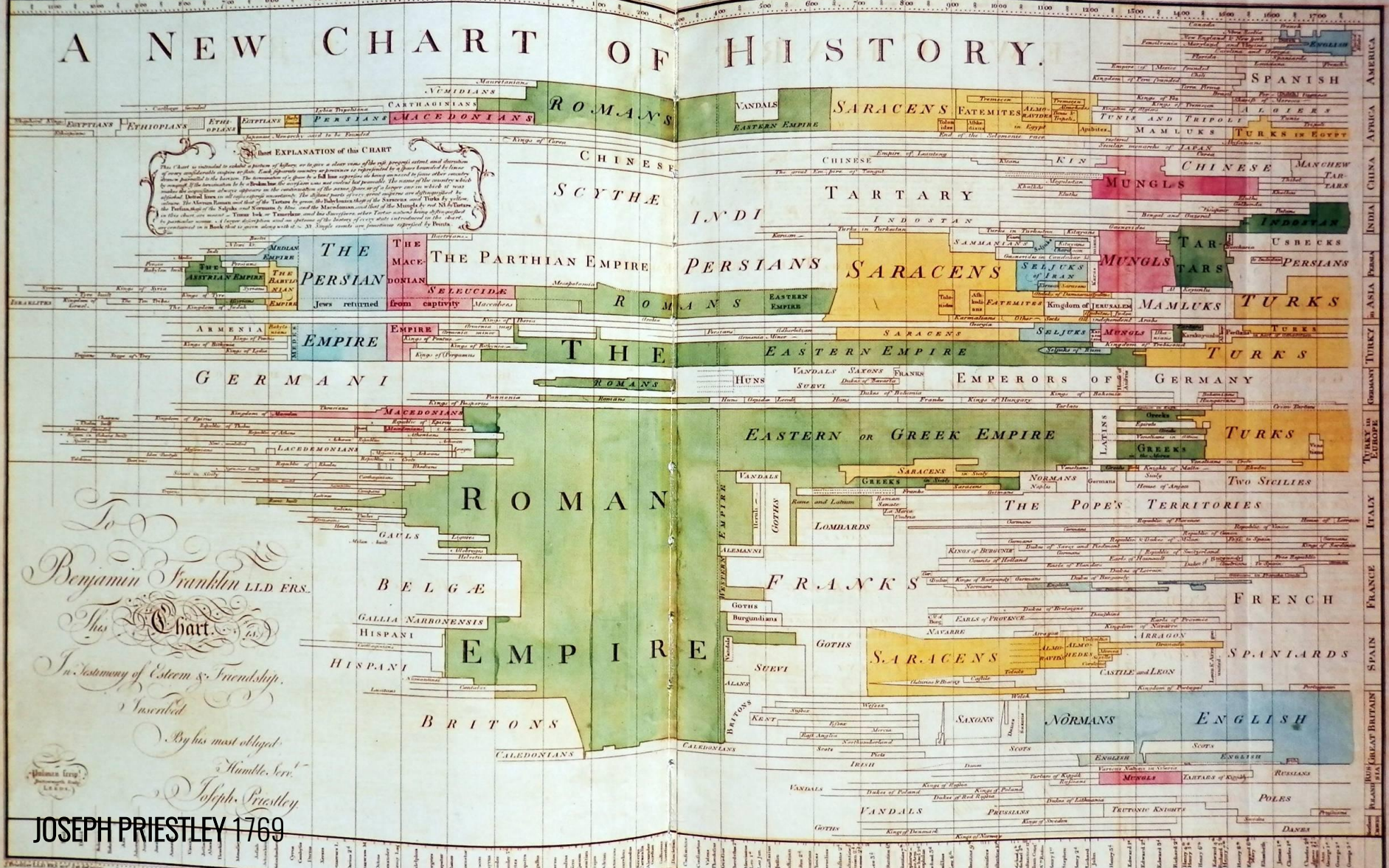
- MOST OFTEN SPARSE AND IRREGULAR
- DATA IS MOSTLY NOMINAL
- CAN HAVE A DURATION (START + END)
- OFTEN SUBJECTIVE / SOCIAL DATA RATHER THAN PHYSICAL MEASURES

# EVENTS

## PROJECT TIMELINE



# A NEW CHART OF HISTORY.



**EXPLANATION OF THIS CHART**  
This Chart is intended to exhibit a picture of History, as to give a clear view of the rise progress, extent and duration of every considerable empire or state. Each separate country or province is represented by a square bounded by lines. The time of its rise is shown by the full line extending to the year of its coming to its height. The time of its decline is shown by the broken line. The names of the countries which have been mentioned above appear in the continuation of the same. Some of a longer size in which it was situated. Other lines in red signify conquests. The different parts of every great empire are distinguished by the letters A, B, C, D, E, F, G, H, I, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z. The names of the several Kings and Queens are also distinguished by the letters A, B, C, D, E, F, G, H, I, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z. In this chart are inserted the names of the several Kings and Queens who have reigned in the several countries mentioned above. The names of the several Kings and Queens are also distinguished by the letters A, B, C, D, E, F, G, H, I, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z. In this chart are inserted the names of the several Kings and Queens who have reigned in the several countries mentioned above. The names of the several Kings and Queens are also distinguished by the letters A, B, C, D, E, F, G, H, I, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z.

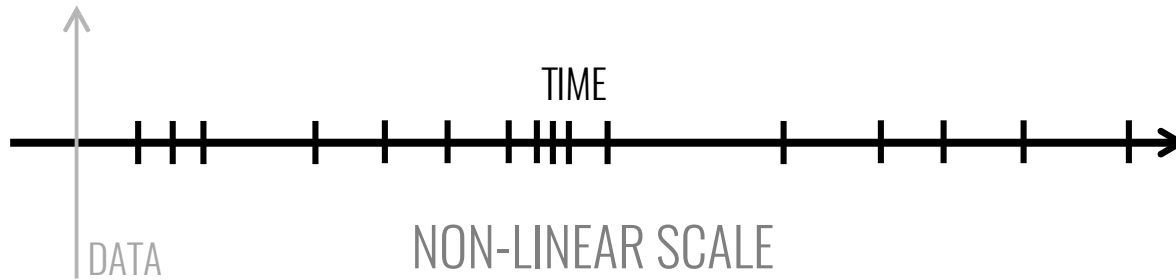
To  
Benjamin Franklin LLD. FRS.  
This Chart  
In testimony of Esteem & Friendship,  
Presented

By his most obliged  
& Humble Serv<sup>t</sup>  
Joseph Priestley

JOSEPH PRIESTLEY 1769

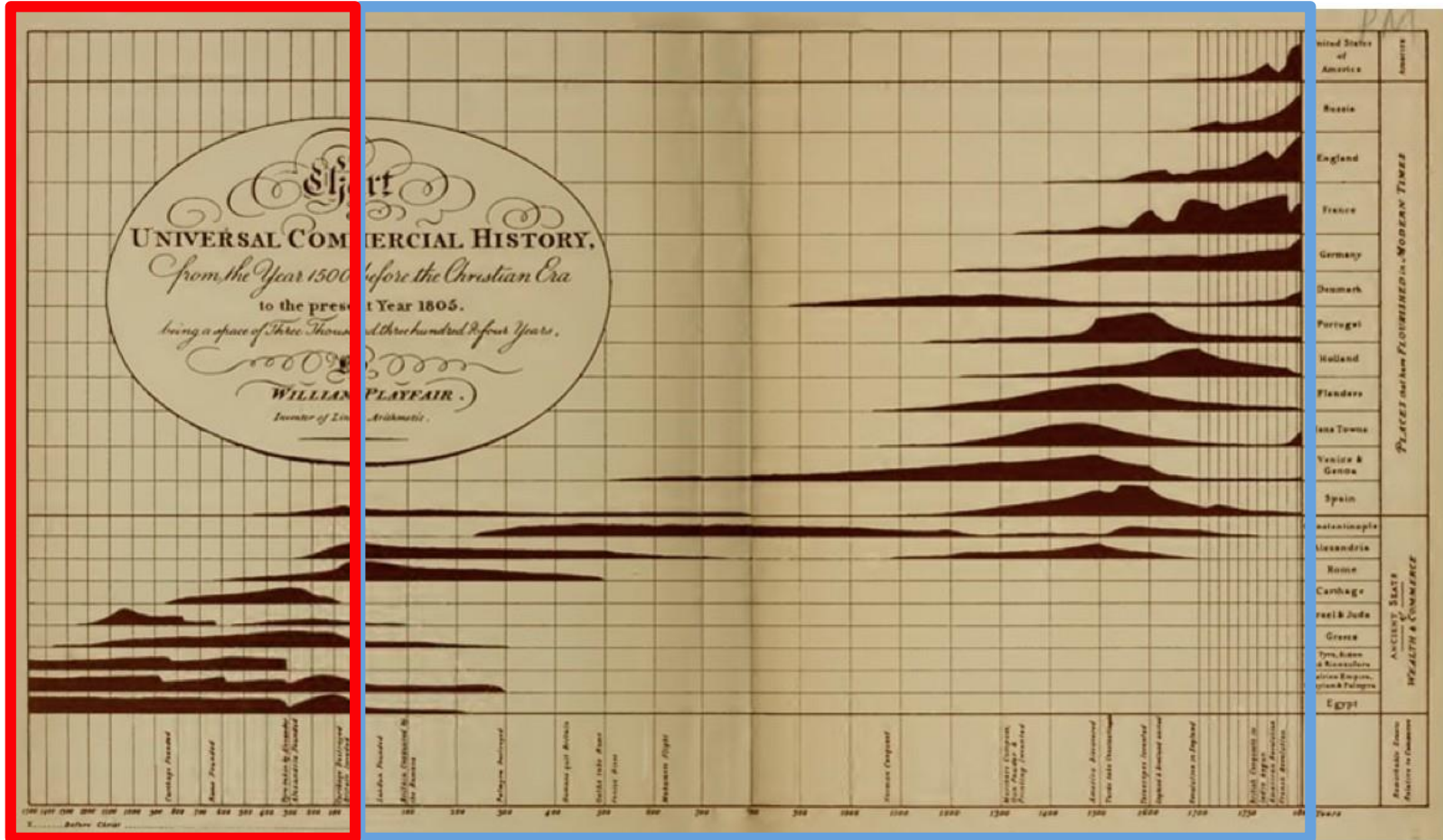
# MAPPING TIME TO AN AXIS

# NON-LINEAR TIME AXES

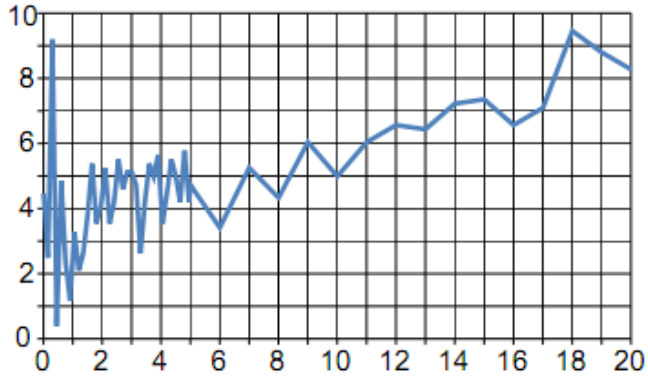


# DUAL-SCALE CHARTS

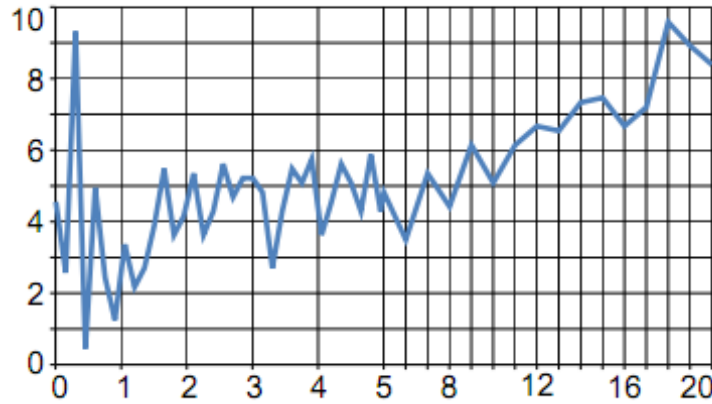
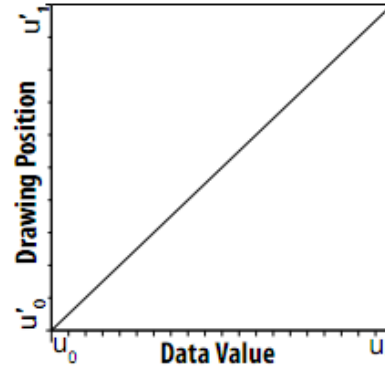
WILLIAM PLAYFAIR  
1805



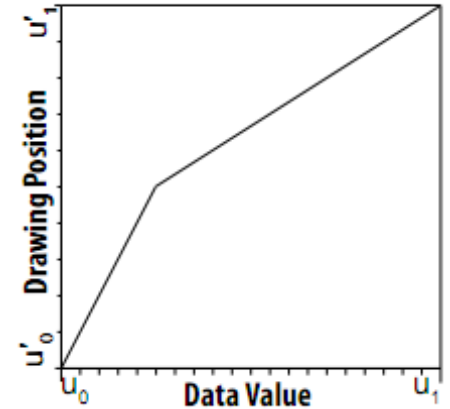
# DUAL-SCALE CHARTS



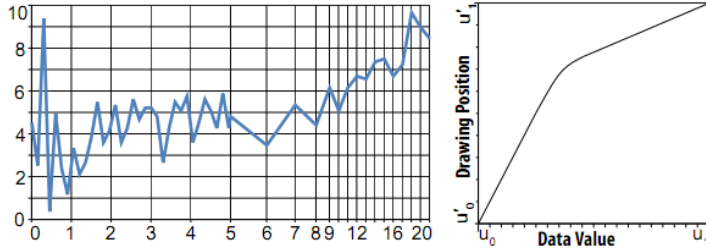
REGULAR CHART



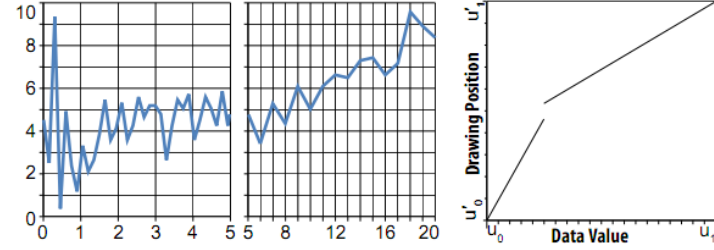
BIFOCAL CHART



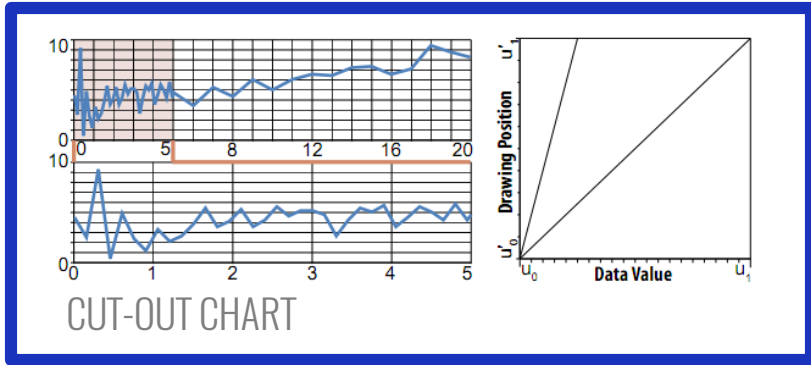
# DUAL-SCALE CHARTS



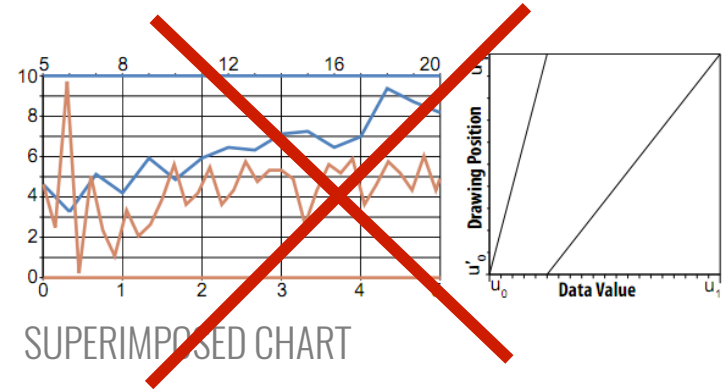
LENS CHART



BROKEN CHART



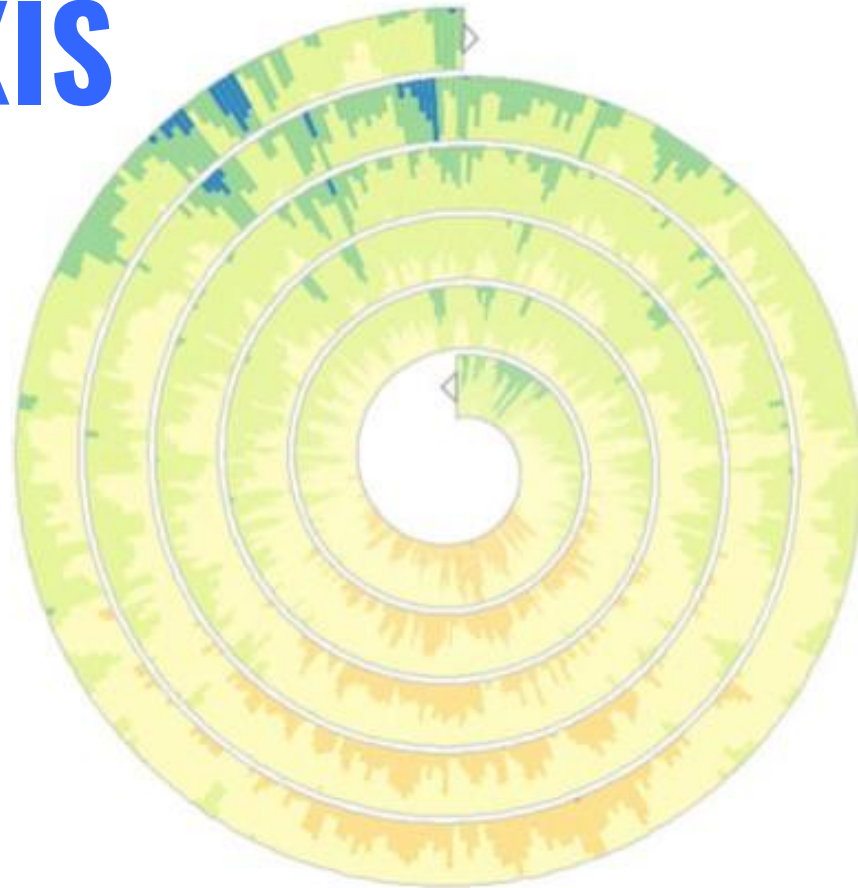
CUT-OUT CHART



SUPERIMPOSED CHART



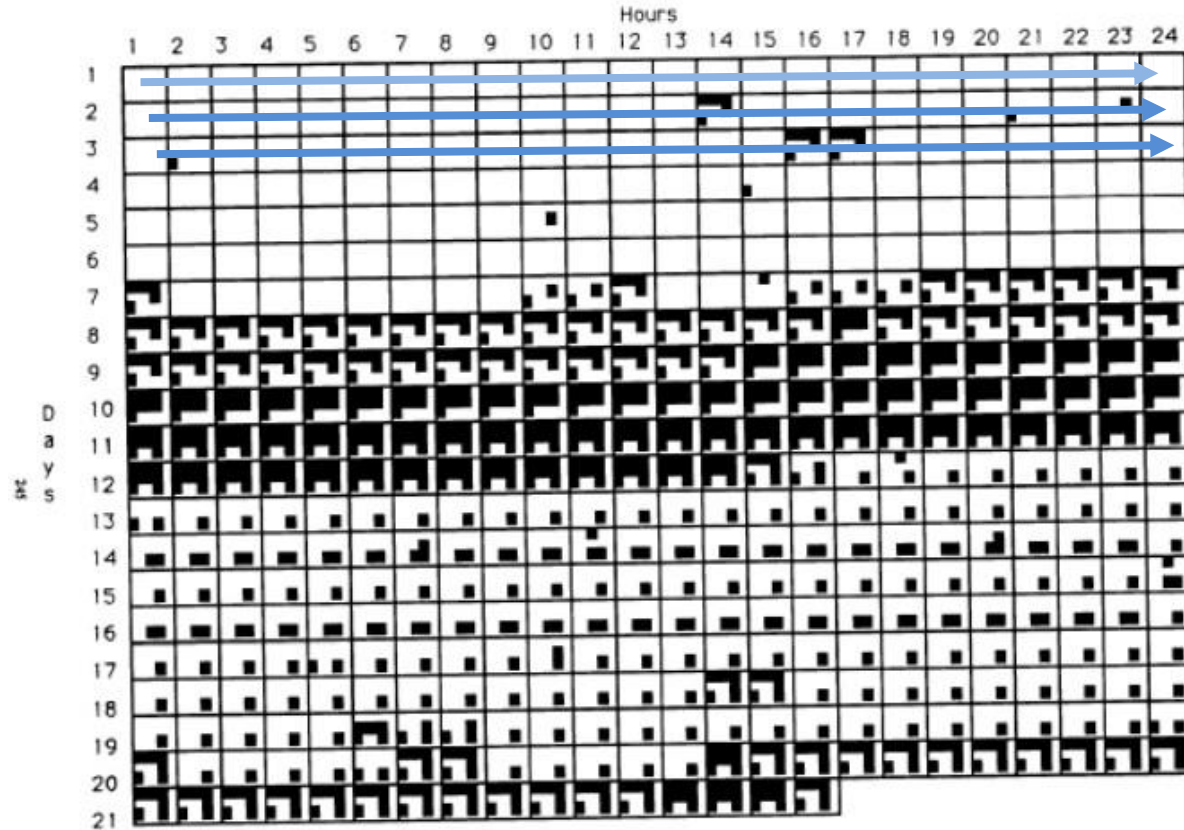
# SPIRAL AXIS



AIGNER ET AL 2011

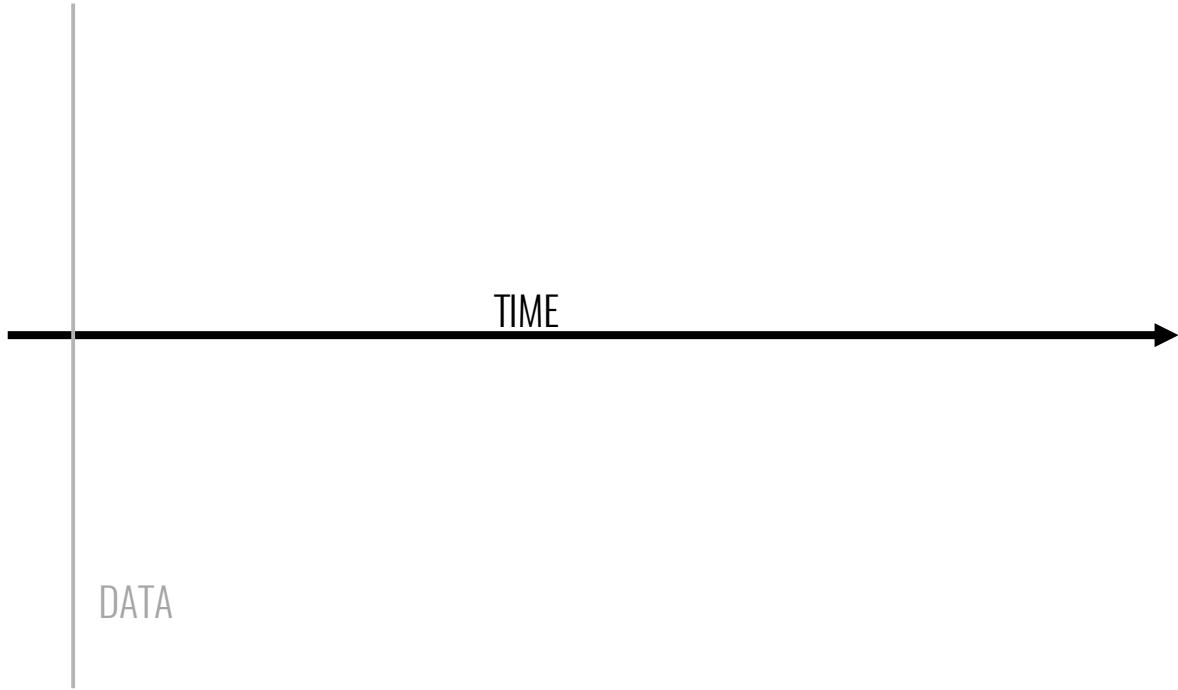


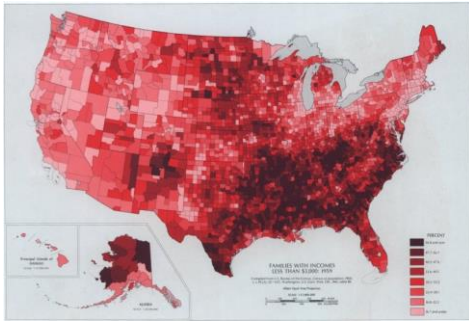
# GRID AXIS



Day by Hour: Thirteen Parameters of Magnetosphere and Solar Wind Data

# MAPPING TIME AND SPACE





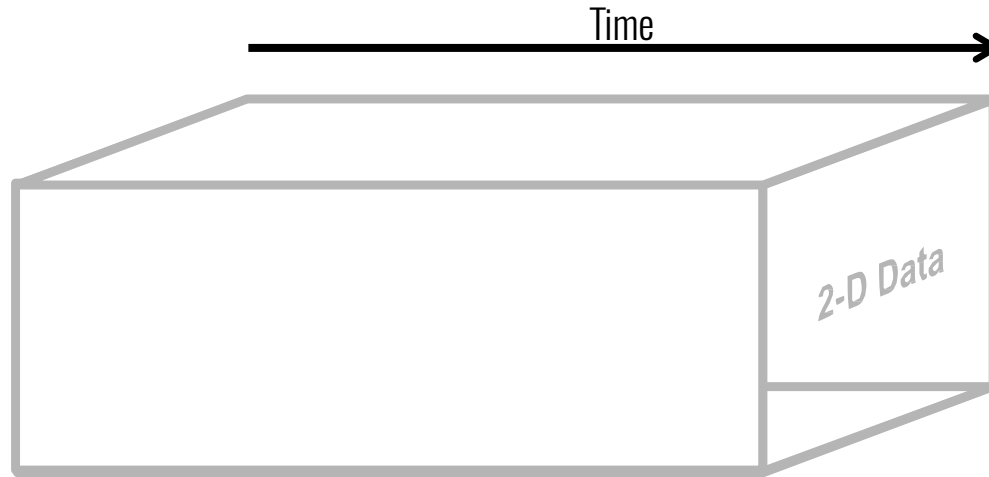
TIME



DATA

# 2D + TIME

SPACE-TIME CUBE MODEL



# DISCRETE TIME FLATTENING

## SEQUENCES

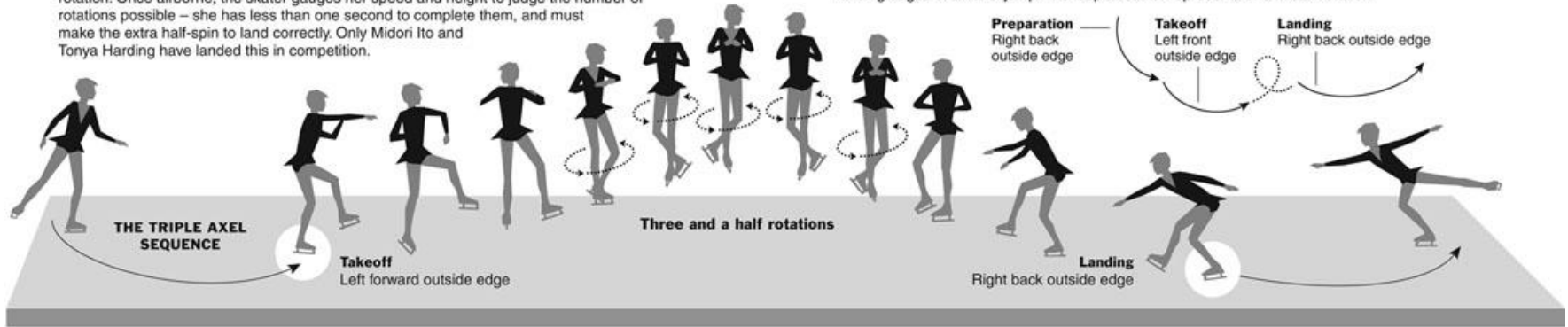
### The Jumping Off Points: Moves That Will Be Made in the Free Skating Programs

#### TRIPLE AXEL: Add an extra half-spin

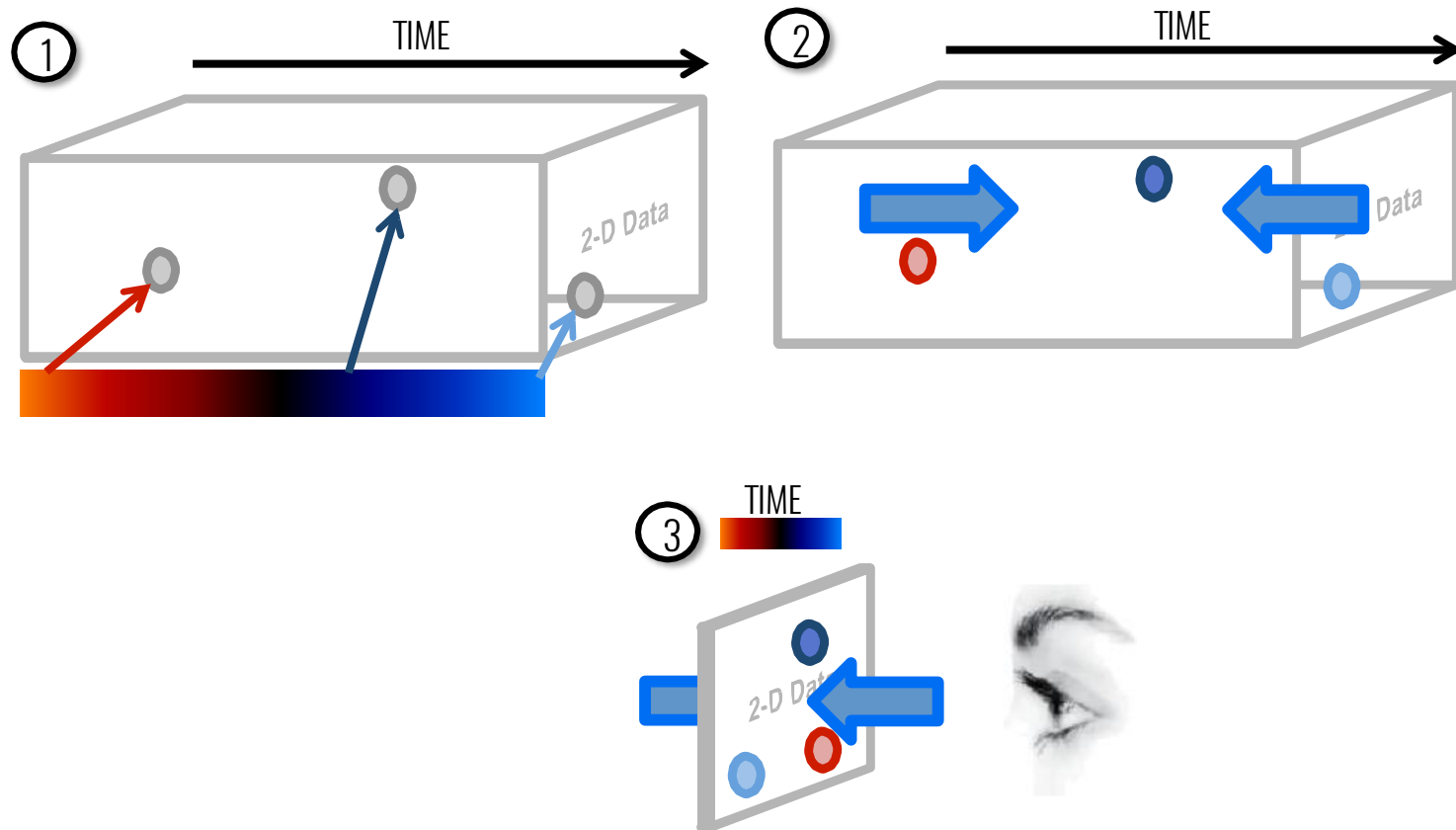
The axel's forward takeoff and backward landing positions add an extra half-rotation to the jump, so skaters need maximum power on takeoff, and precise upper body control during rotation. Once airborne, the skater gauges her speed and height to judge the number of rotations possible – she has less than one second to complete them, and must make the extra half-spin to land correctly. Only Midori Ito and Tonya Harding have landed this in competition.

#### SKATING THE EDGES: An overhead view of the axel

In skating terminology, the path of a jump is described as a series of edges – semicircular arcs that follow the path of the skate blade. The diagram shows the preparatory, takeoff and landing edges of an axel jump. The loop at center represents one midair rotation.



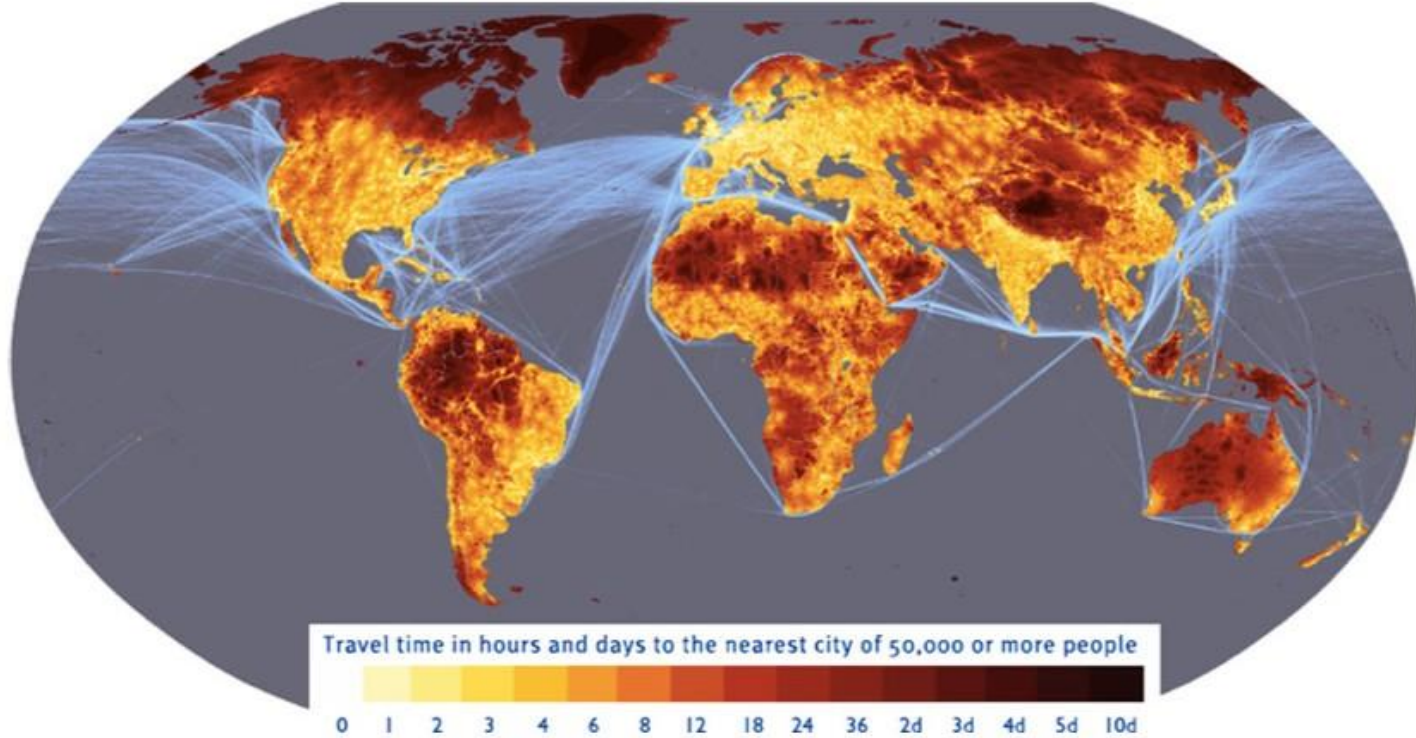
# COLORED TIME FLATTENING





# COLORED TIME FLATTENING

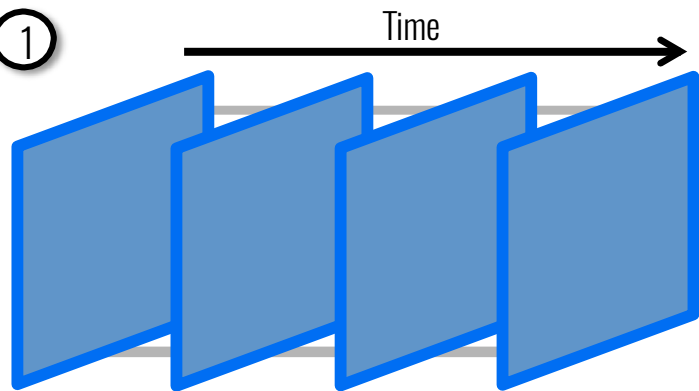
TRAVEL TIMES



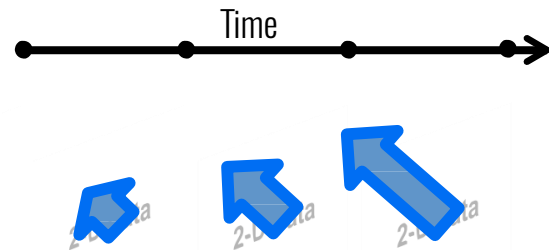
NELSON 2008

# TIME JUXTAPOSING

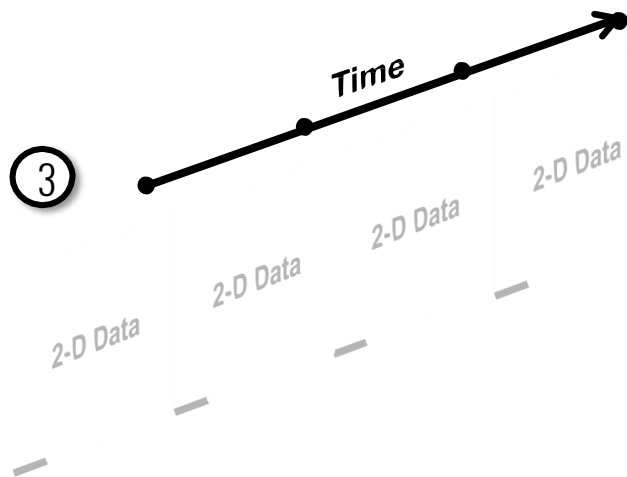
①



②

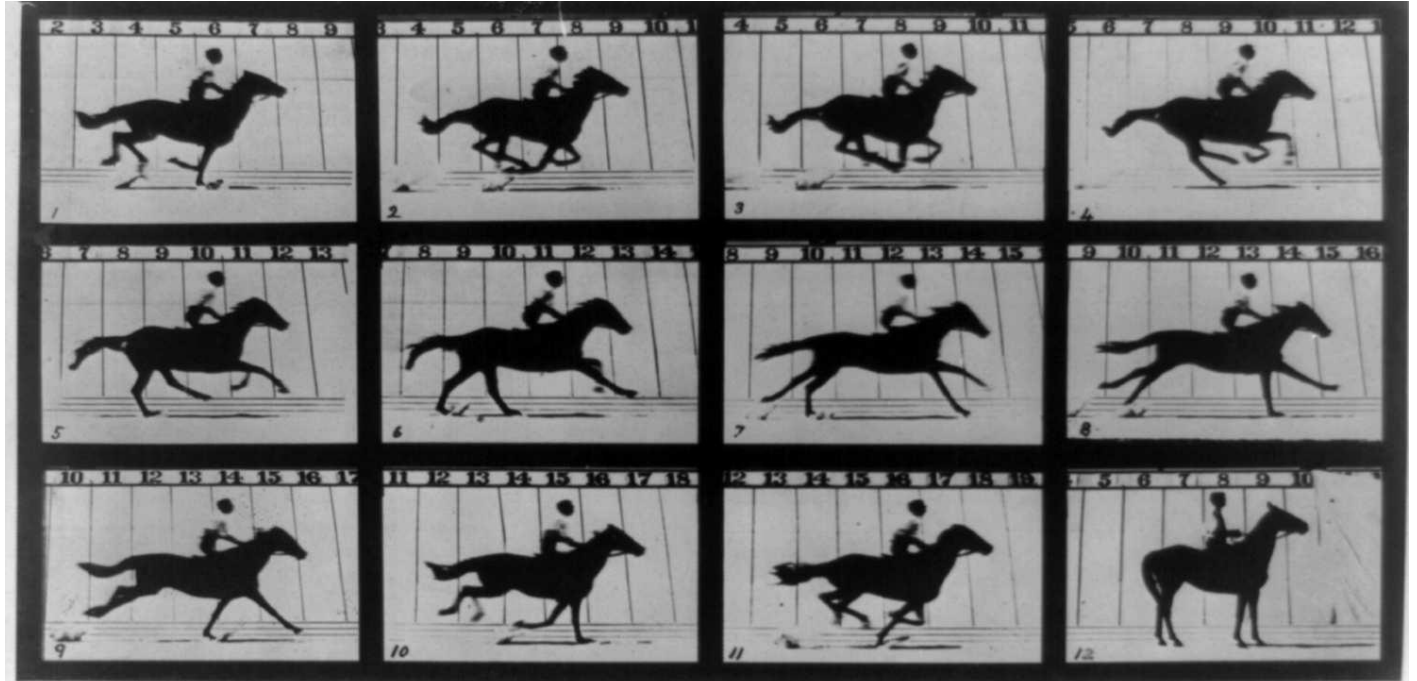


③



# TIME JUXTAPOSING

MUYBRIDGE'S CHRONOPHOTOGRAPHY TECHNIQUE



Copyright, 1878, by MUYBRIDGE.

MORSE'S Gallery, 417 Montgomery St., San Francisco

## THE HORSE IN MOTION.

Illustrated by  
MUYBRIDGE.

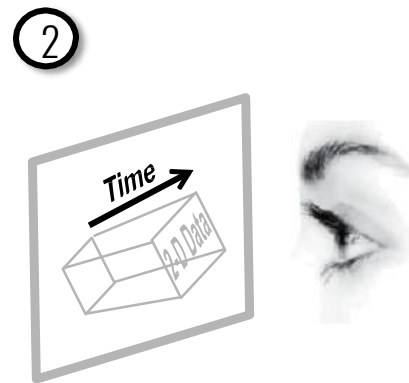
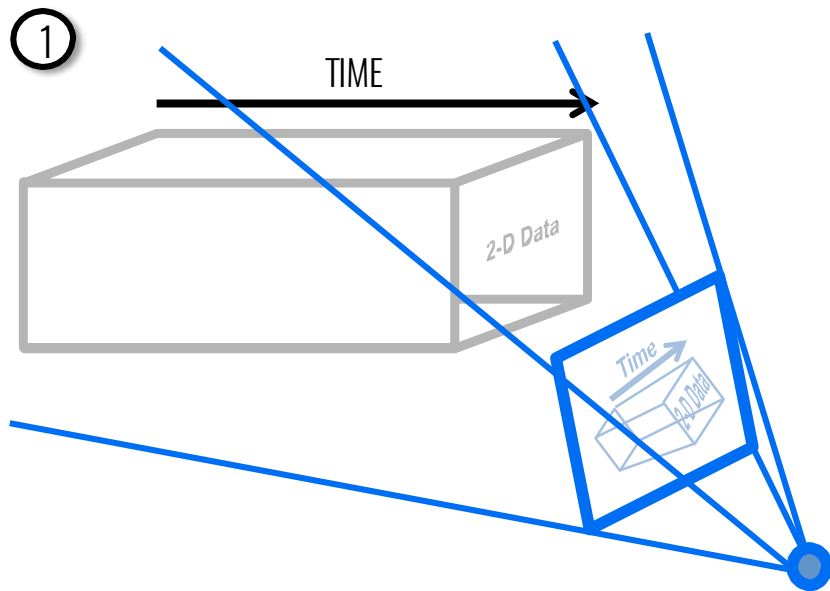
AUTOMATIC ELECTRO-PHOTOGRAPH.

Patent for apparatus applied for. "SALLIE GARDNER," owned by LELAND STANFORD; ridden by G. DOMM, running at a 1.40 gait over the Palo Alto track, 19th June, 1878.

The negatives of these photographs were made at intervals of twenty-seven inches of distance, and about the twenty-fifth part of a second of time; they illustrate consecutive positions assumed during a single stride of the mare. The vertical lines were twenty-seven inches apart; the horizontal lines represent elevations of four inches each. The negatives were each exposed during the two-thousandth part of a second, and are absolutely "unstitched."

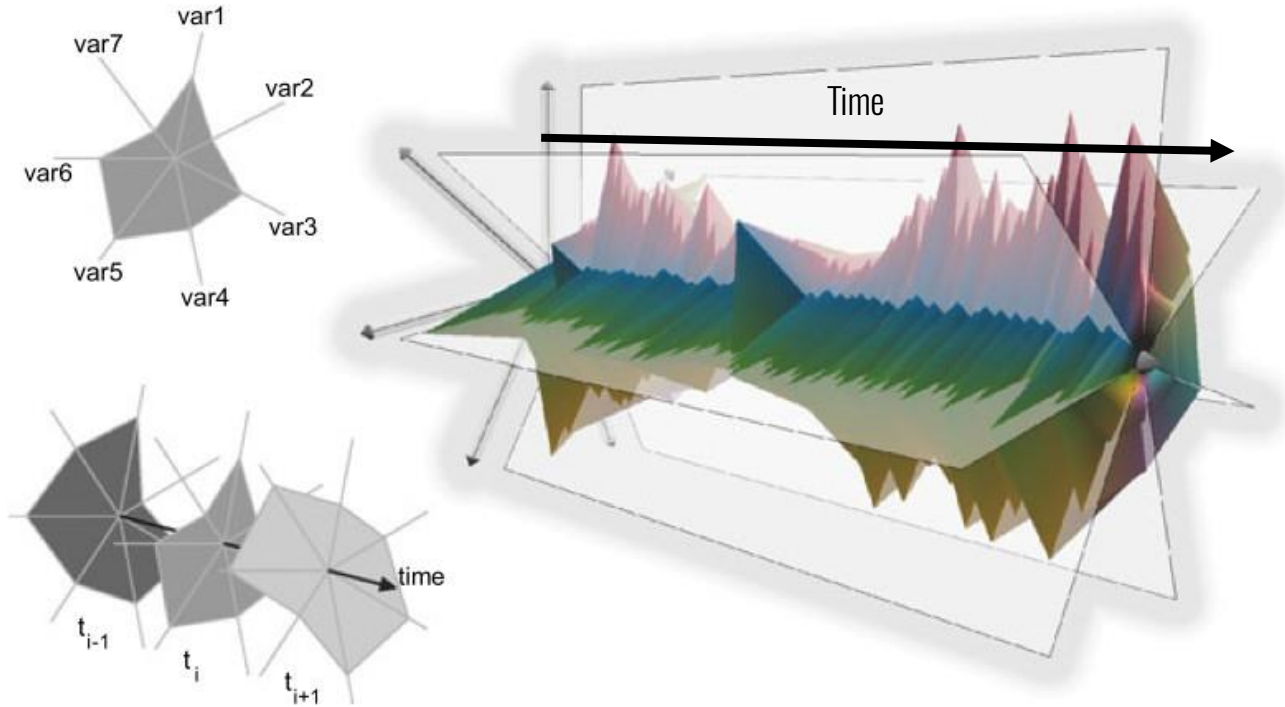
MUYBRIDGE 1878

# 3D RENDERING



# 3D RENDERING

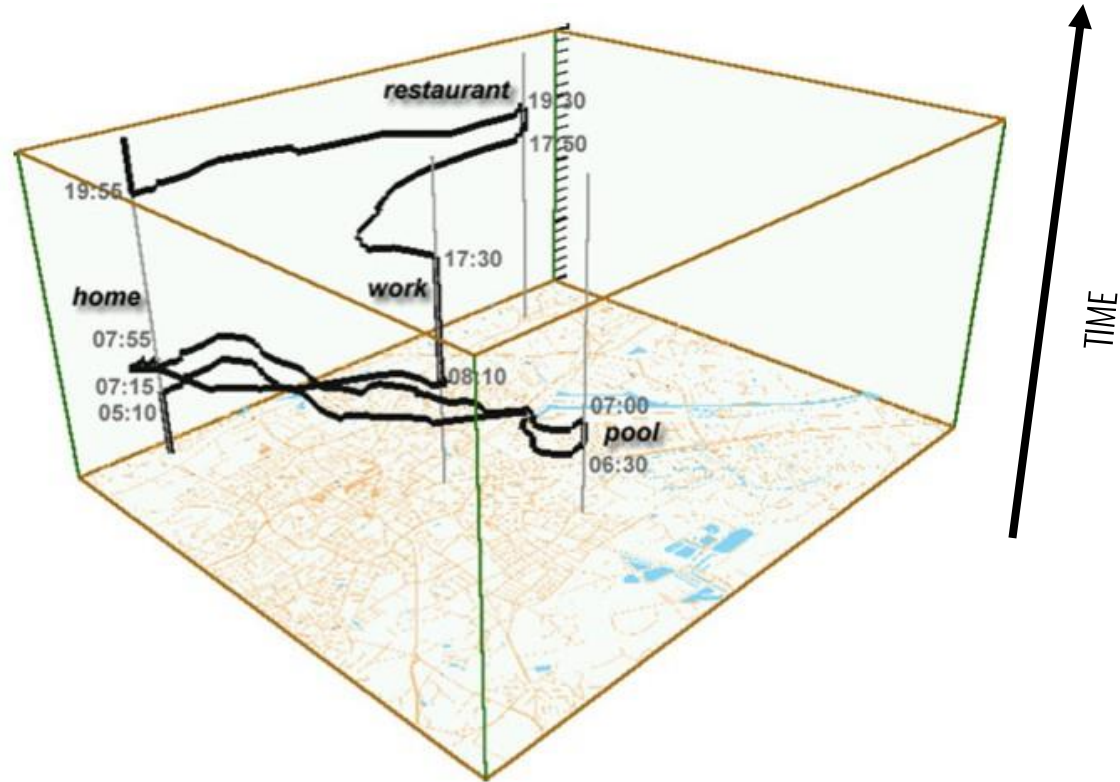
KIVIAT TUBE



AIGNER ET AL 2011

# 3D RENDERING

## PATHS



# The TimeViz Browser

A Visual Survey of Visualization Techniques for Time-Oriented Data  
by Christian Tominski and Wolfgang Aigner

# of Techniques: 115

Search:

How to use:  
**Want** - I want to see.  
**?** - I'm neutral.  
**Hide** - Don't show me.

## Data

Frame of Reference

- Abstract
- Spatial

Number of Variables

- Univariate
- Multivariate

## Time

Arrangement

- Linear
- Cyclic

Time Primitives

- Instant
- Interval

Display a menu





# Timeline Storyteller

CONTACT US TOP

## Examples

Preparing data

How do I use it?

Source code

Acknowledgements

## Project Team:

Matthew Brehmer

Bongshin Lee

Nathalie Henry

Riche

Darren Edge

Christopher White

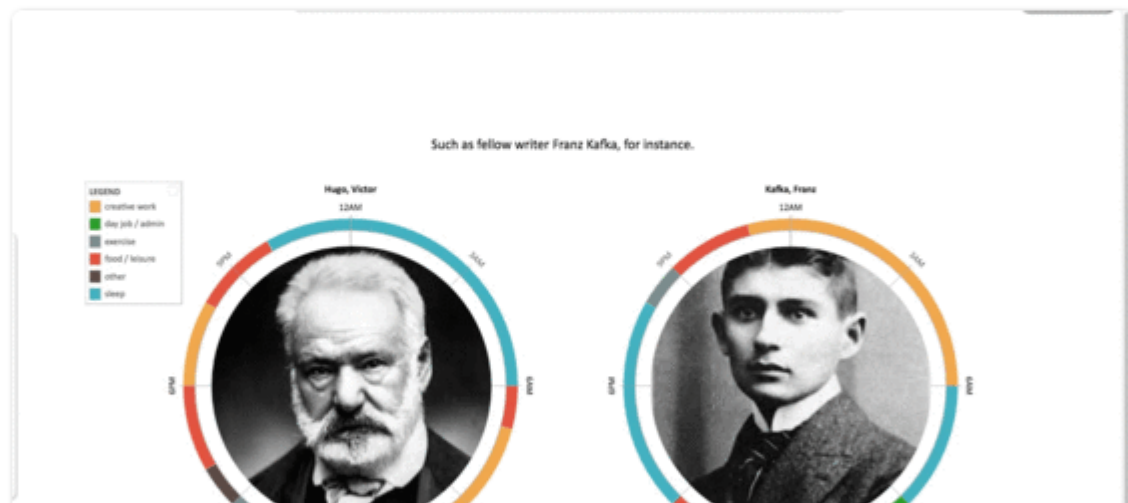
Kate Lytvynets

David Tittsworth



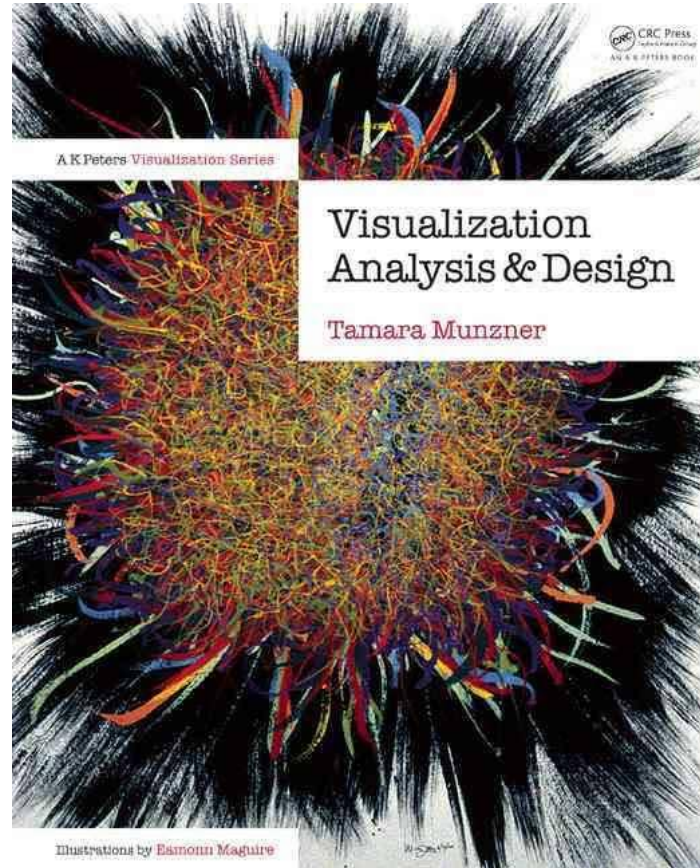
**Timeline Storyteller** is an open-source expressive visual storytelling environment for presenting timelines in the browser or in Microsoft Power BI.

Use it to present different aspects of timeline data using a palette of timeline representations, scales, and layouts, as well as controls for filtering, highlighting, and annotation.





# READINGS



# ACKNOWLEDGEMENTS

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- Wesley Willett (University of Calgary)
- Pierre Dragicevic (Inria)
- Uta Hinrichs (University of St. Andrews)